

Diagnostic statistical analyses to detect the seismicity and geodetic anomalies relative to the normal predictions

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and

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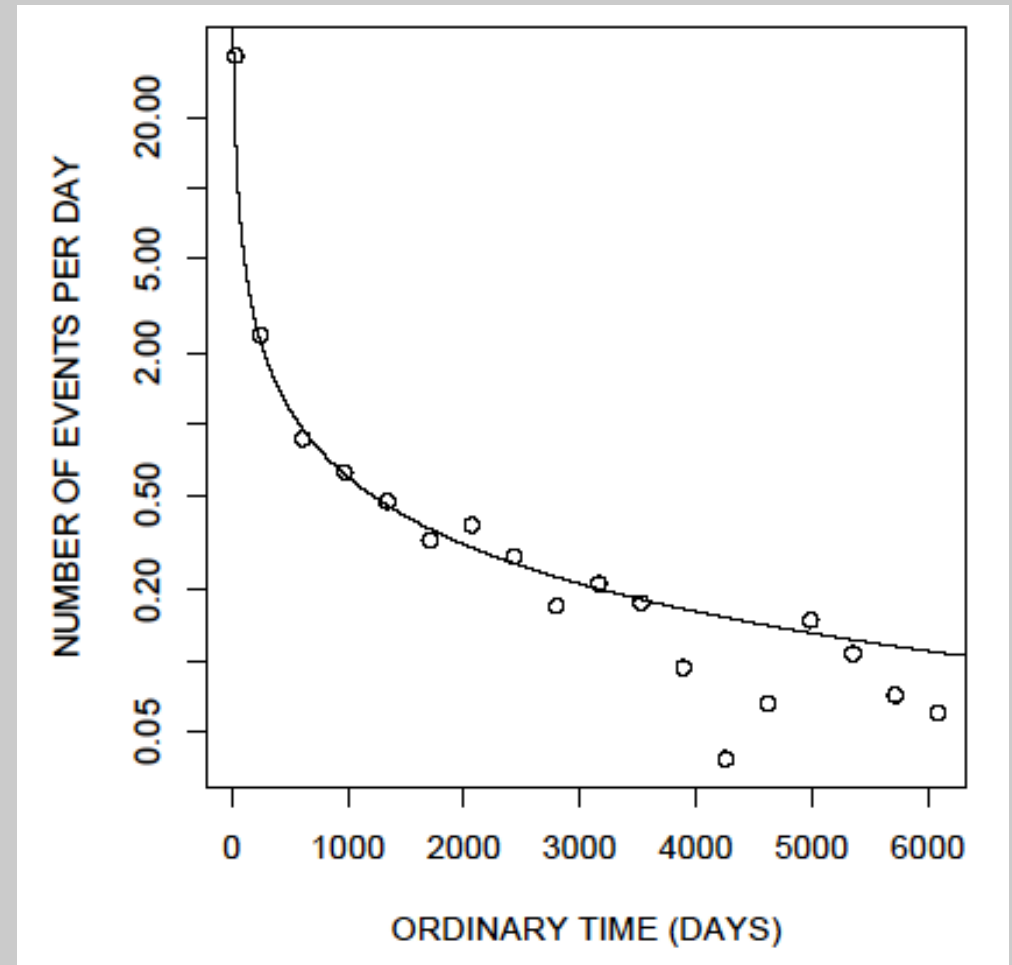
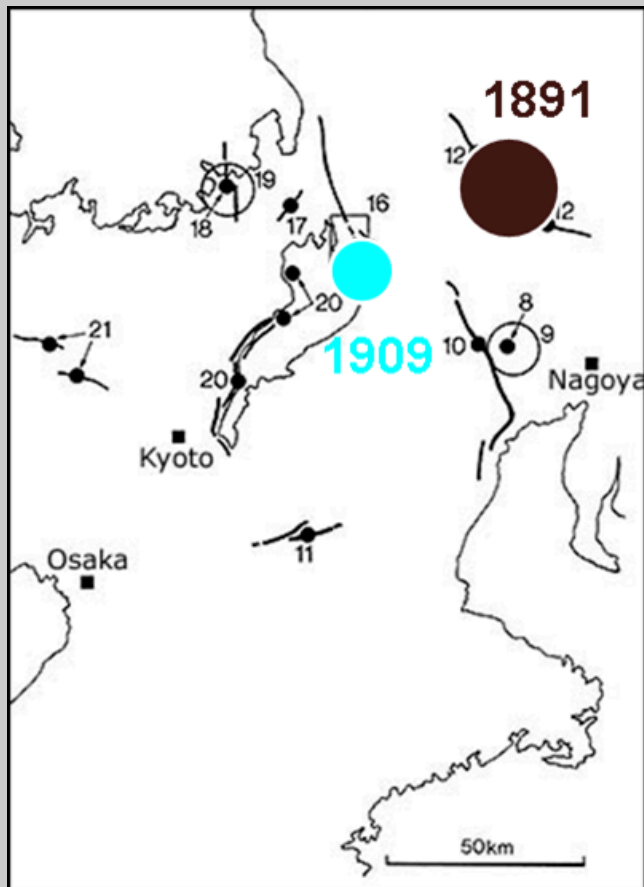
Aftershocks



Omori (1894)

$$n(t) = K(t + c)^{-1}$$

1891 Nobi Earthquake of M8.1



Utsu (1961)

The Omori-Utsu formula for aftershock decay rate

$$v(t) = K(t + c)^{-p}$$

t : Elapsed time from the mainshock

K , c , p : constant parameters

Utsu (1961, 1969)

1891 Nobi (M8) Aftershock freq.

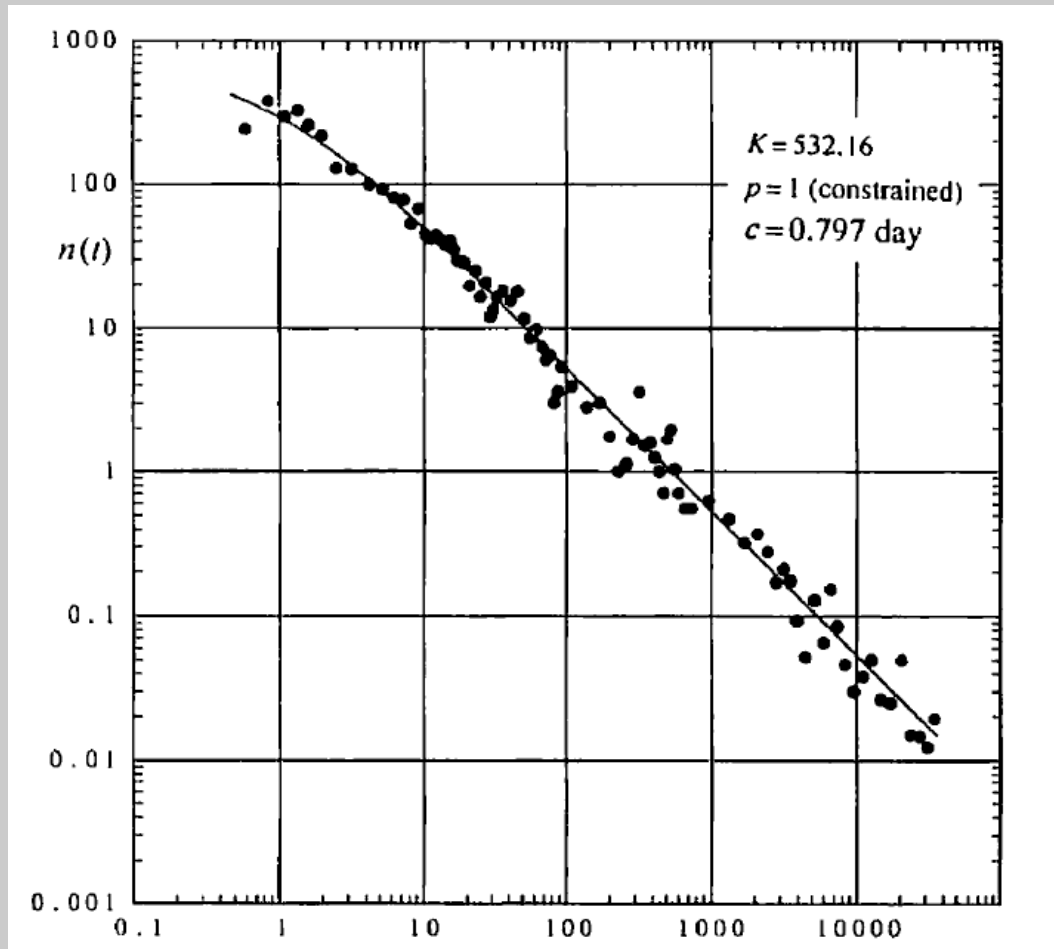


Fig. 1. Occurrence rate (top) and cumulative number (bottom) of felt earthquakes at Gifu after the Nobi earthquake of 1891. Smooth curves represent the Omori formula fitted to the data.

Data from Omori (1895) and Utsu (1969)

Ogata (1983, *J. Phys. Earth*)

Observed time interval: $[S, T]$

Occurrence time data; t_1, t_2, \dots, t_n

Log-likelihood function:

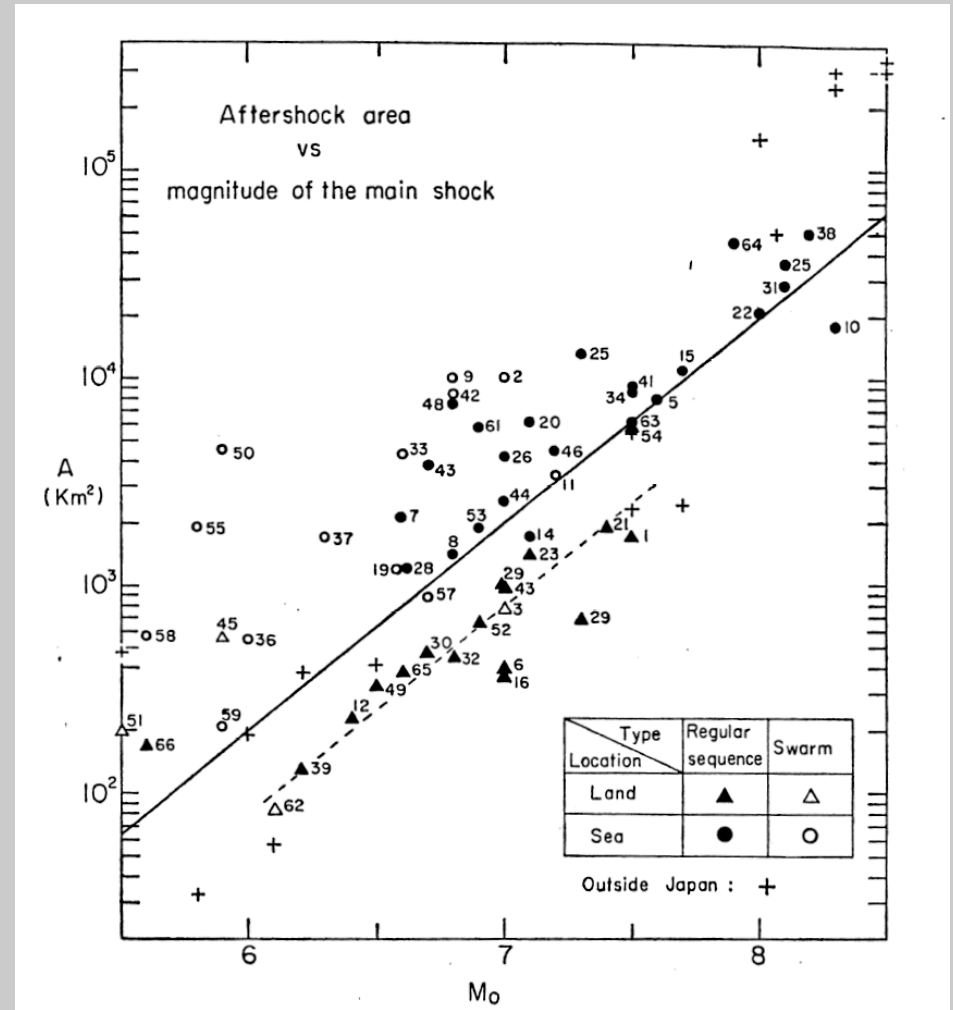
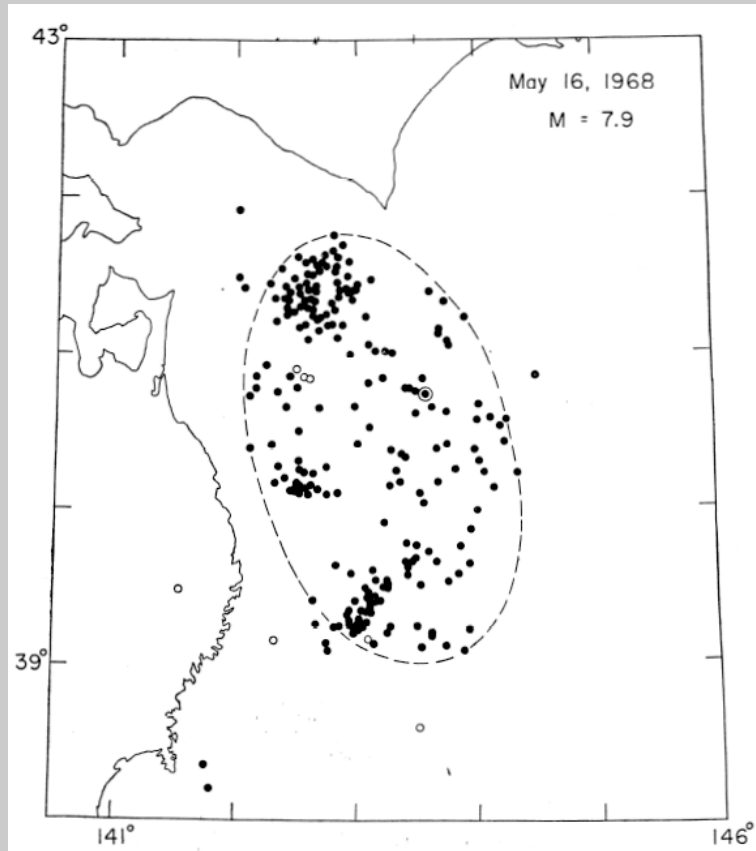
$$\ln L(\theta; S, T) = \sum_{S < t_i < T} \ln \lambda_{\theta}(t_i) - \int_S^T \lambda_{\theta}(t) dt$$

$$l(K, c, p) = \sum_{S < t_i < T} \ln \frac{K}{(t_i + c)^p} - \int_S^T \frac{K}{(t + c)^p} dt$$

Maximum Likelihood Estimate (**MLE**)

Utsu & Seki (1954)

Utsu (1969)



$$\log S = 1.02M - 4.01$$

$$\log L = 0.5M - 1.8$$

Utsu (1970, *Geophys. Bull. Hokkaido Univ.*)

Standard aftershock activity:

Occurrence rate of aftershock of M_s is

$$n(t) = \frac{10^{0.85(M_0 - M_s) - 1.83}}{(t + 0.3)^{1.3}}$$

during $1 < t < 100$ days ($M_0 \geq 5.5$), where
 $p=1.3$, $c=0.3$ and $b=0.85$ are median estimates.

The constant 1.83 is the best fit to 66 aftershock sequences in Japan during 1926-1968

Utsu (1970)

Secondary Aftershocks

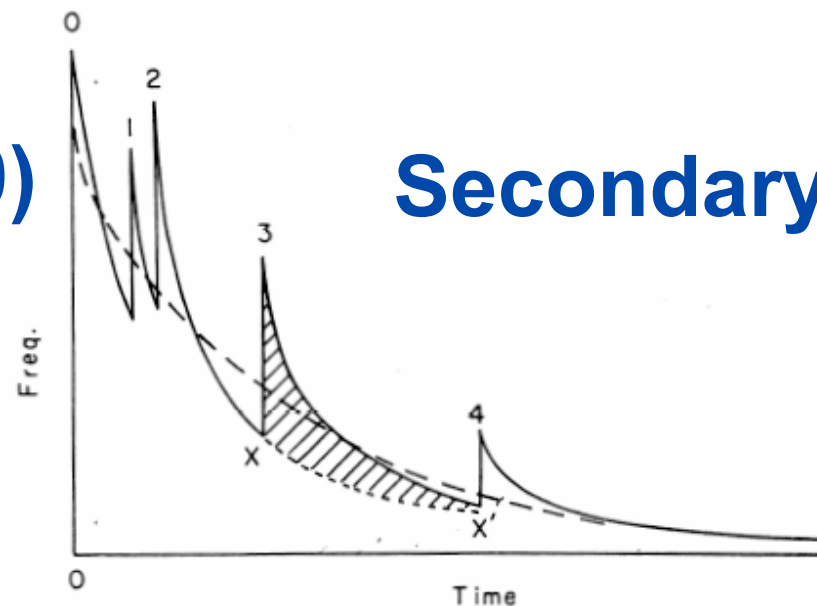
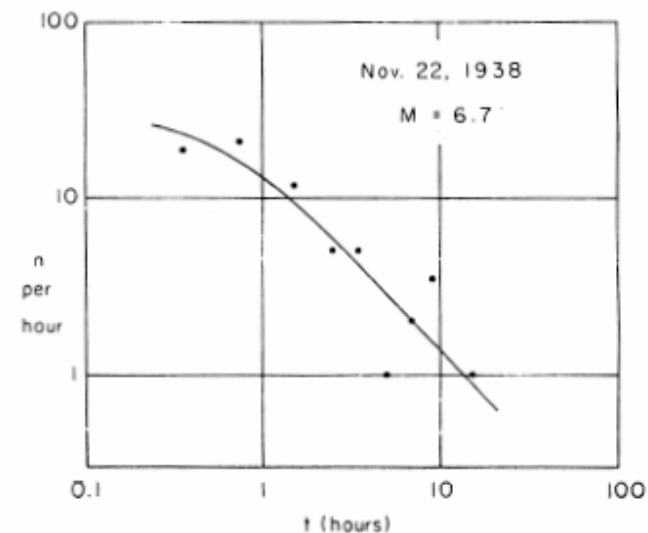
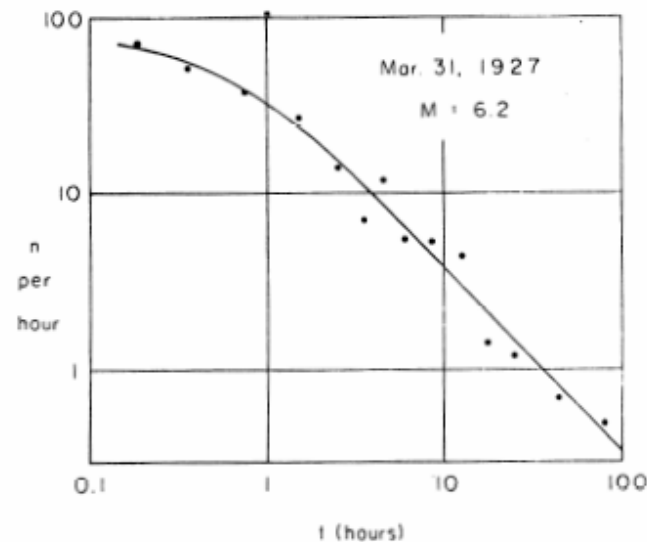


Fig. 105. A schematic graph of Type 1-C aftershock sequence. The broken line represents the curve for the modified Omori formula fitting the whole sequence. The shaded area indicates the secondary aftershocks triggered by shock 3.



Omori-Utsu formula:

$$\nu(t) = \frac{K}{(t + c)^p}$$

ETAS model:

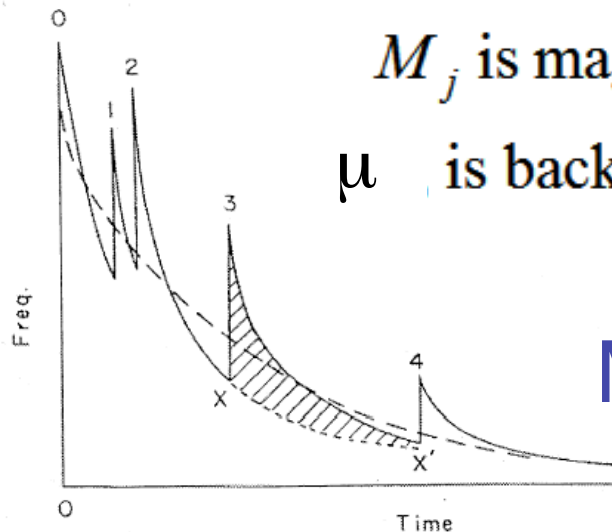
$$\lambda(t) = \mu + \sum_{\{j: t_j < t\}} e^{\alpha\{M_j - M_c\}} \nu(t - t_j)$$

where

t_j is occurrence time of j th event;

M_j is magnitude of j th event;

μ is background rate; and parameters are $(\lambda_0, K, c, \alpha, p)$.



Maximum Likelihood Estimates

Ogata

$$\lambda(t) = \mu + \sum_{t_i < t} c(m_i)g(t - t_i)$$

- Hawkes (1971, *J. Roy. Stats. Soc. B*) Self-exciting process
- Hawkes and Oakes (1974, *JAP*) → Epidemic-type model →
- Kendall (1949, *JRSSB*) Age-dependent birth & death branching process
- Hawkes & Adamopoulos (1973, *Bull. Int. Stats. Inst.*) Cluster earthquake cluster model
- Lomnitz (1974, *Global Tectonics and Earthquake Risk*, Elsevier) Tagged Klondike-type model
- Kagan & Knopoff (1981, *JGR*) Stochastic earthq. synthesis
- Ogata (1981, *IEEE-IT*) Thinning simulation algorithm
- Ogata and Akaike (1982, *JRSSB, AISM*) Maximum Likelihood Estimation

Space-Time ETAS model(Ogata,1998,AISM)

$$\lambda(t, x, y) = \mu + \sum_{\{j: t_j < t\}} \frac{K}{(t - t_j + c)^p} \left\{ \frac{Q_j(x, y)}{e^{\alpha M_j}} + d \right\}^{-q}$$

where

$$Q_j(x, y) = (x - x_j, y - y_j) S_j \begin{pmatrix} x - x_j \\ y - y_j \end{pmatrix}$$

Heterogeneity in Space

$$\mu \implies \mu(x, y);$$

$$K \implies K(x_j, y_j); \quad \alpha \implies \alpha(x_j, y_j);$$

$$p \implies p(x_j, y_j); \quad q \implies q(x_j, y_j)$$

Hierarchical Space-Time (HIST) ETAS model

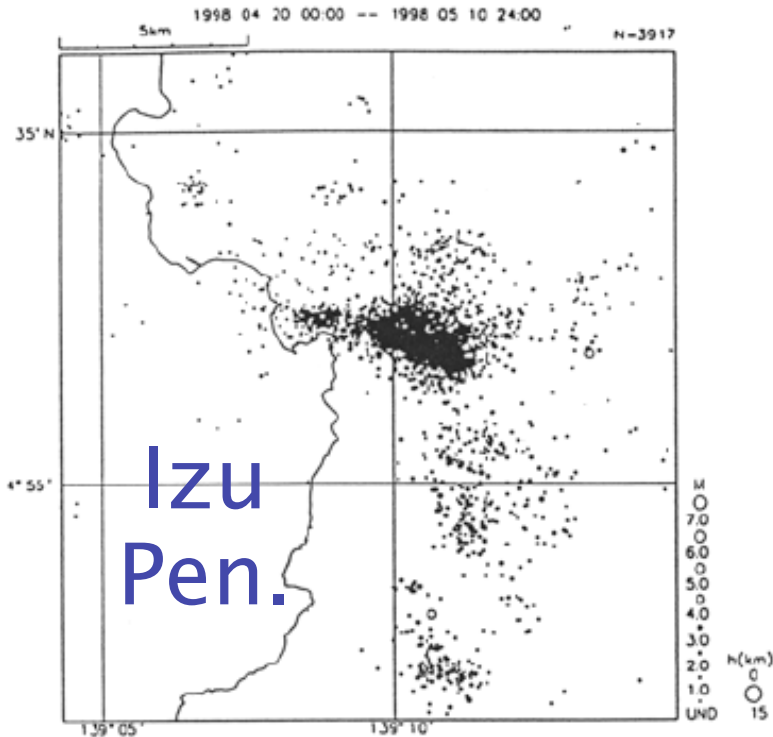
estimated an Objective Bayesian method with smoothness constraints

Ogata(2003,JGR)

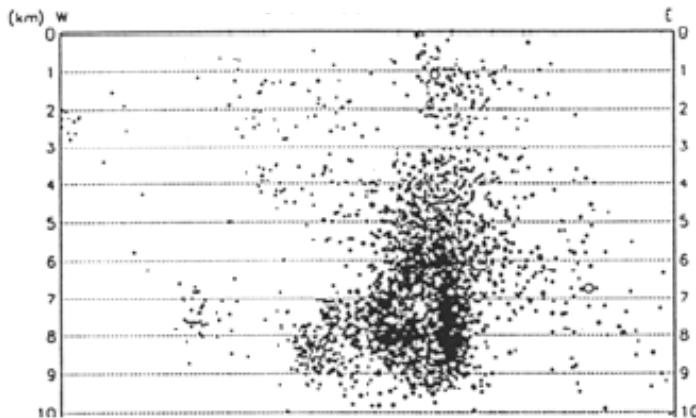
Off the East coast of Izu Peninsula Swarm

11-2

LATITUDE



LONGITUDE

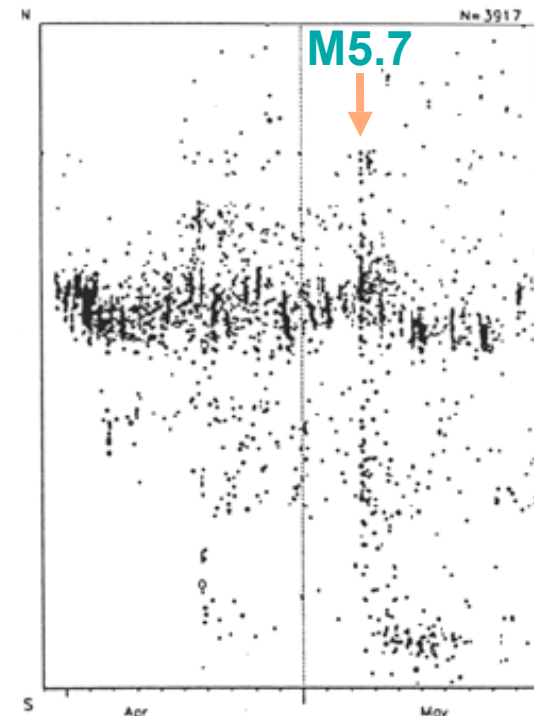


DEPTH

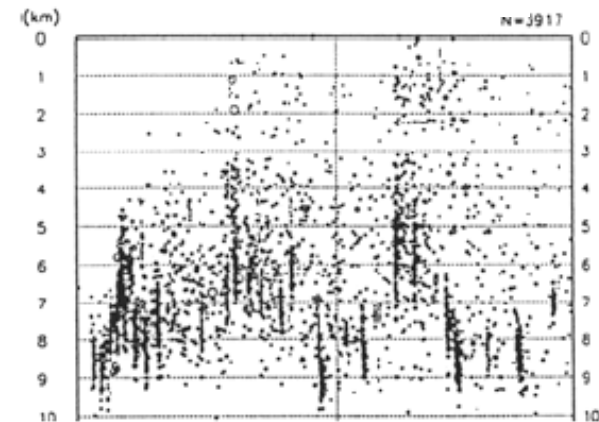
TIME

時空間分布図(南北)

LATITUDE



TIME

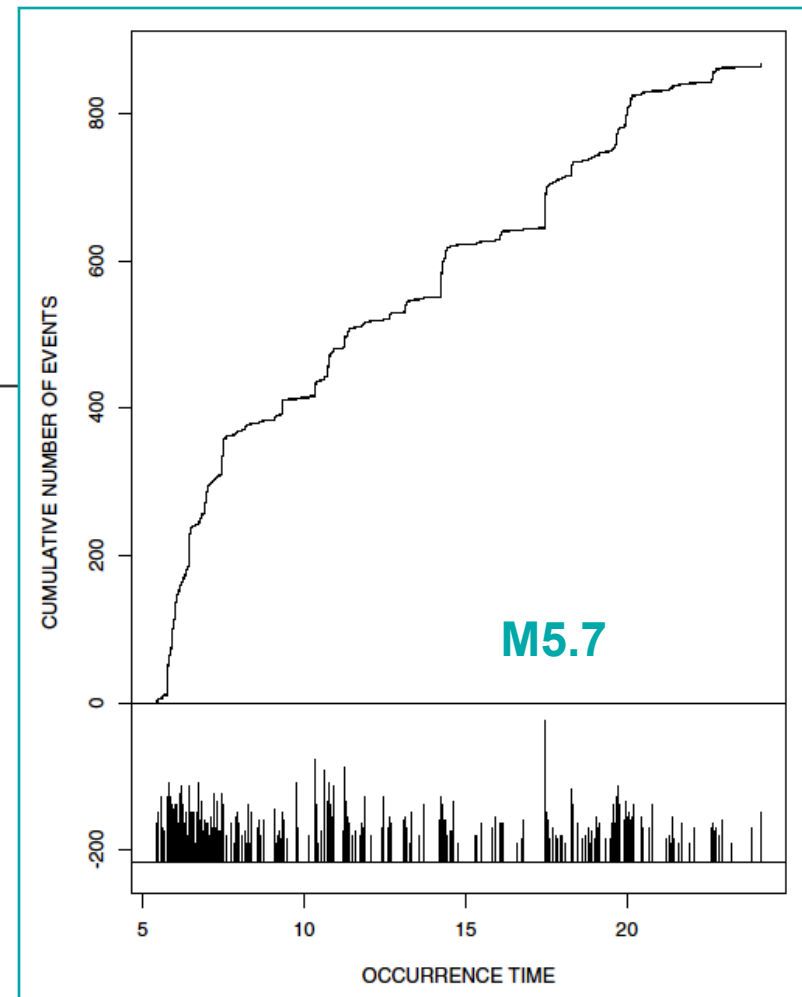
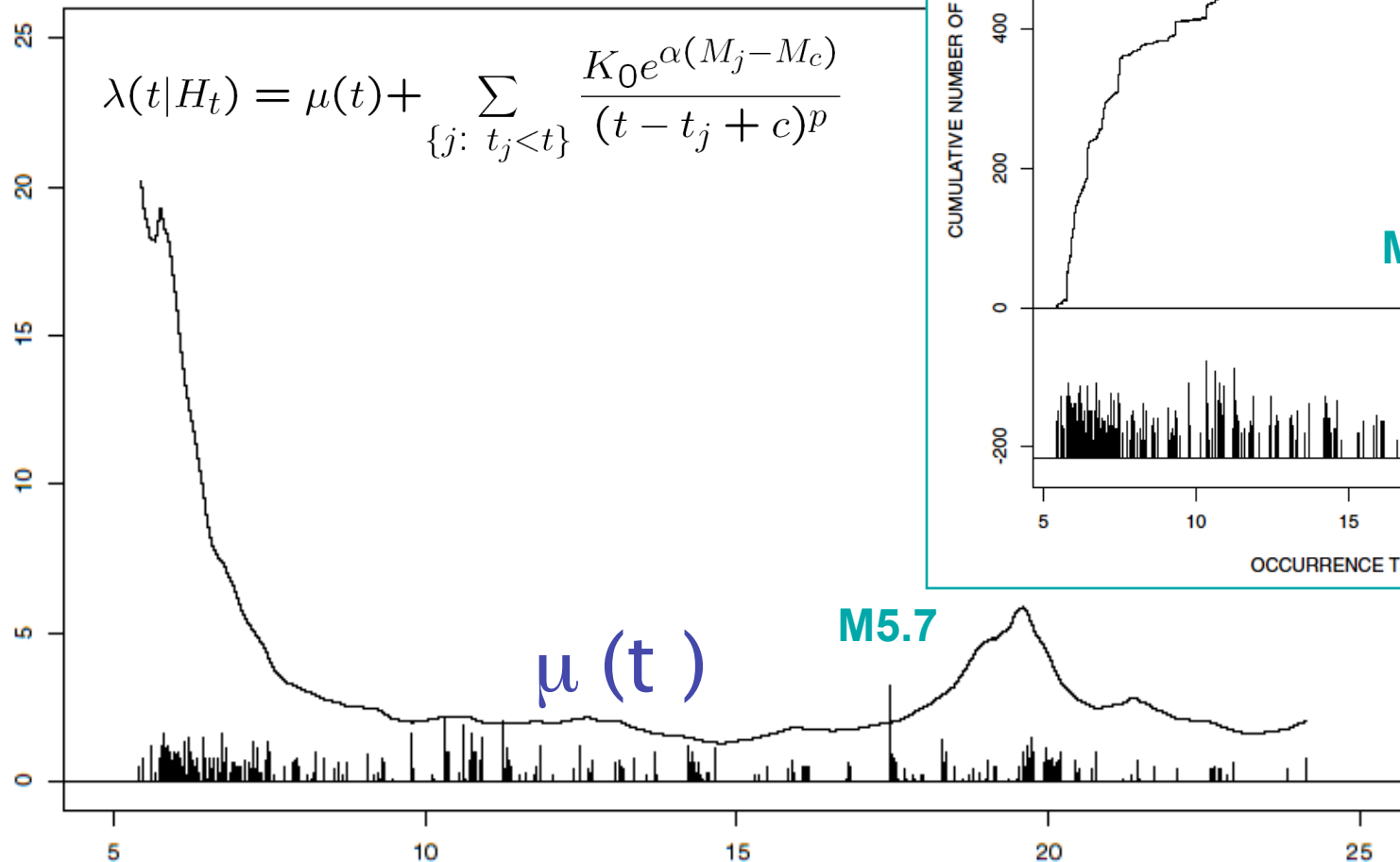


DEPTH

11-3

Off the East coast of Izu Peninsula Swarm

Exogeneous occurrence rate / day

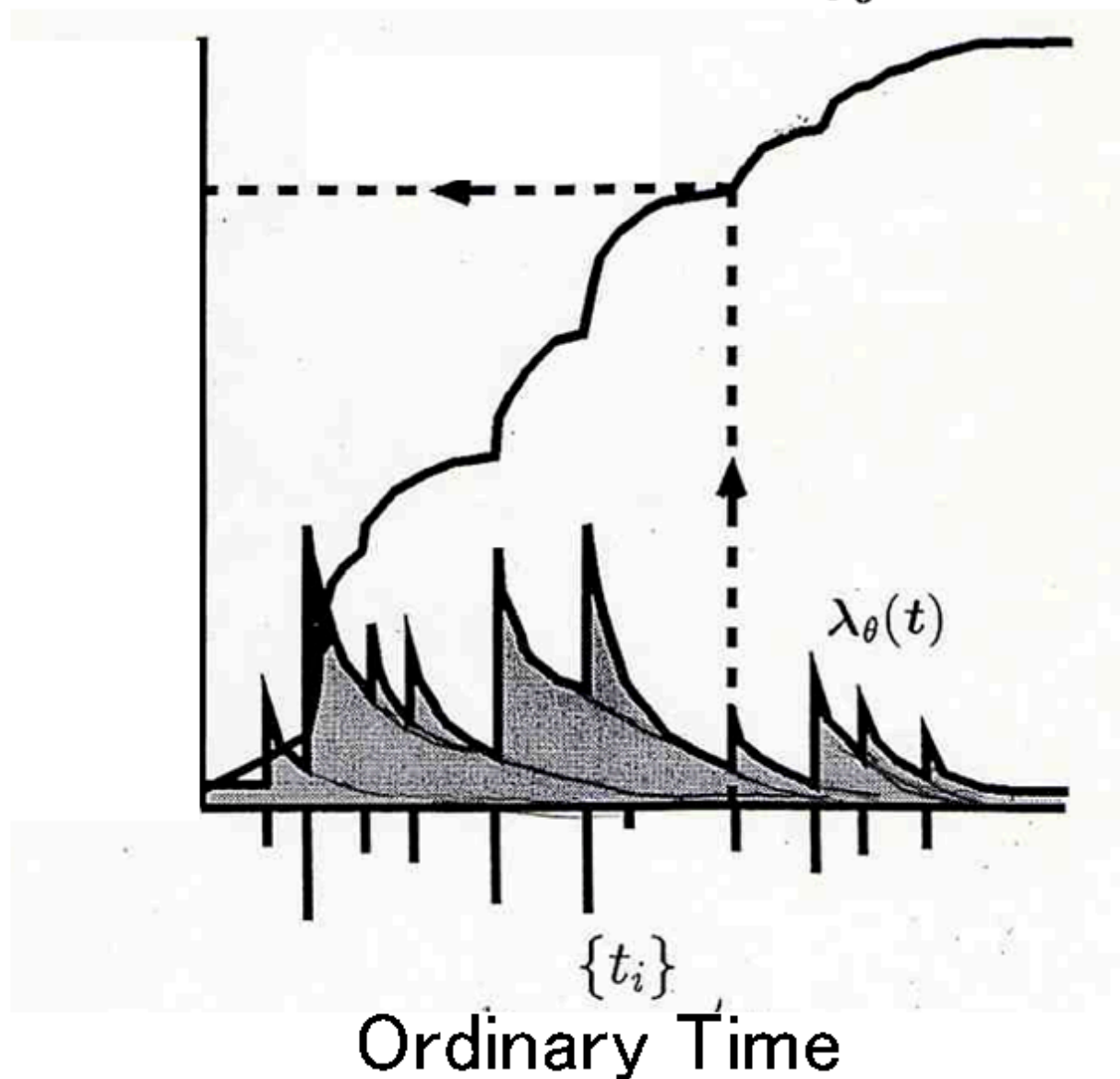


Elapsed days from 16 APR 1998

Diagnostic Analysis by Time Transformation

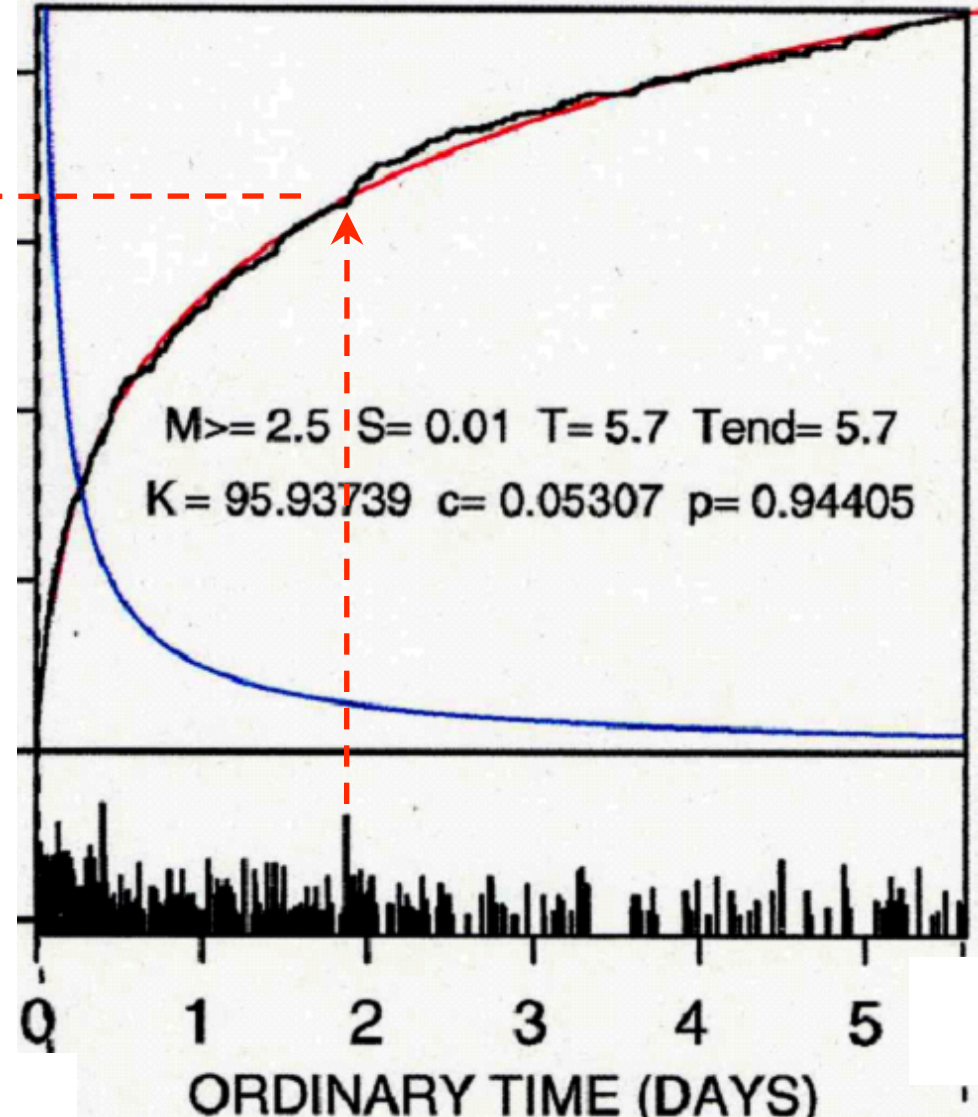
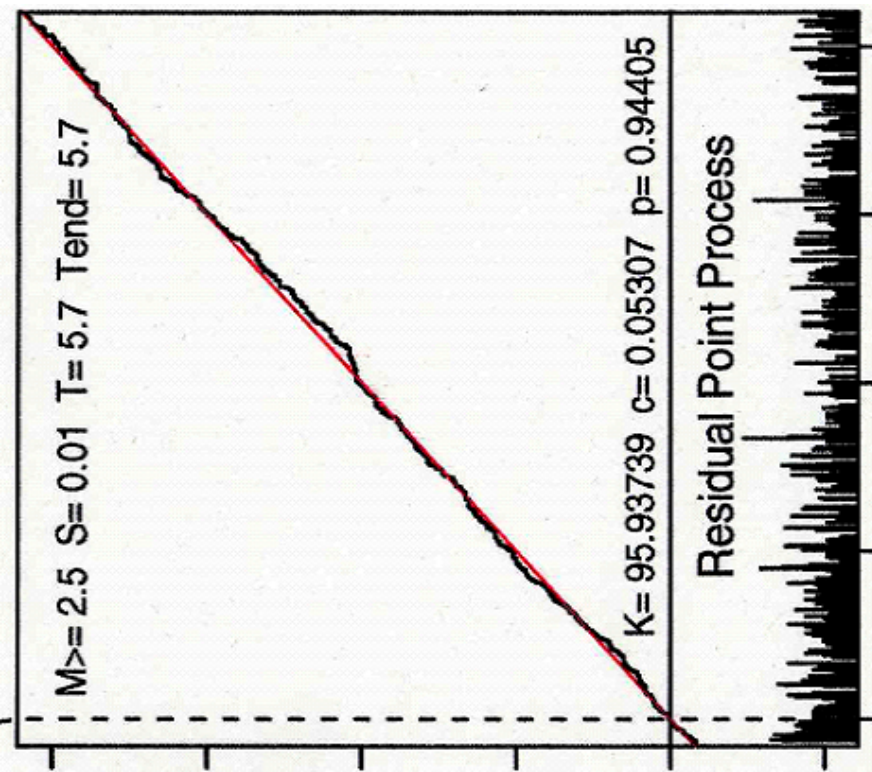
Theoretical cumulative
number of the events:

$$\Lambda(t) = \int_0^t \lambda(s) ds$$



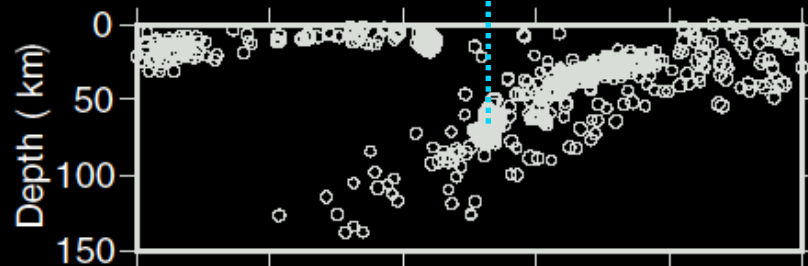
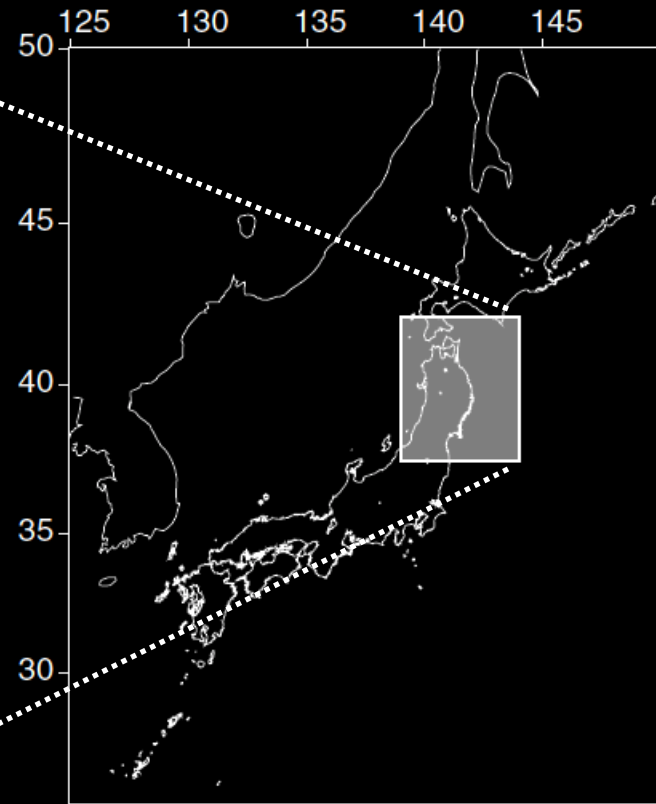
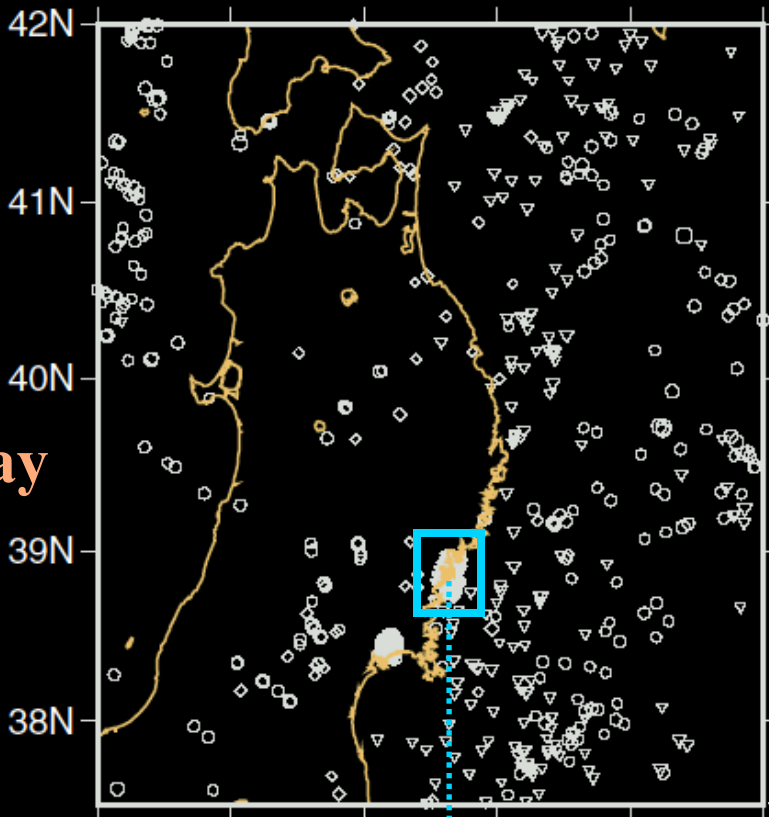
Theoretical cumulative number of the events:

$$\Lambda(t) = \int_0^t \lambda(s) ds$$



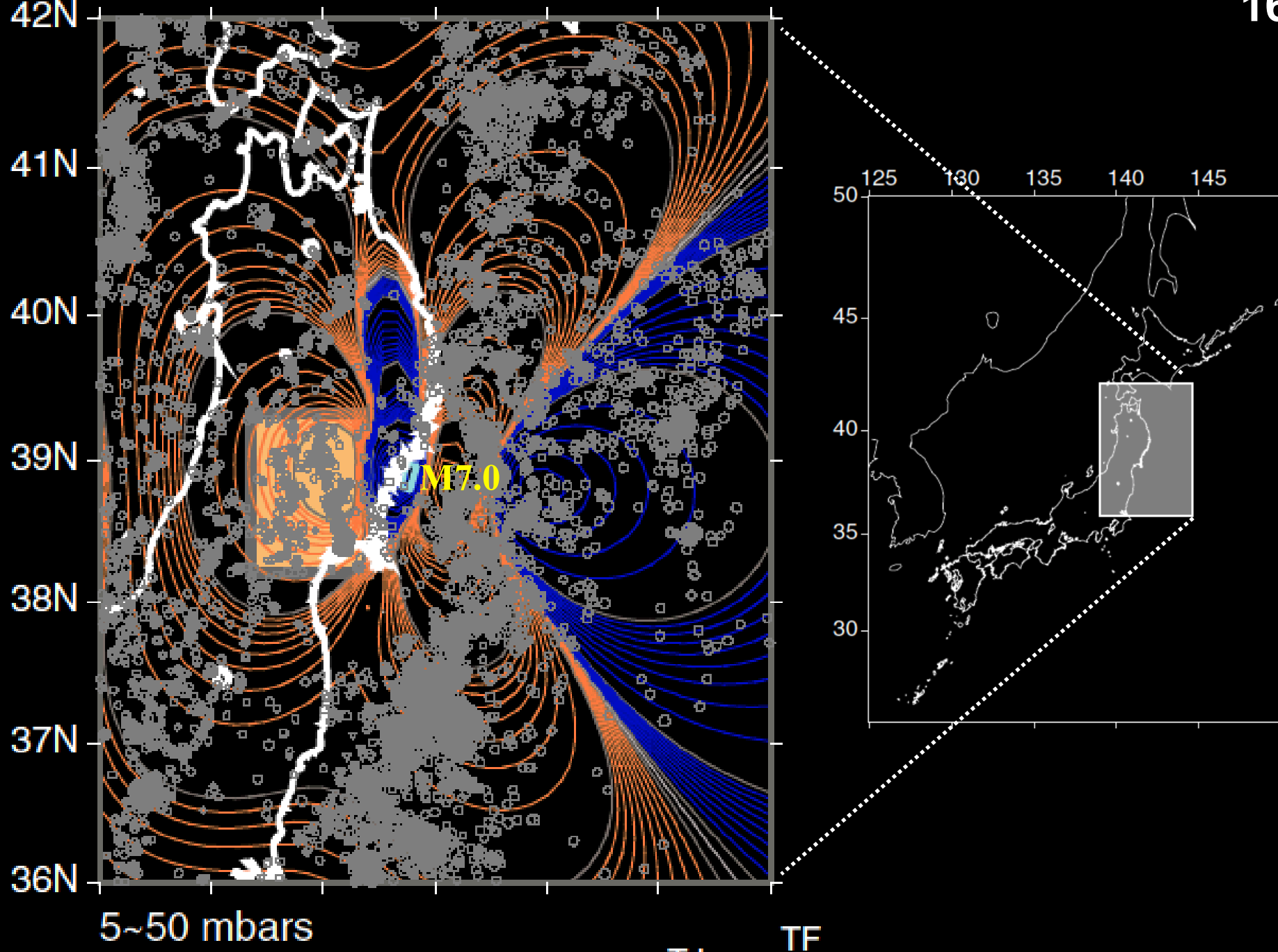
2003 May - July; $H \leq 150.0\text{km}$; $M \geq 2.0$

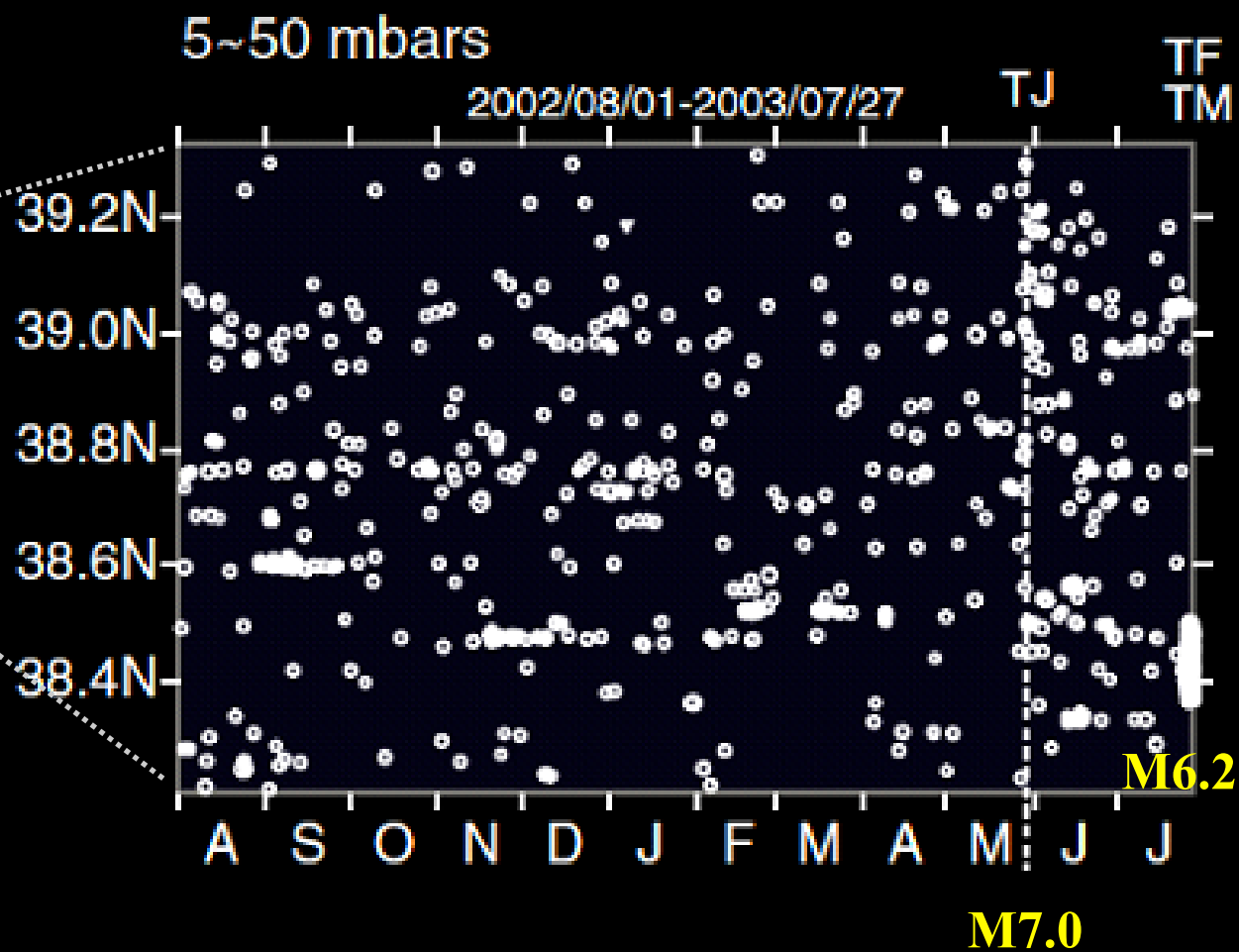
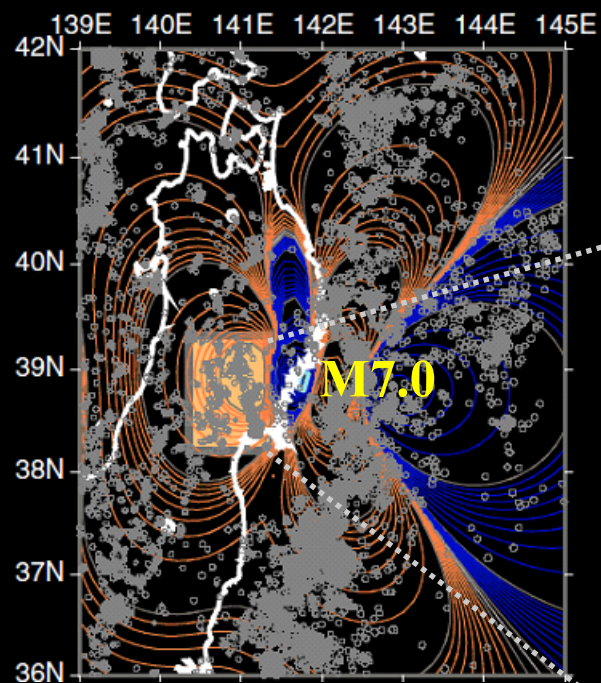
139E 140E 141E 142E 143E 144E

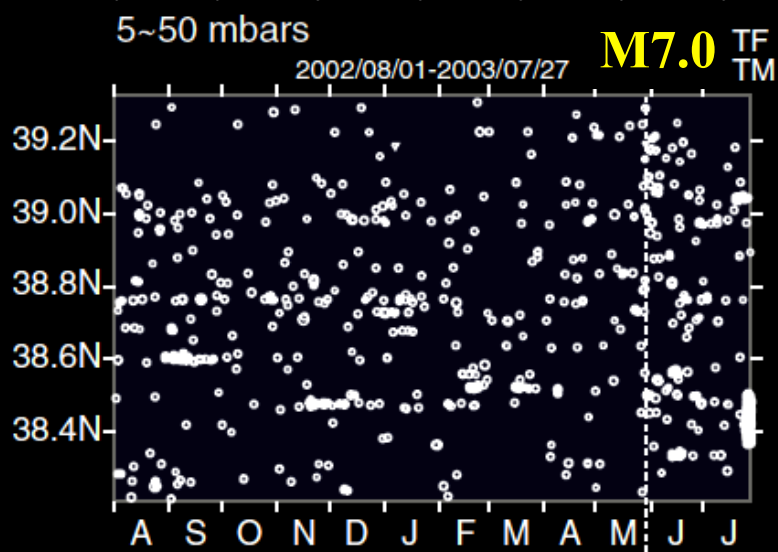
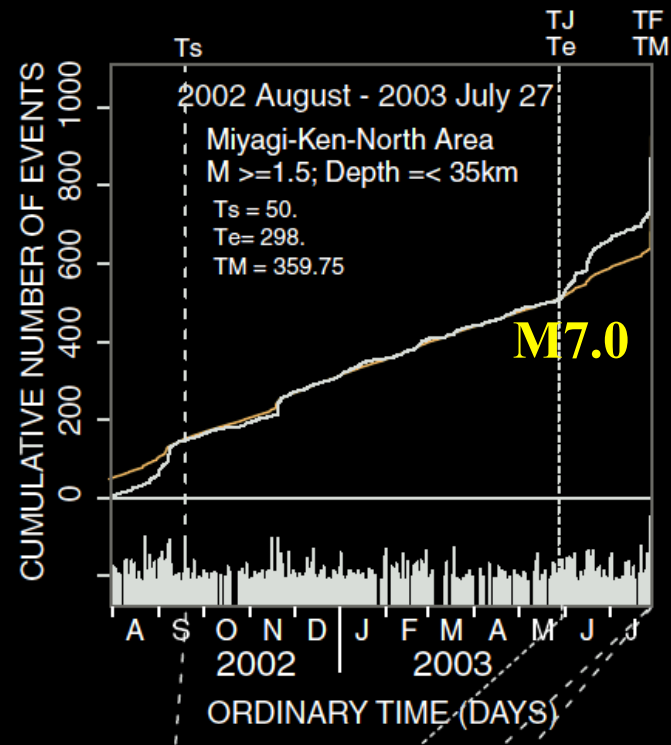
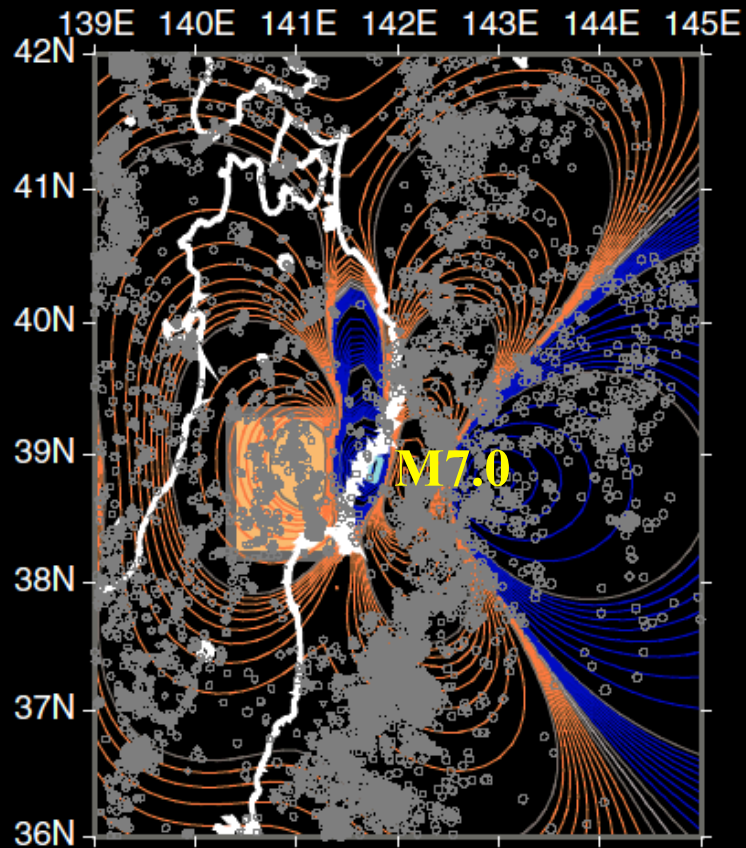


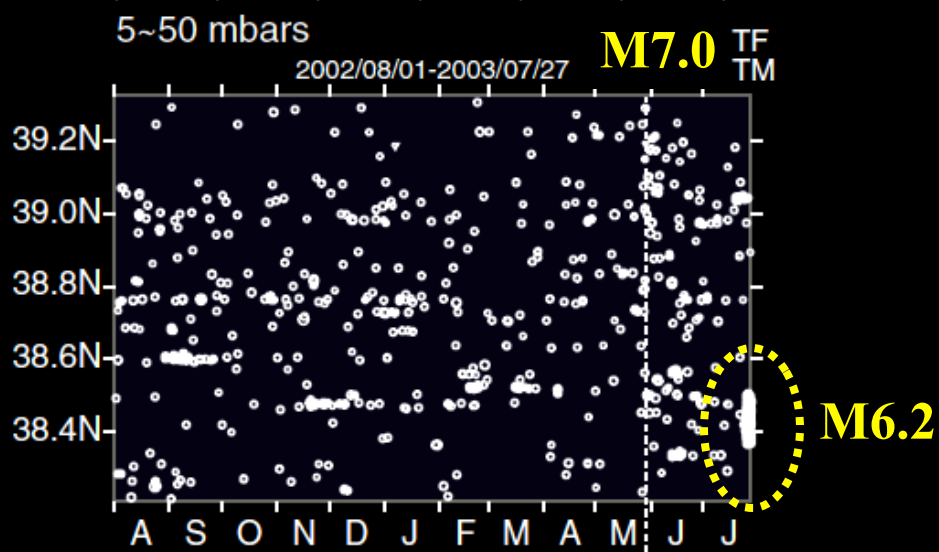
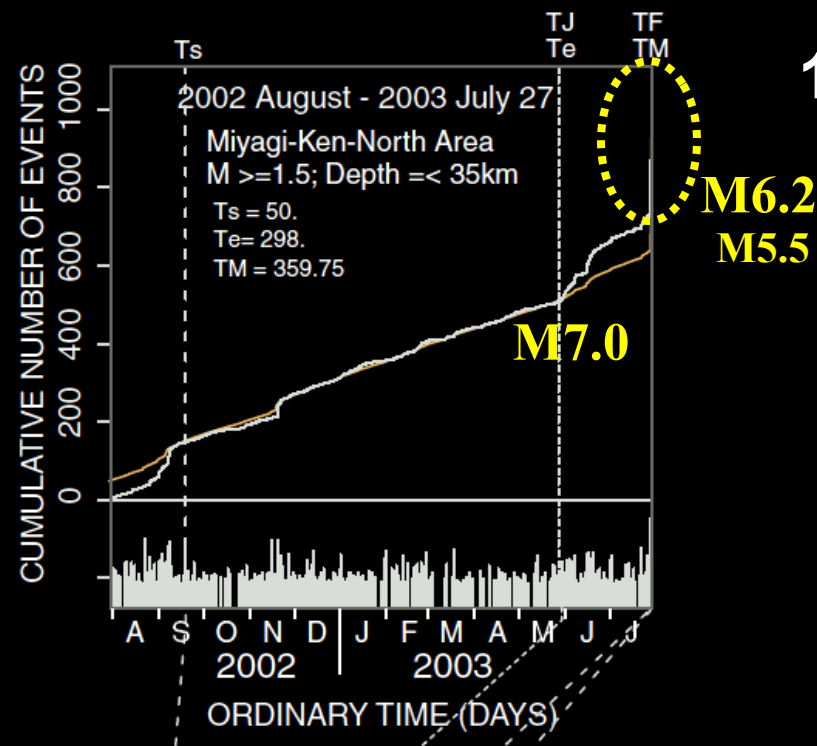
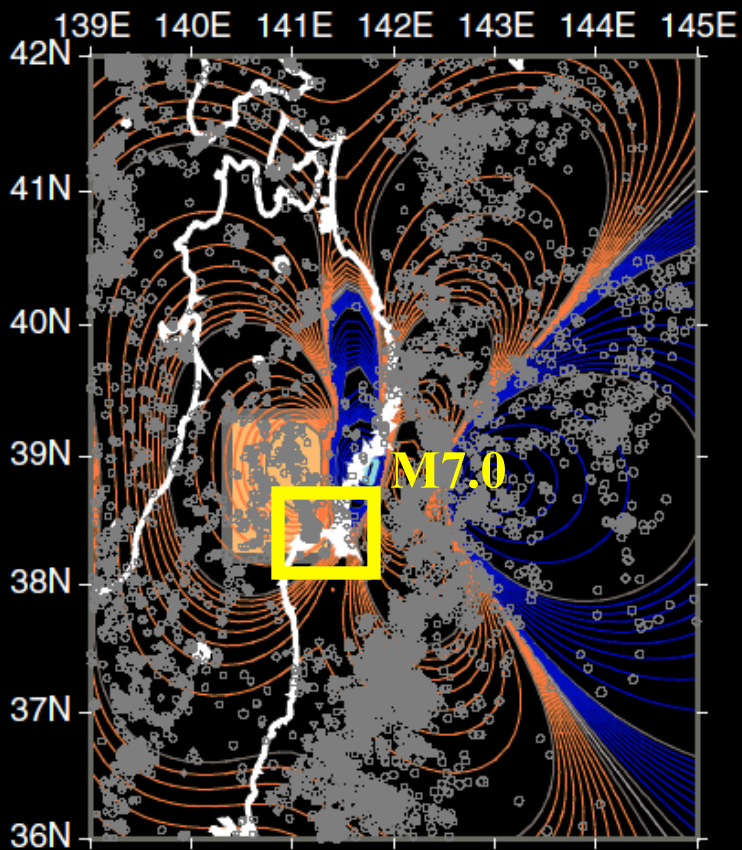
M7.0
2003 May
depth
71km

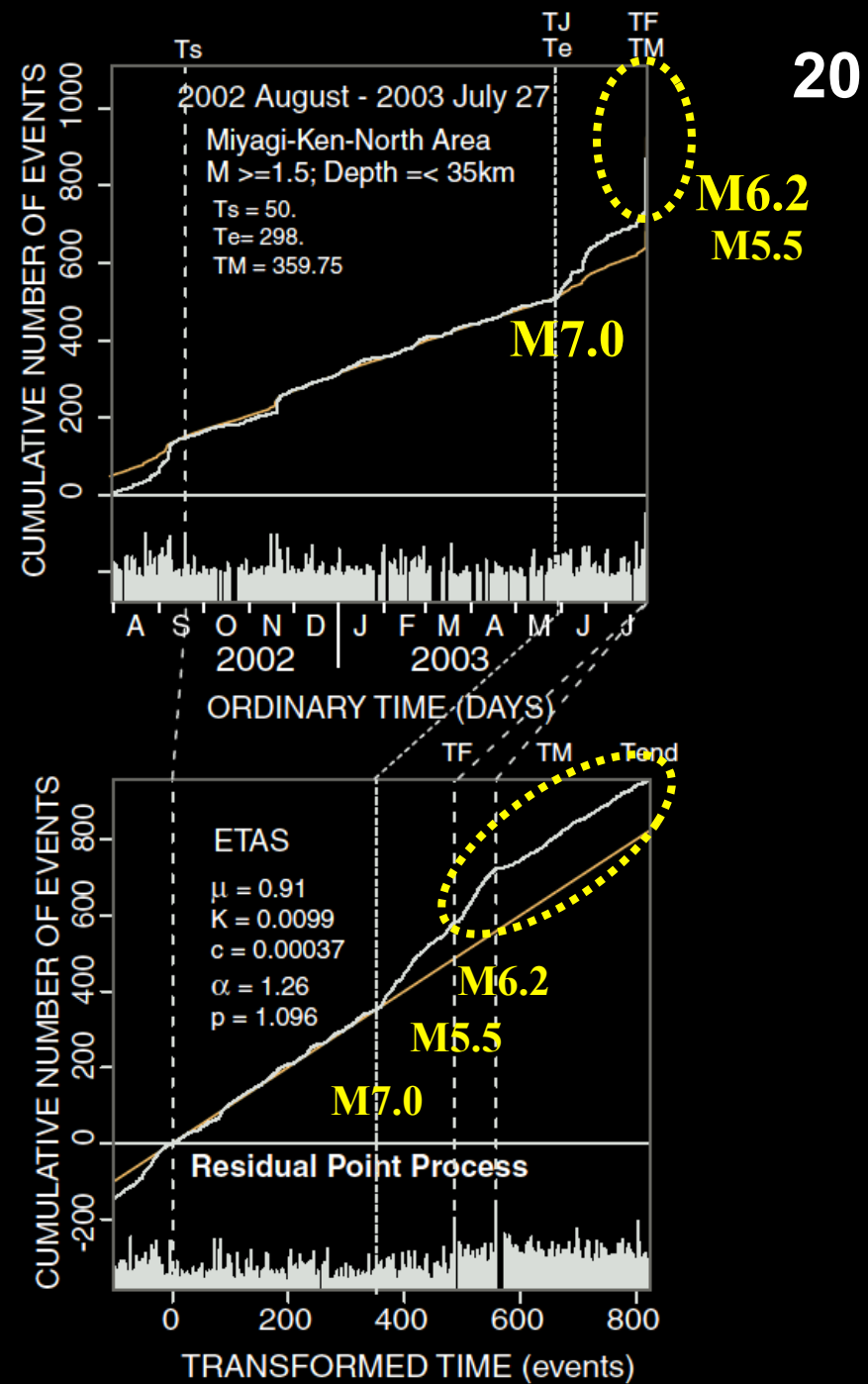
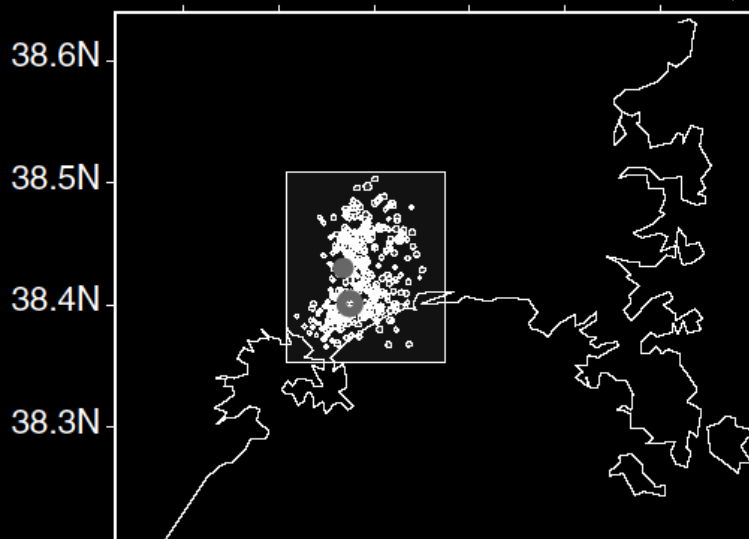
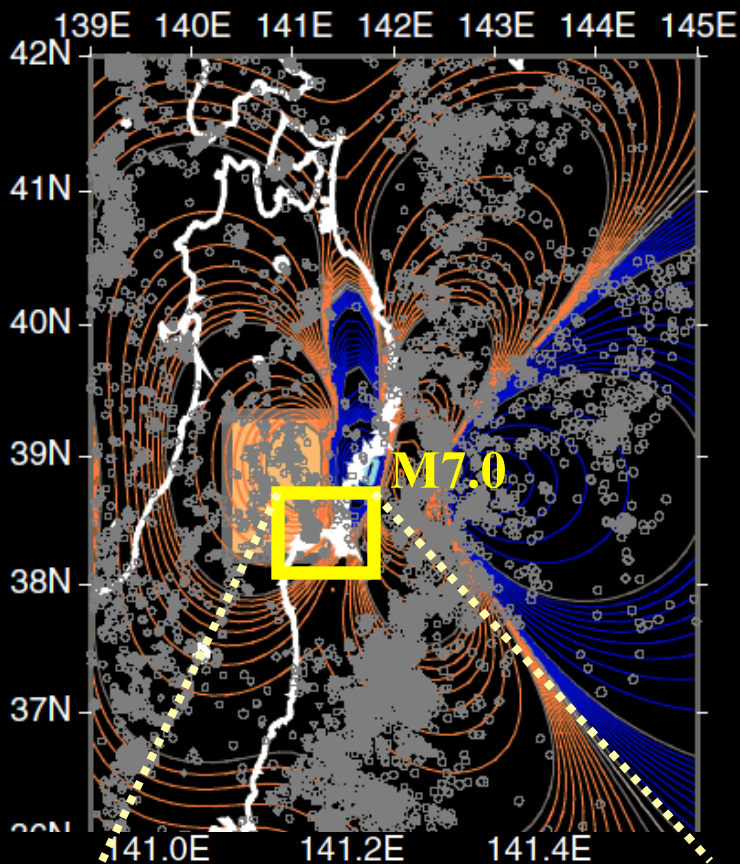
M6.2, 2003 July, depth 12km



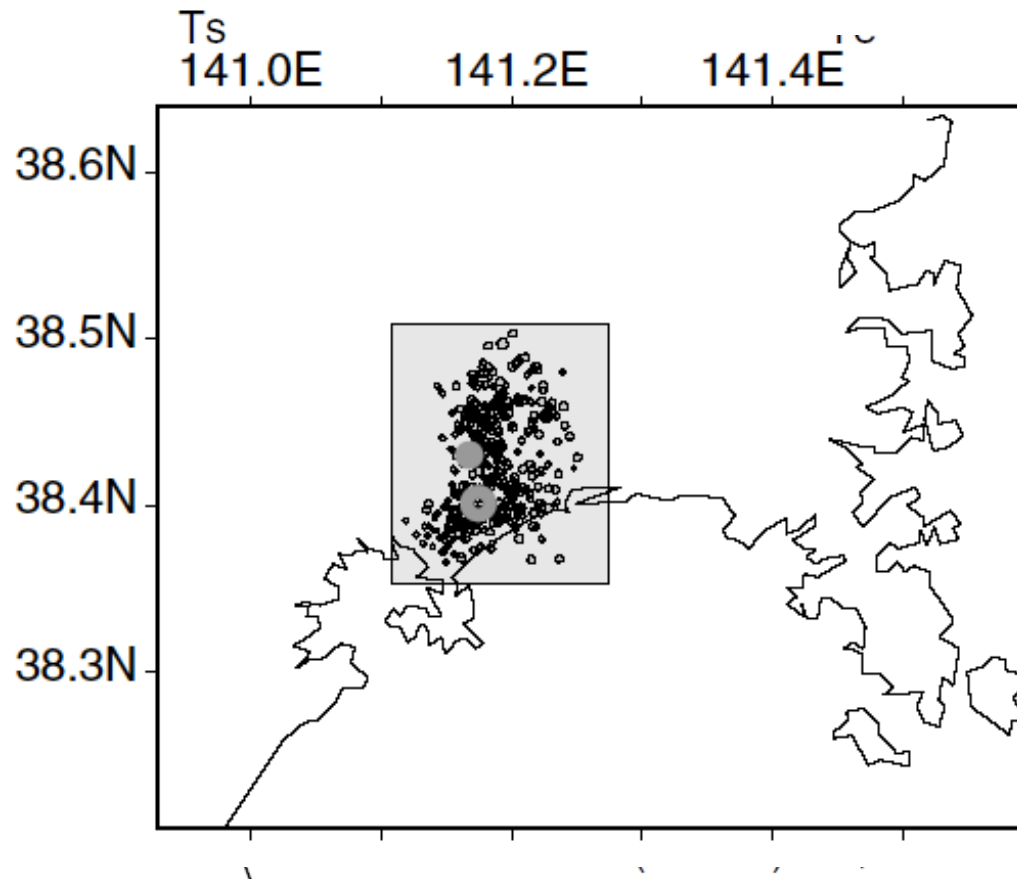




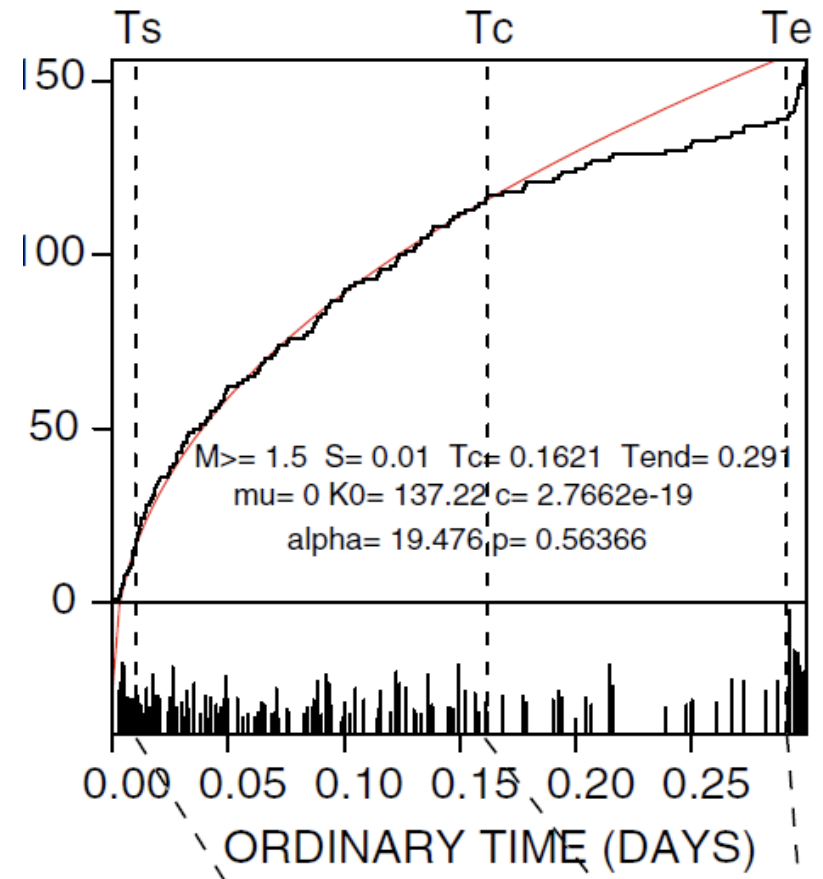




2003 Miyagi-Ken-North foreshocks ($M \geq 1.5$) till the mainshock

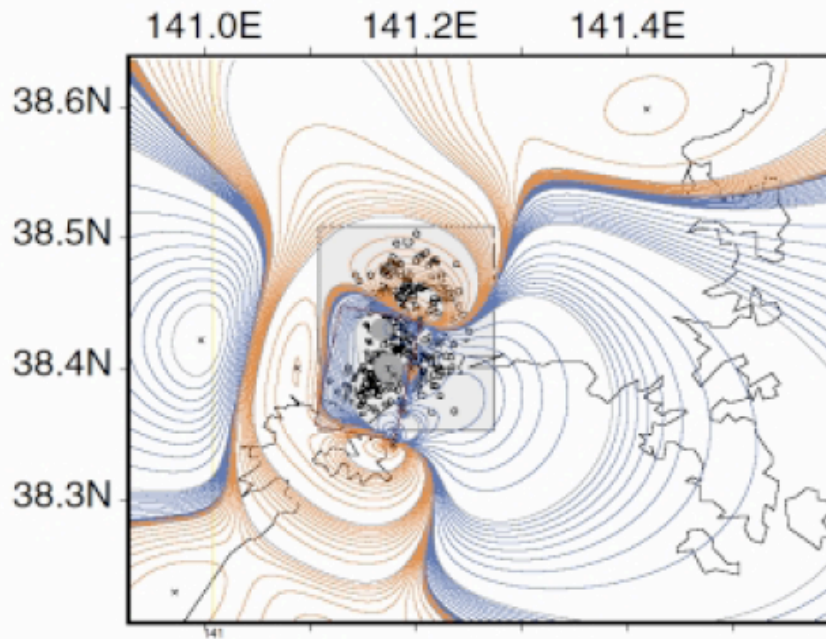


A change-point

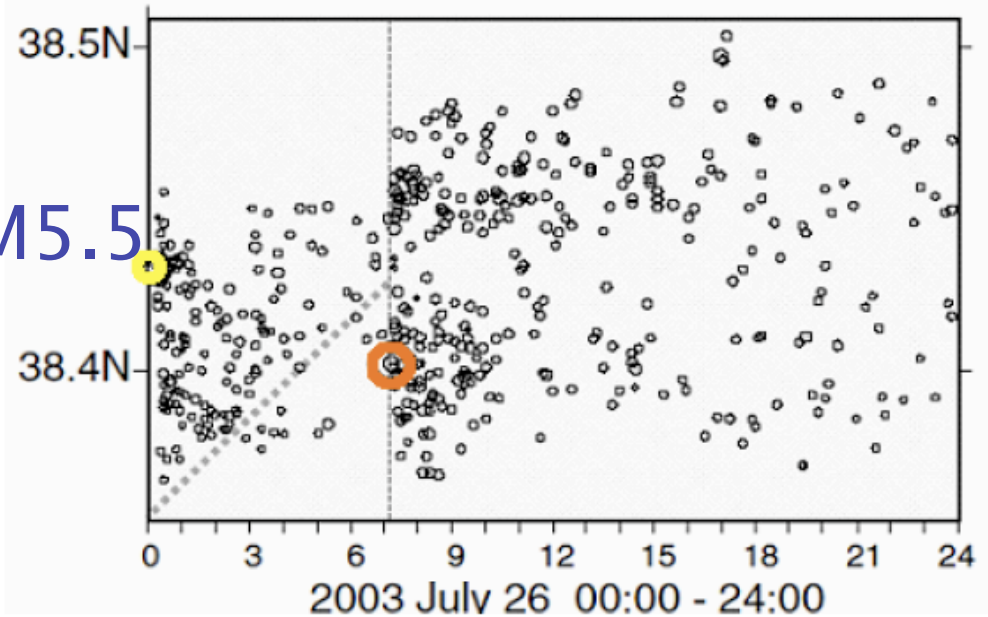


M6.2
↓

2003年M6.2宮城県北部地震の前震
Foreshocks of the Miyagi-Ken-North



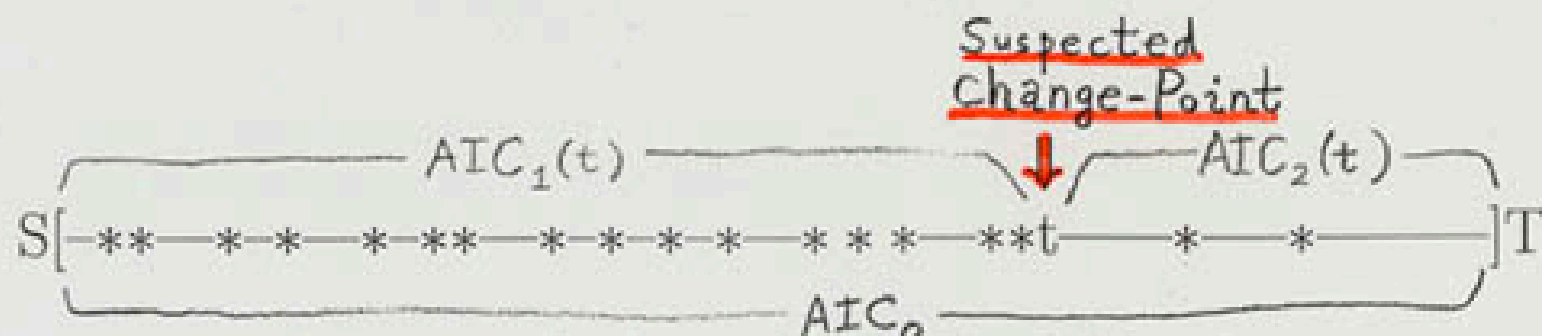
M5.5



Change-Point Analysis

Change-Point Analysis by the AIC

$$AIC = (-2) \max\{\log\text{-likelihood}\} + 2\{\text{number of parameters}\}$$



$$AIC_0 = (-2) \max_{\theta} \log_e \bar{L}(\theta; S, T) + 2k_0,$$

$$AIC_1(t) = (-2) \max_{\theta} \log_e L(\theta; S, t) + 2k_1,$$

$$AIC_2(t) = (-2) \max_{\theta} \log_e L(\theta; t, T) + 2k_2;$$

AIC_0 is compared with $AIC_{12}(t) + 2k(N)$ to choose the case of smaller value, where

$$AIC_{12}(t) = AIC_1(t) + AIC_2(t),$$

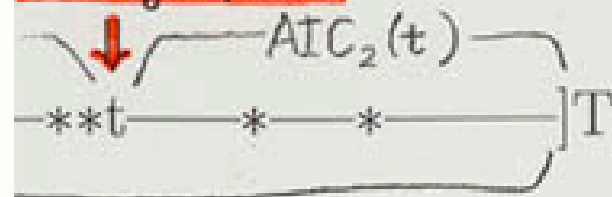
and $k(N)$ is the bias correction in search of t minimizing $AIC_{12}(t)$ (*change-point problem*) and is a certain function of the number of events N in the interval $[S, T]$.

Change-Point Analysis by the AIC

$$AIC_{12} = AIC_1 + AIC_2 + \underline{2k(N)}$$

{number of parameters}

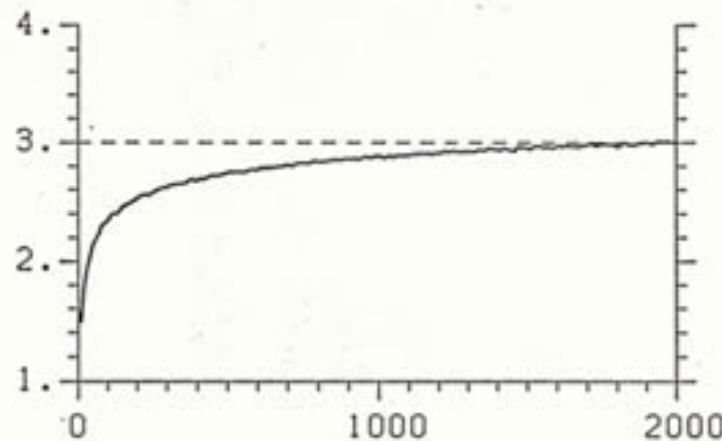
Suspected
Change-Point



$$\theta; S, T) + 2k_0,$$

$$\theta; S, t) + 2k_1,$$

$$\theta; t, T) + 2k_2;$$



Data size N

AIC_0 is compared with $AIC_{12}(t) + 2k(N)$ to choose the case of smaller value, where

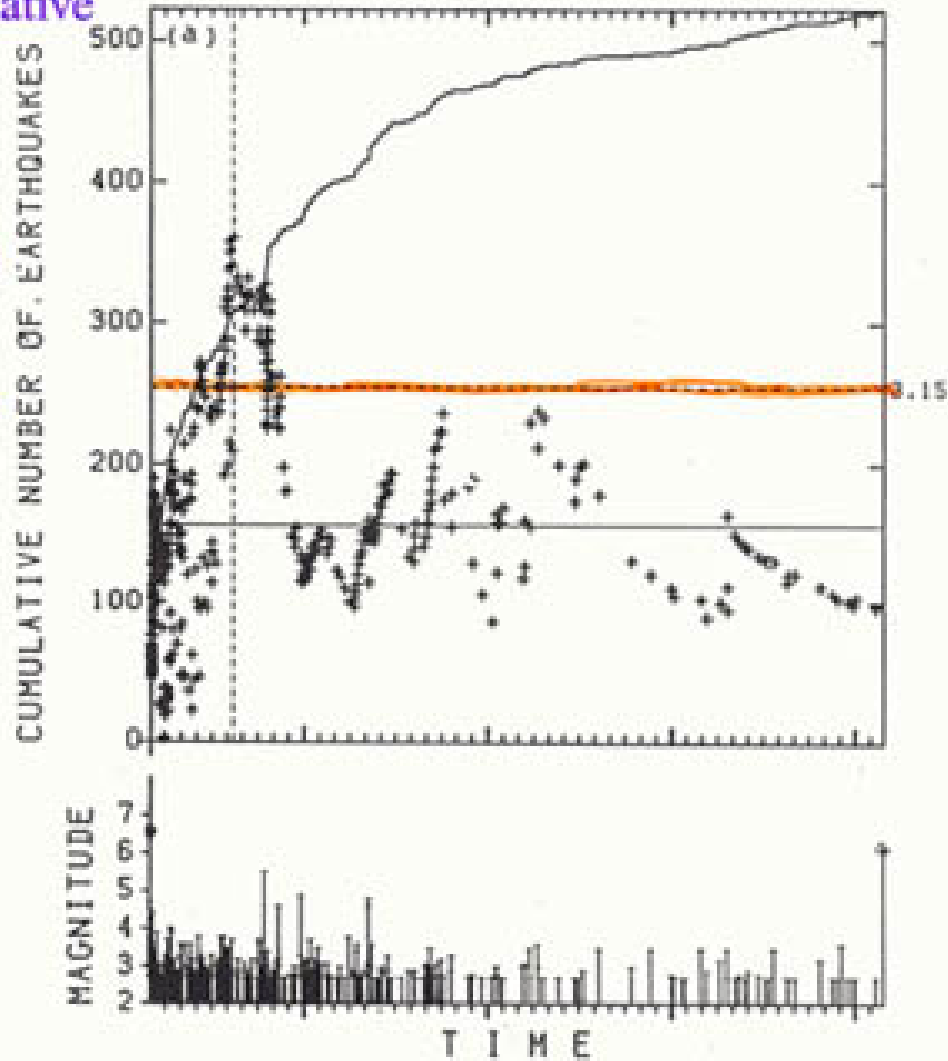
$$AIC_{12}(t) = AIC_1(t) + AIC_2(t),$$

and $k(N)$ is the bias correction in search of t minimizing $AIC_{12}(t)$ (*change-point problem*) and is a certain function of the number of events N in the interval $[S, T]$.

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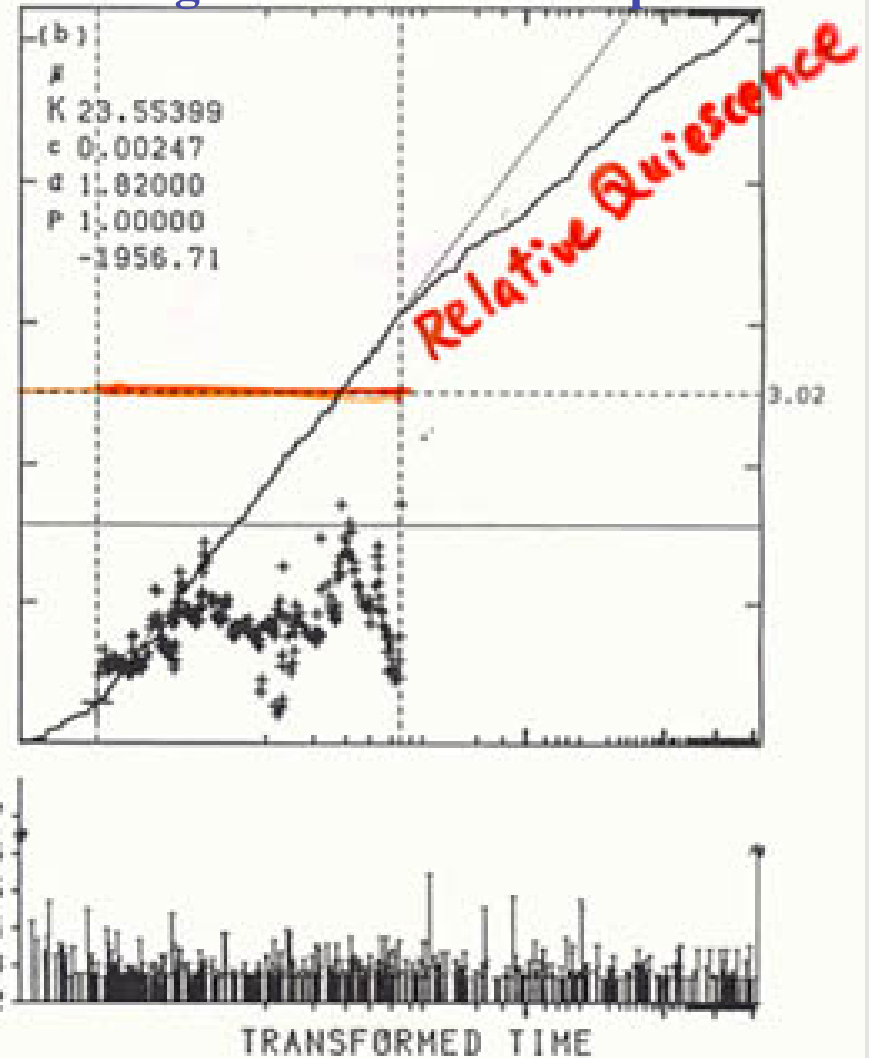
N=522 T=47.880 T0=0.030 T1=5.370

KAGOSHIMA 1997.3/26 - 5/13 H=2.7



ETAS

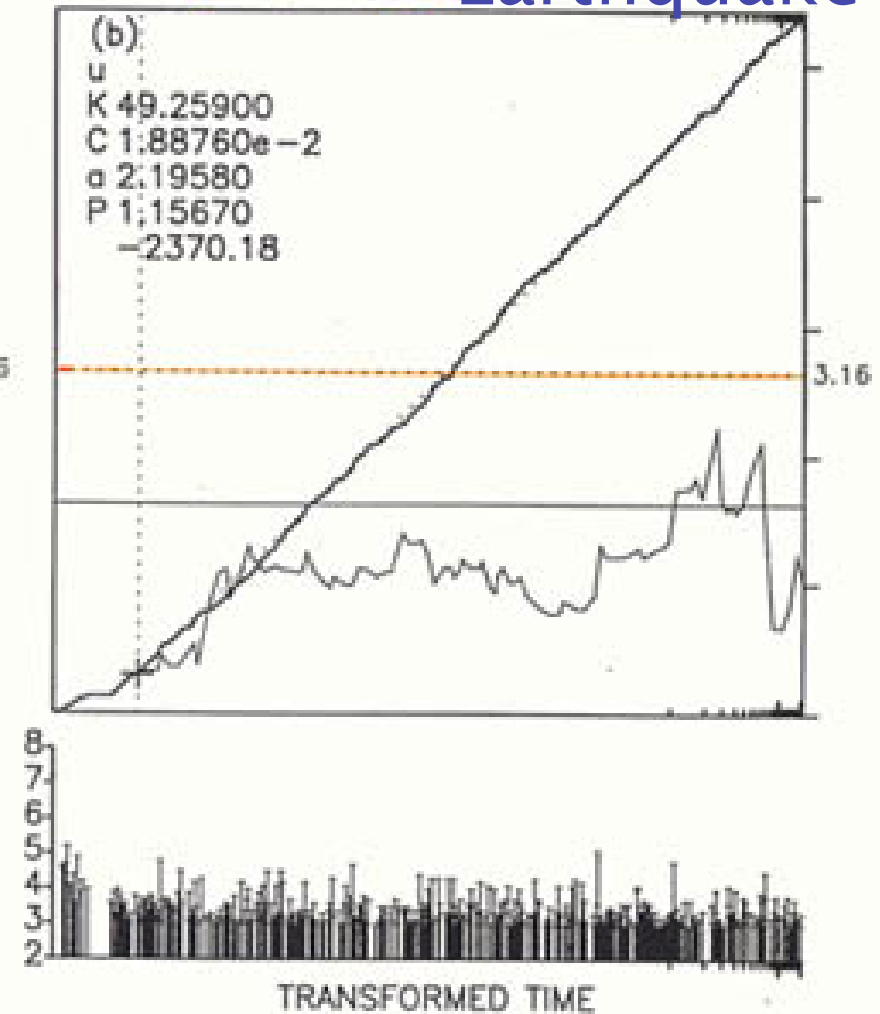
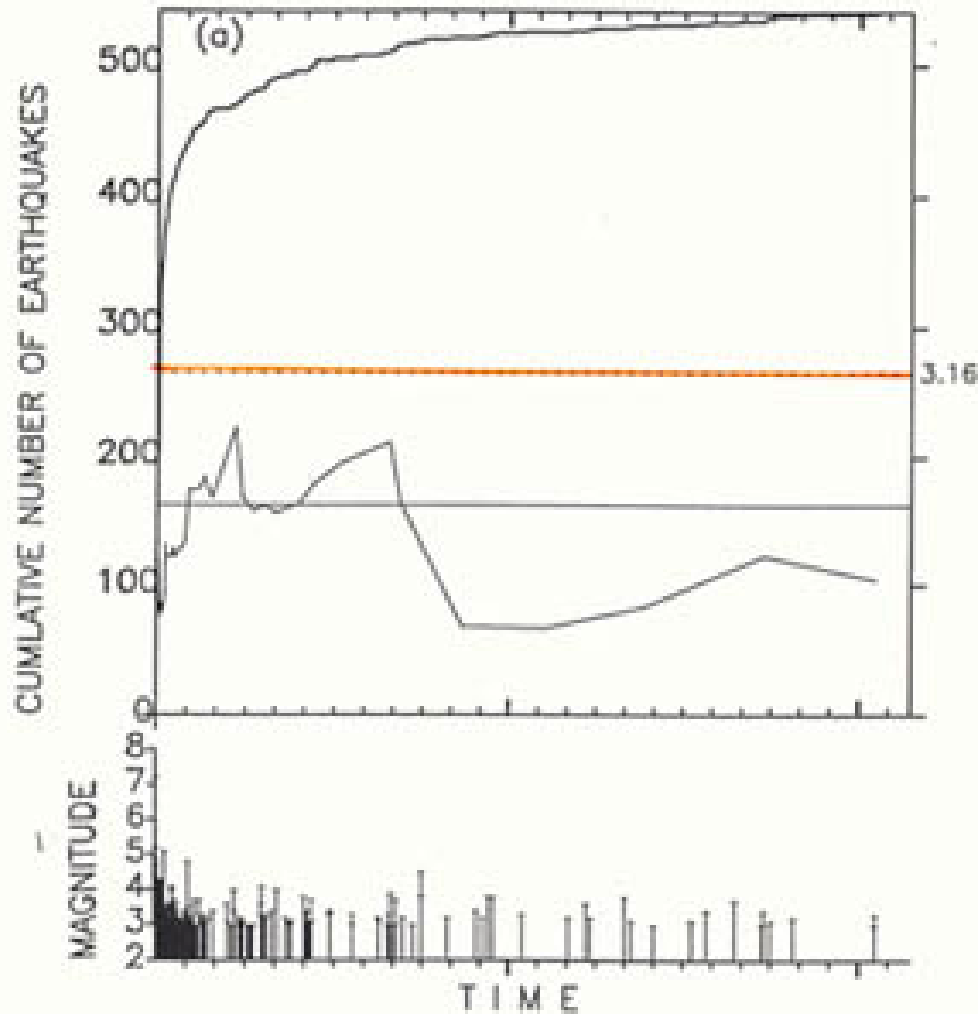
1997 Kagoshima NW Earthquake



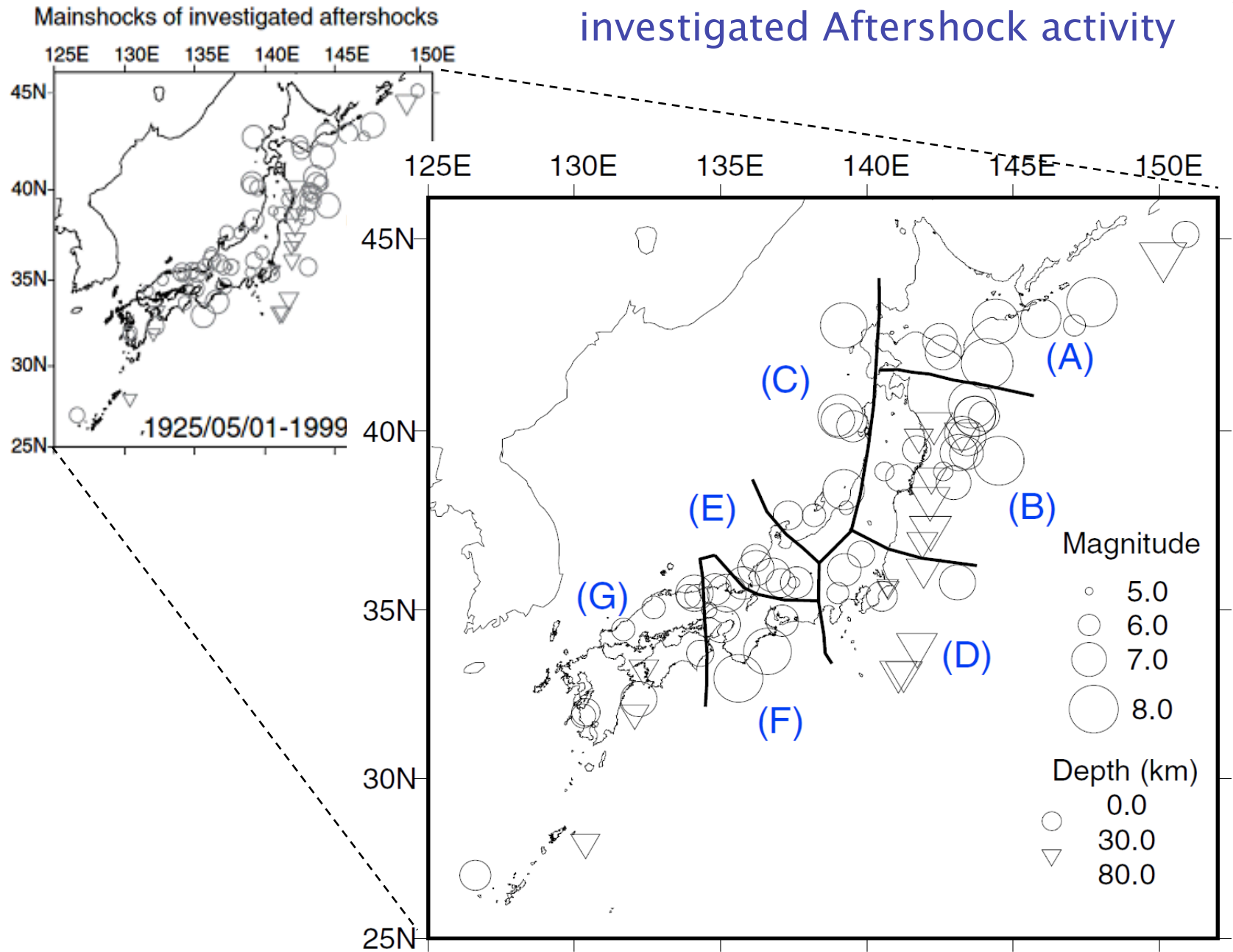
n=541 t=773.00 tc=773.00 t0=0.020

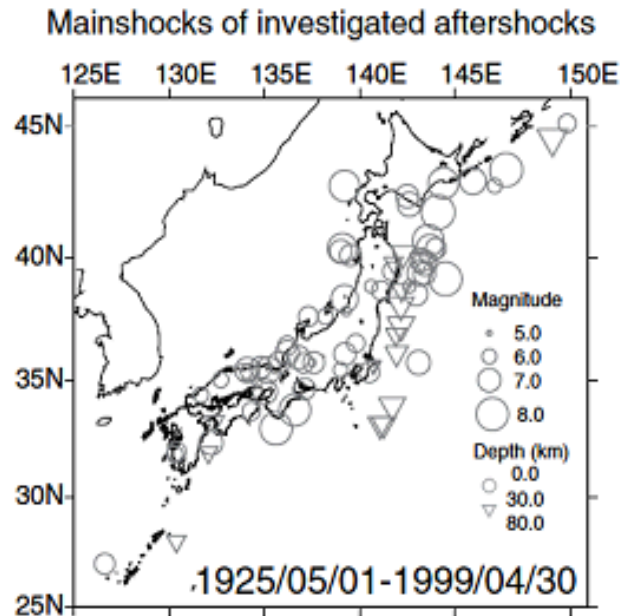
95Kobe Aftershocks M0 7.2, Mc 3.0

1995 Kobe Earthquake

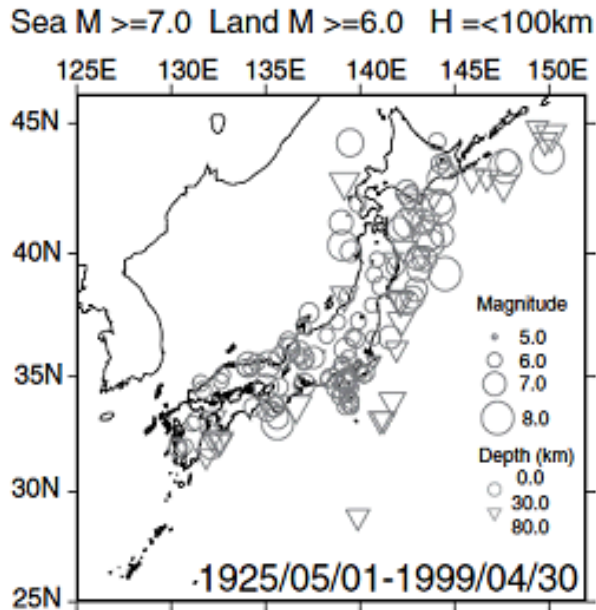


The mainshocks location of investigated Aftershock activity

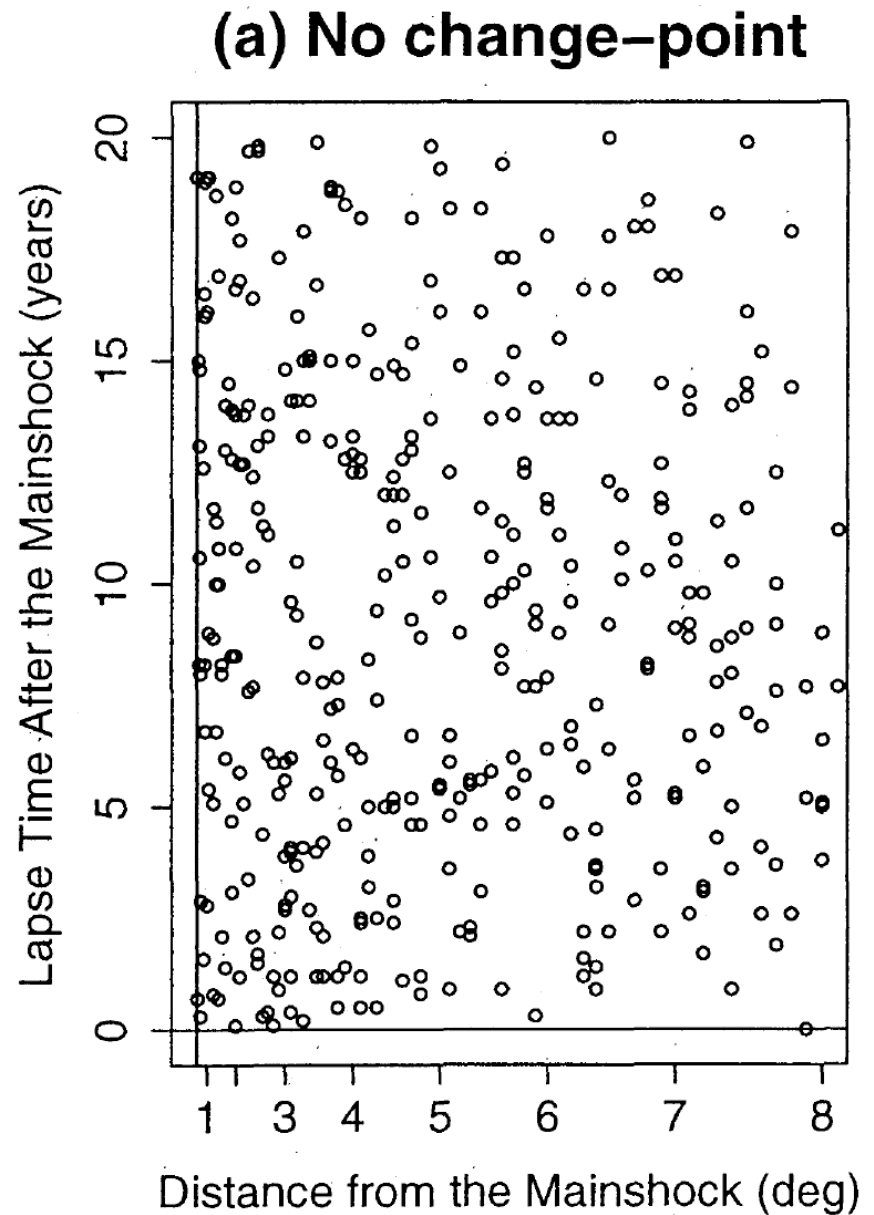
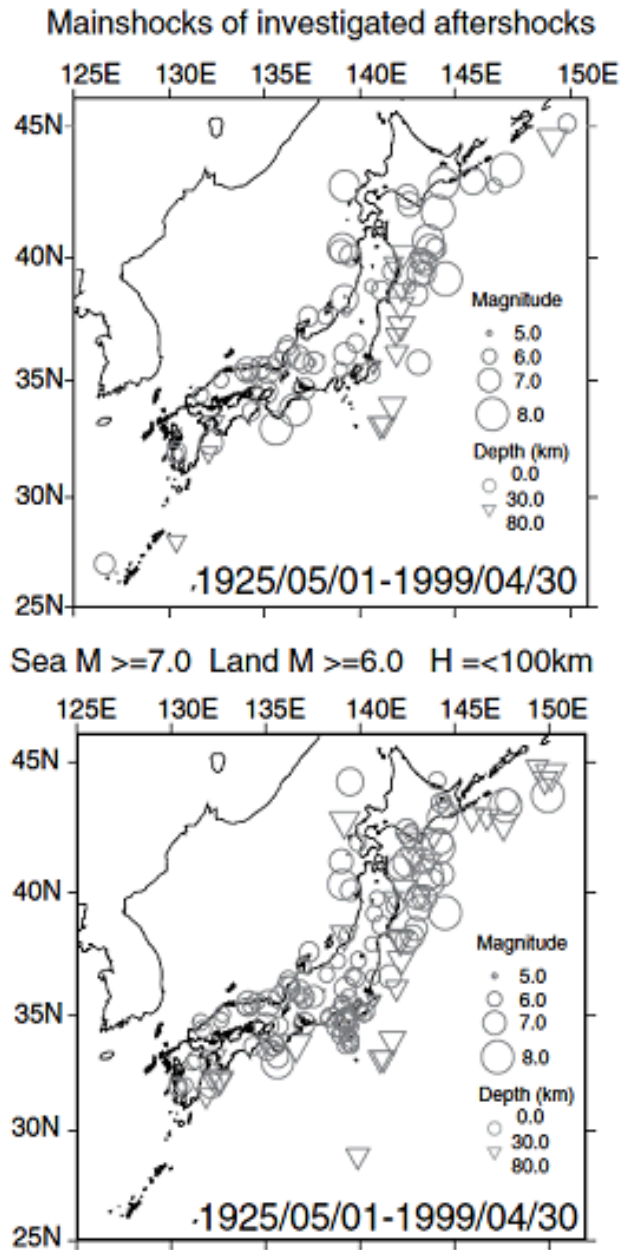




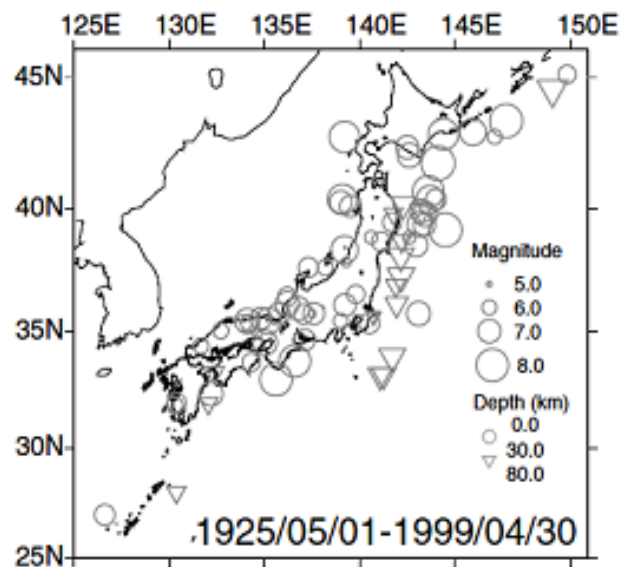
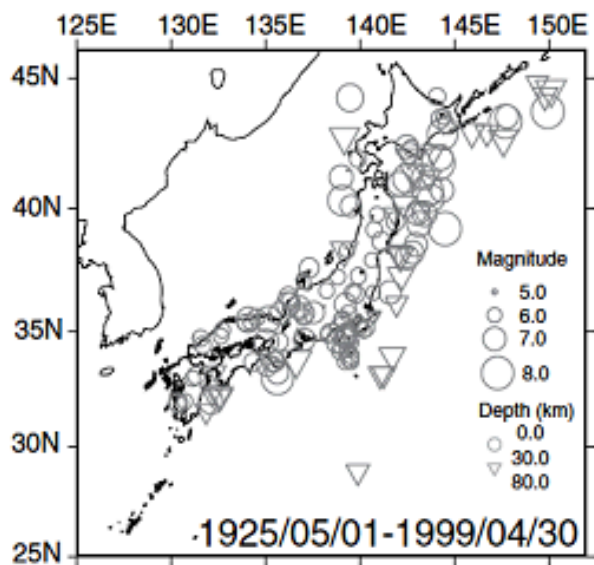
The mainshocks location of investigated Aftershock activity



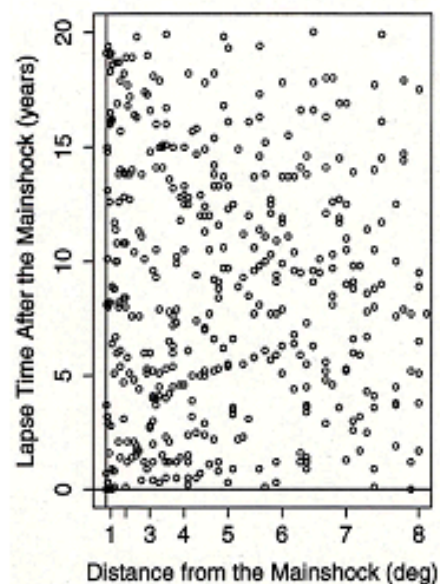
The subsequent large earthquakes



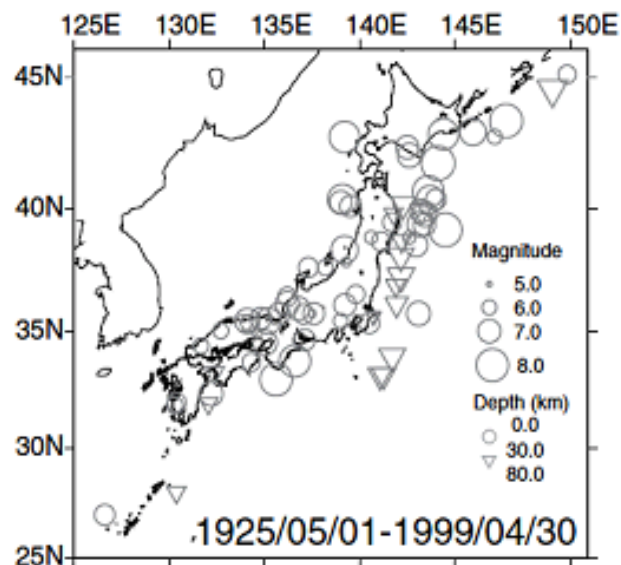
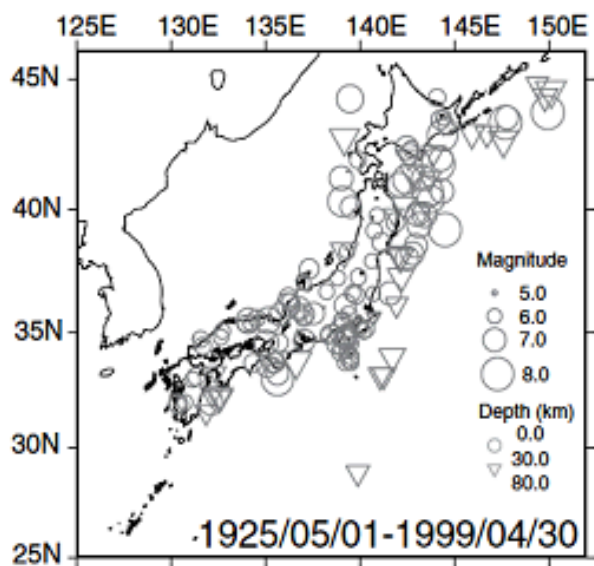
Mainshocks of investigated aftershocks

Sea $M \geq 7.0$ Land $M \geq 6.0$ $H \leq 100\text{km}$ 

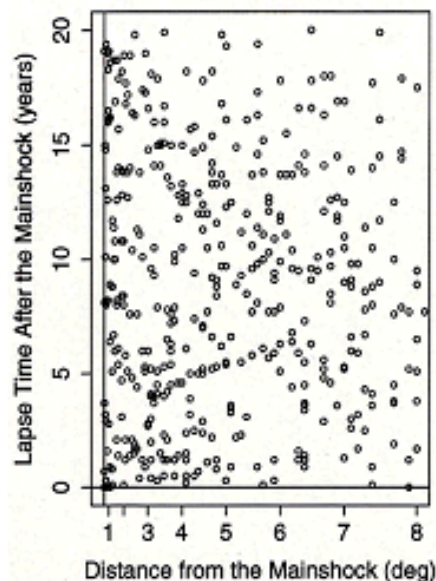
(a) No change point



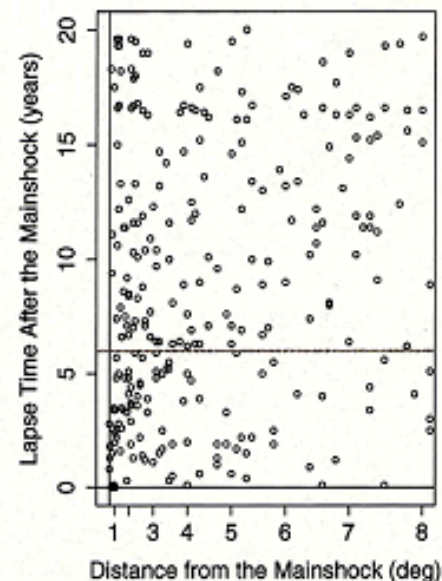
Mainshocks of investigated aftershocks

Sea $M \geq 7.0$ Land $M \geq 6.0$ $H = < 100\text{km}$ 

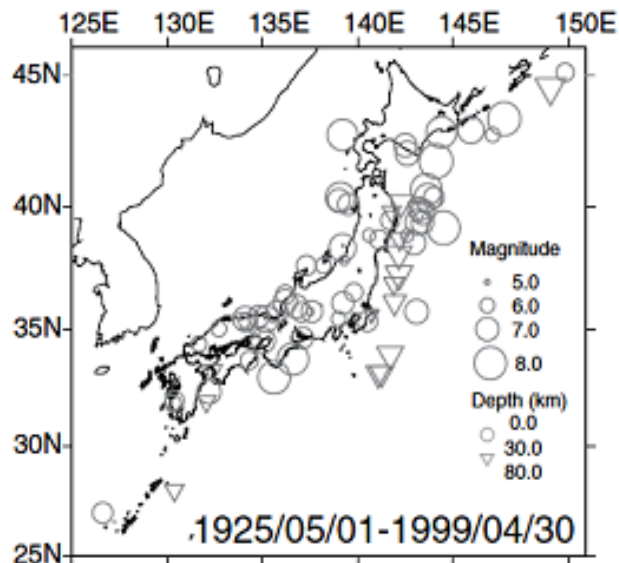
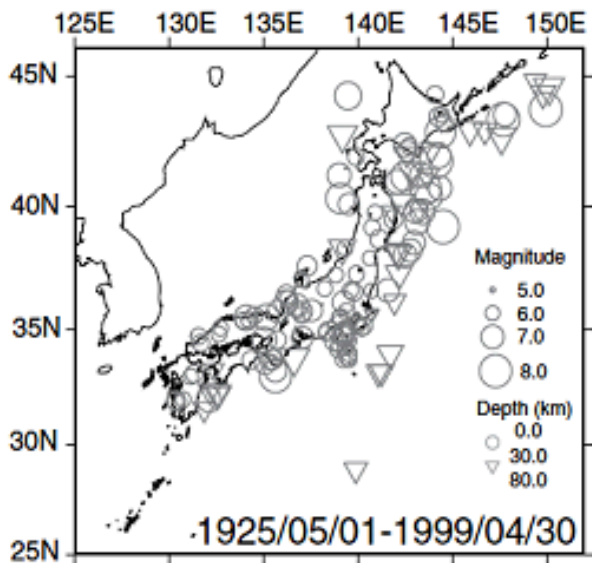
(a) No change point



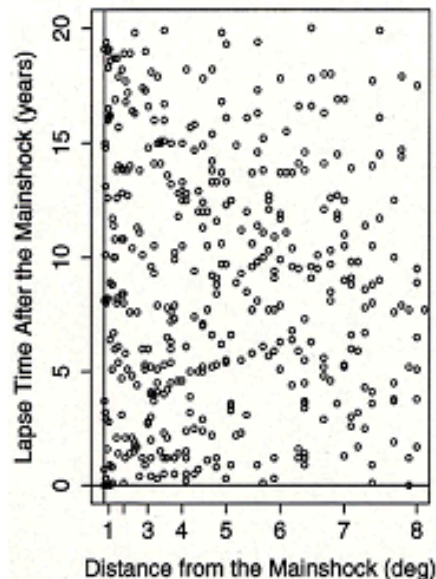
(b) Relative quiescence



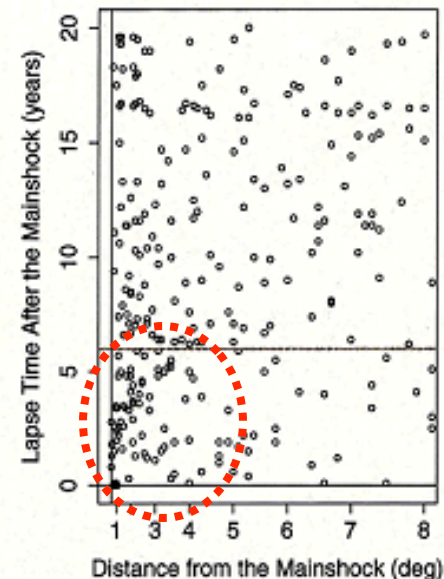
Mainshocks of investigated aftershocks

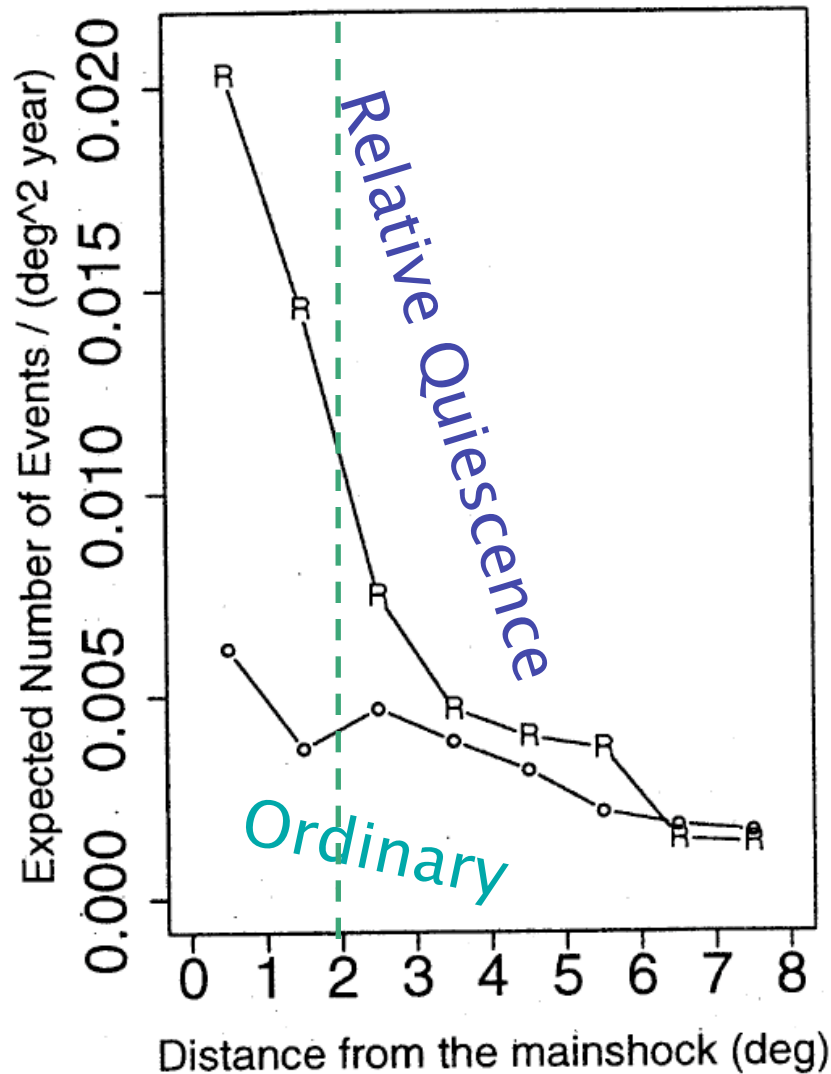
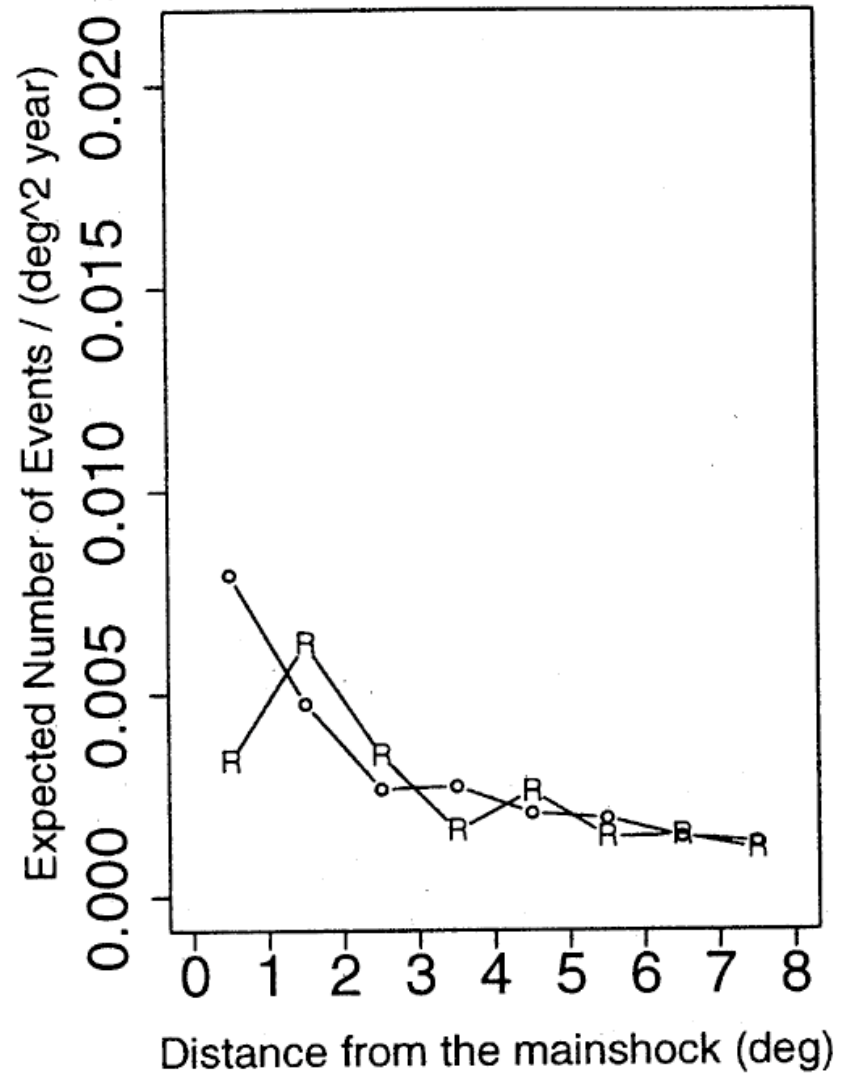
Sea $M \geq 7.0$ Land $M \geq 6.0$ $H \leq 100\text{km}$ 

(a) No change point



(b) Relative quiescence



(a) first 6 years span(b) next 14 years span

Proposed possible mechanisms of precursory seismic quiescence

- Dilatancy hardening [*Kelleher and J. Savino, 1975*]
- Bi-modal asperity model [*Kanamori, 1981*]
- Stress weakening due to a creep [*Wyss et al., 1981*]
- Slip-weakening [*Cao and Aki, 1985*]
- Computer simulations
[*Mikumo and Miyatake, 1983; Hainzl et al., 2000*].

→ Mechanism within the source

Seismic Quiescence

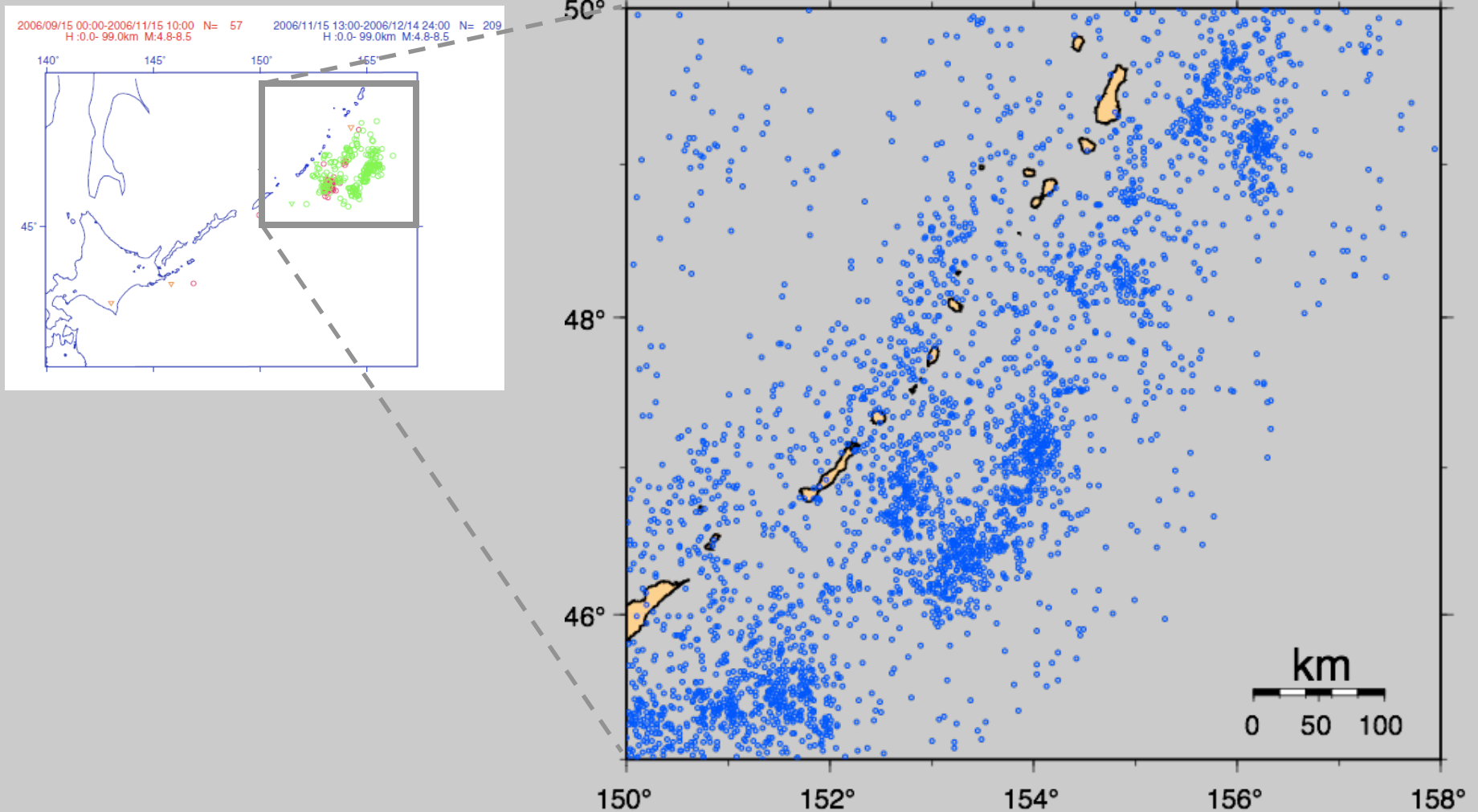
- **Reports:** Inoue (1965), Utsu (1968), Mogi (1969), Ohtake et al. (1977), Wyss (1986), Kisslinger (1986), etc., about 200 papers
- **Significantly wider area than the source:** Inoue (1965), Motoya (1987), Ogata (1988, 1992, 1999)
- **Simulation based on rate- and state-dependent friction law:** Kato, Ohtake and Hirasawa (1997)

The November 2006 and January 2007 Kuril Earthquakes

Collaborative with Shinji Toda)

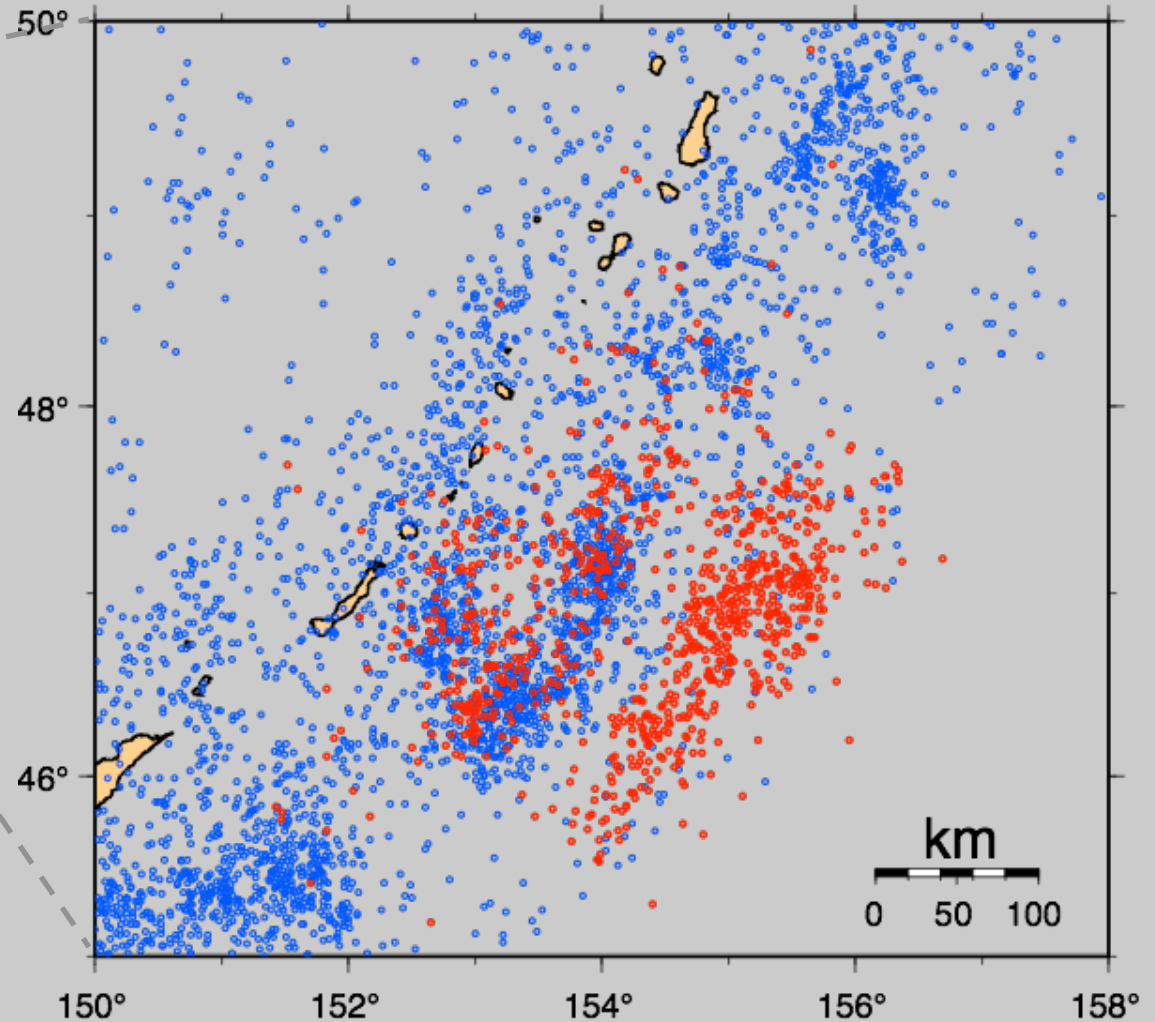
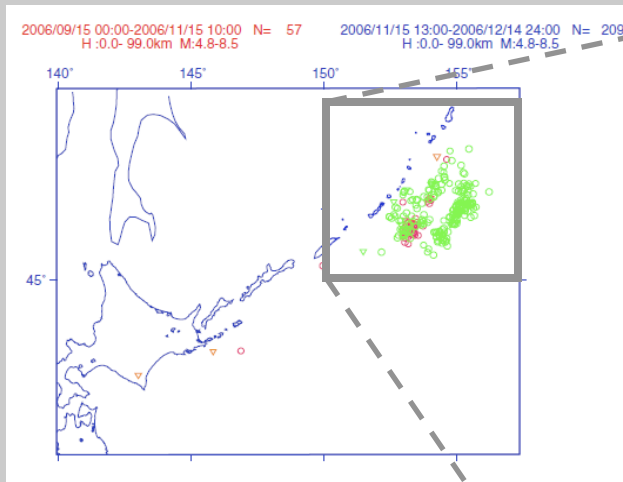
Background seismicity off Kuril Island and aftershocks
of the November 2006 great earthquake of M8.3

USGS/NEIC 1973-2006.11.14



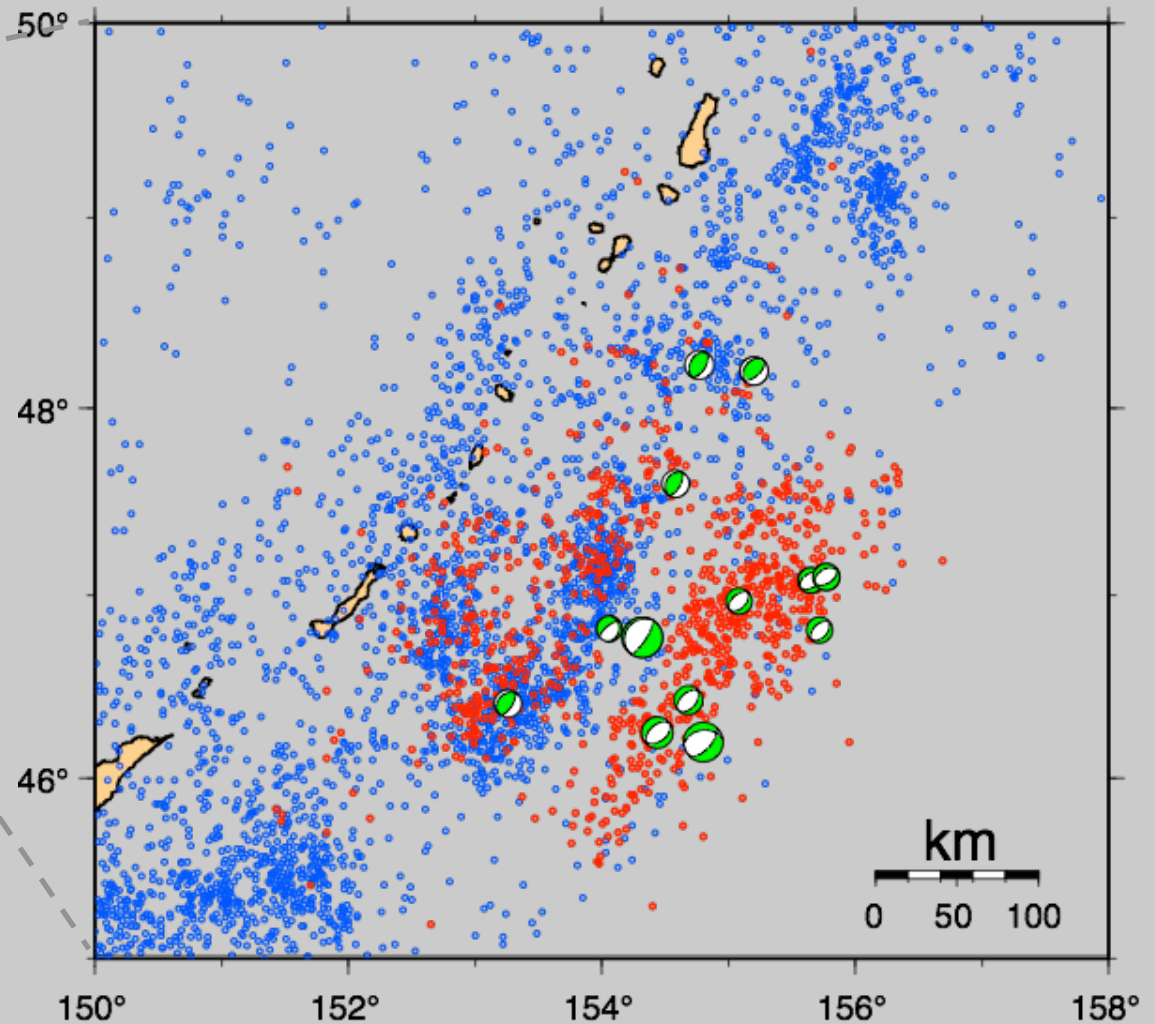
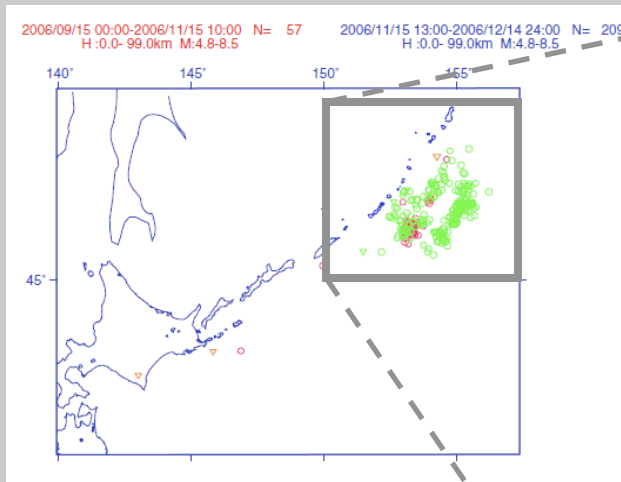
Background seismicity off Kuril Island and aftershocks
of the November 2006 great earthquake of M8.3

USGS/NEIC 1973-2006.11.14 2006.11.15-2007.1.13



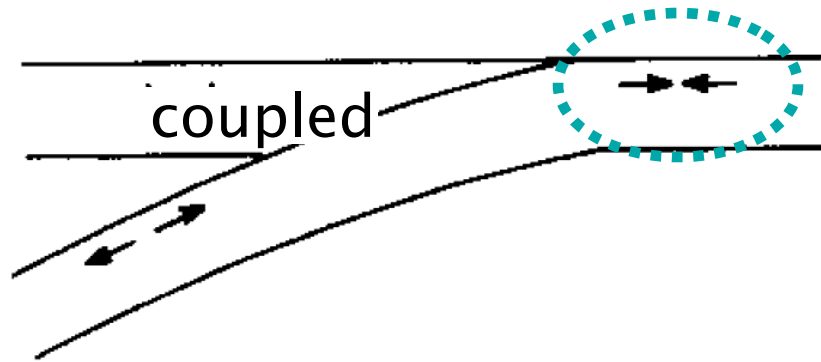
Background seismicity off Kuril Island and aftershocks
of the November 2006 great earthquake of M8.3

USGS/NEIC 1973-2006.11.14 2006.11.15-2007.1.13

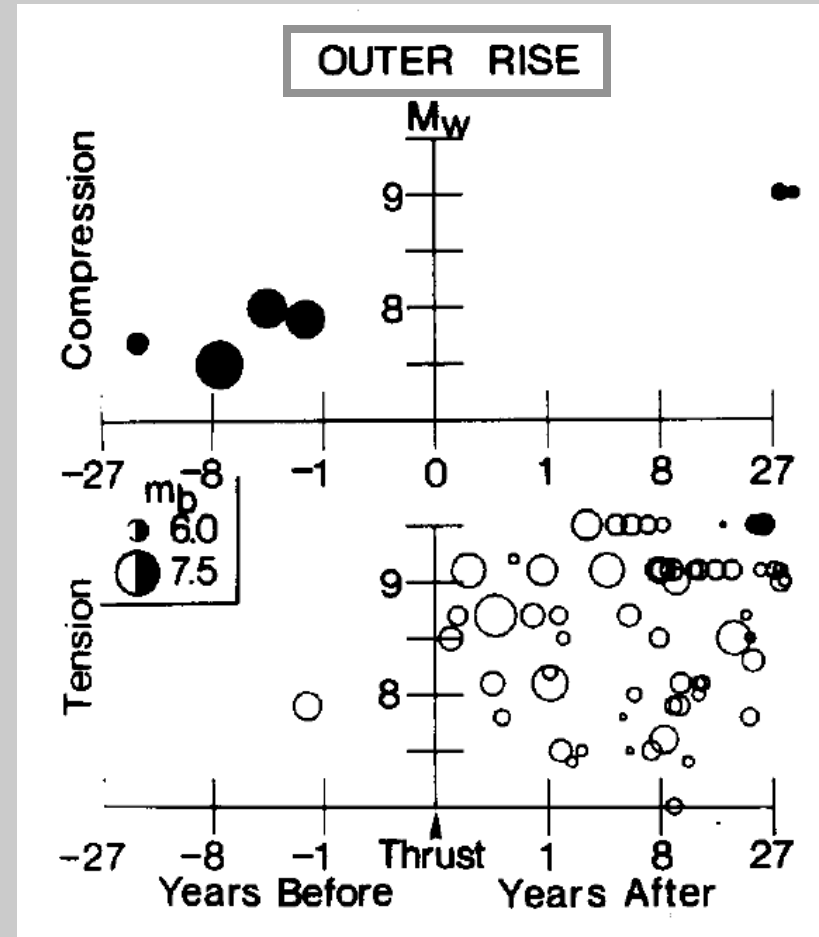
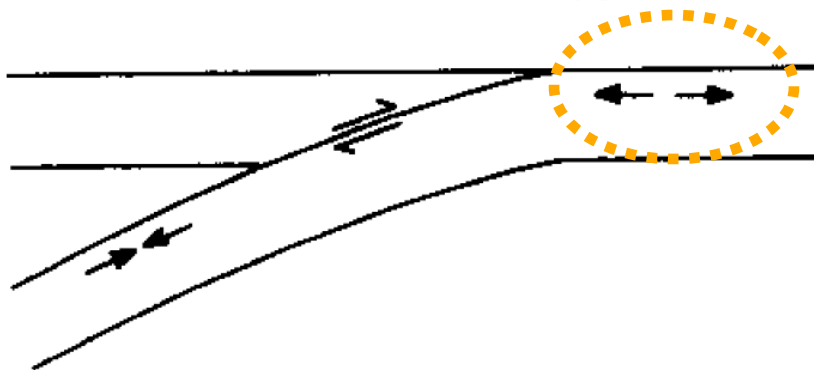


Lay, Astiz, Kanamori and Christensen, 1989, PEPI

Before Thrust

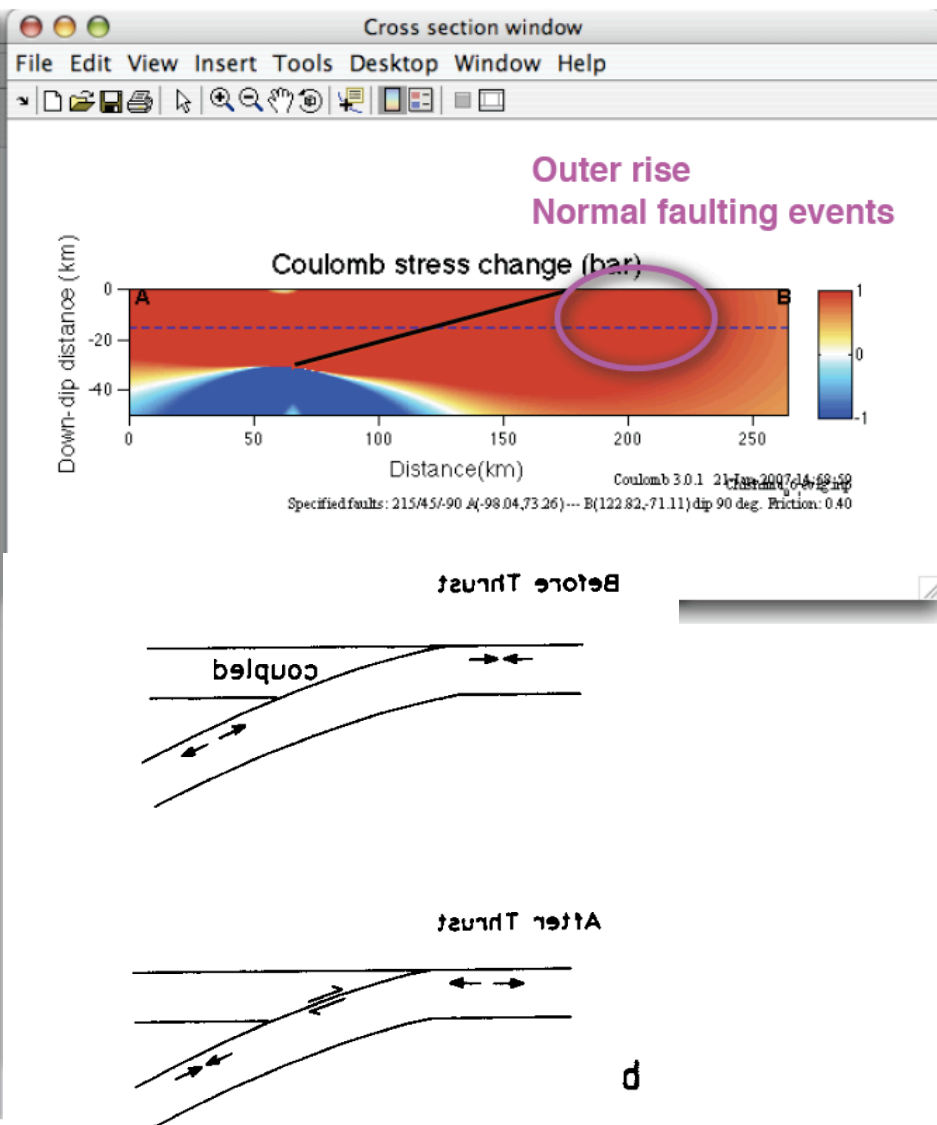
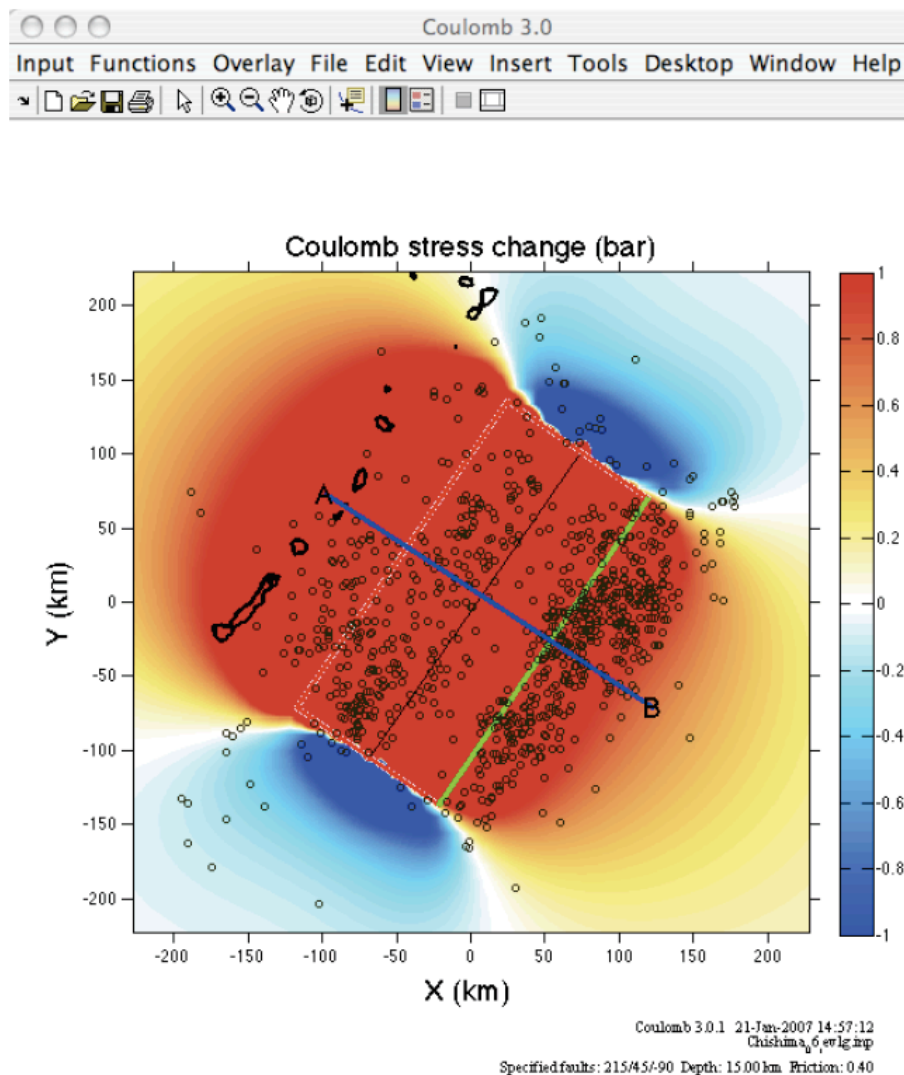


After Thrust

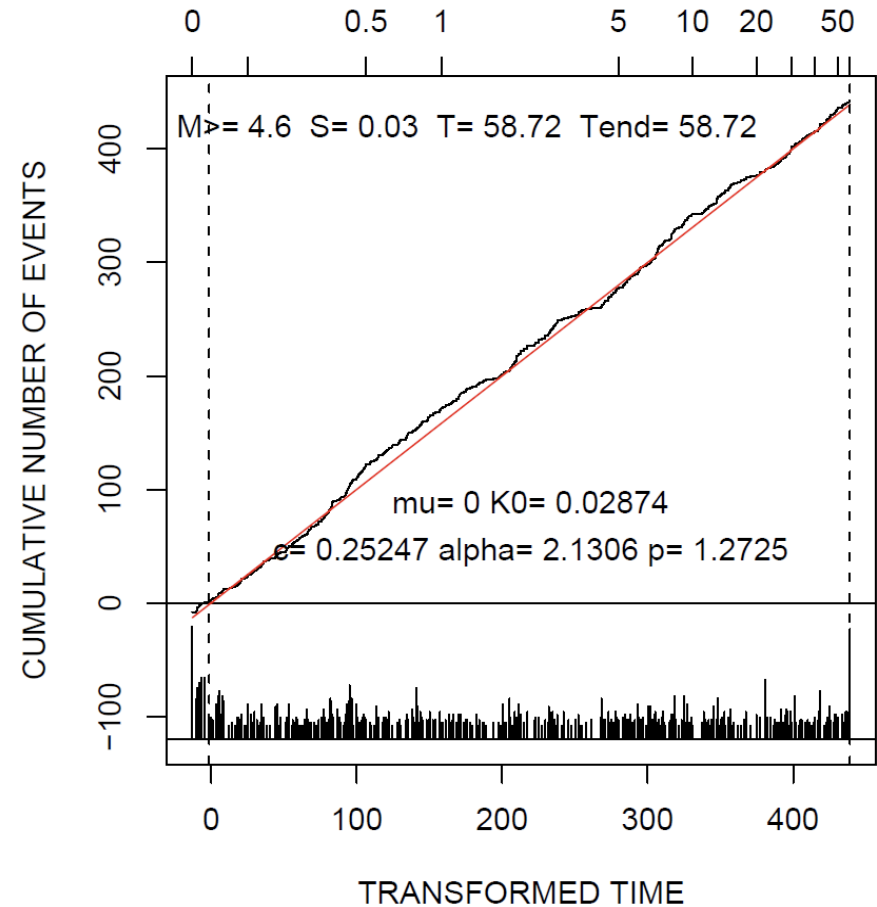
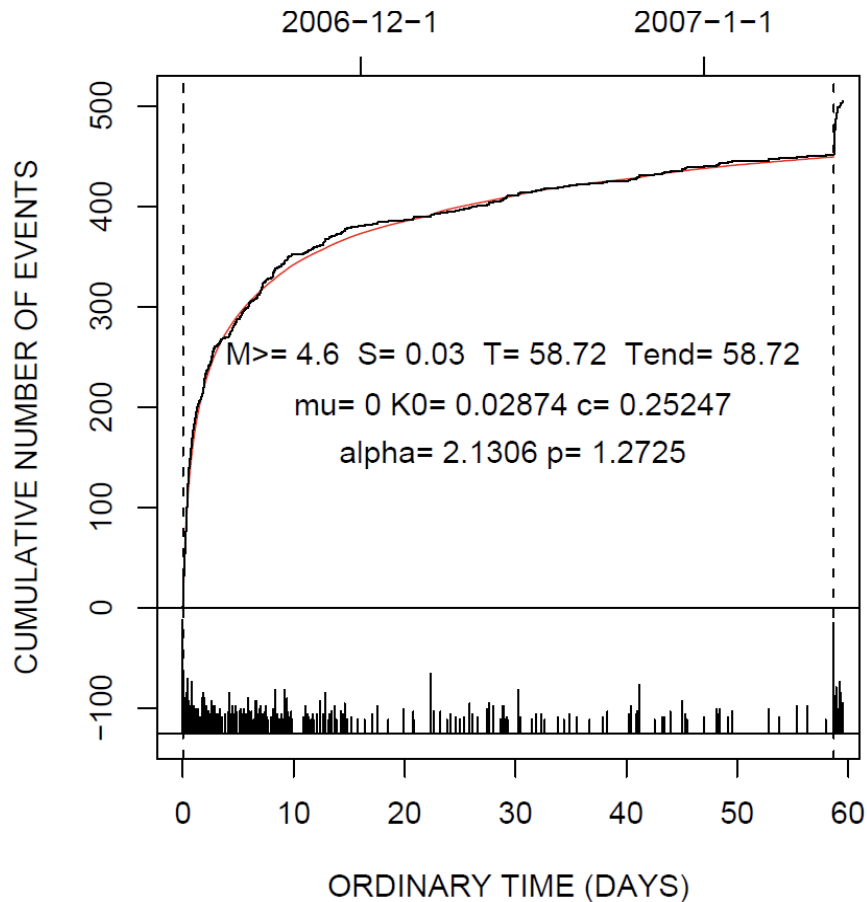


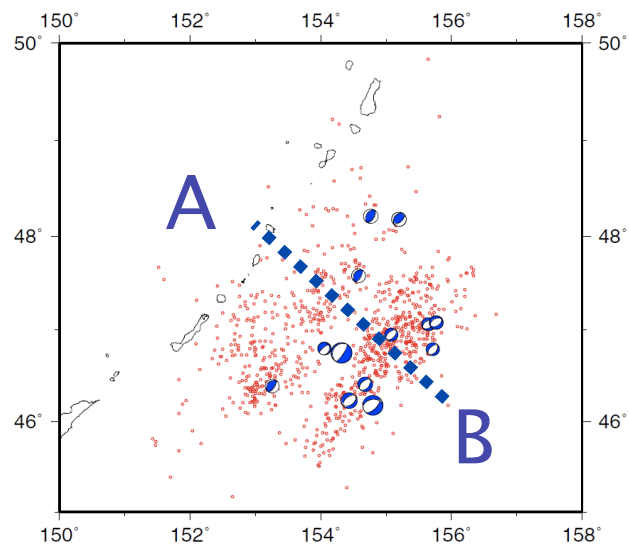
2006年11月15日千島列島東方海溝型地震による 周辺正断層へのクーロン応力変化

Coulomb 3.0 (Toda, Stein, Lin & Sevilgen) による計算結果

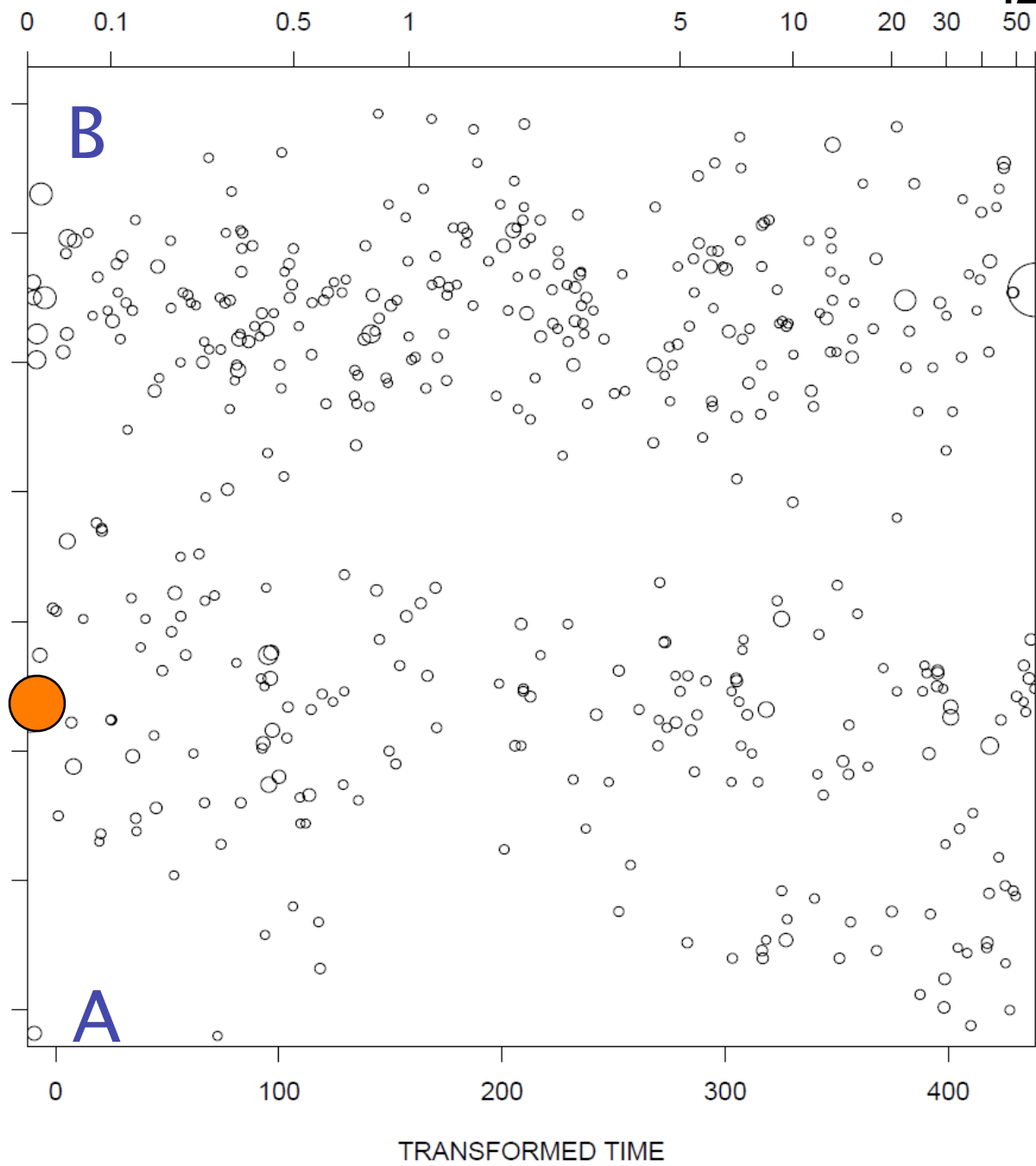


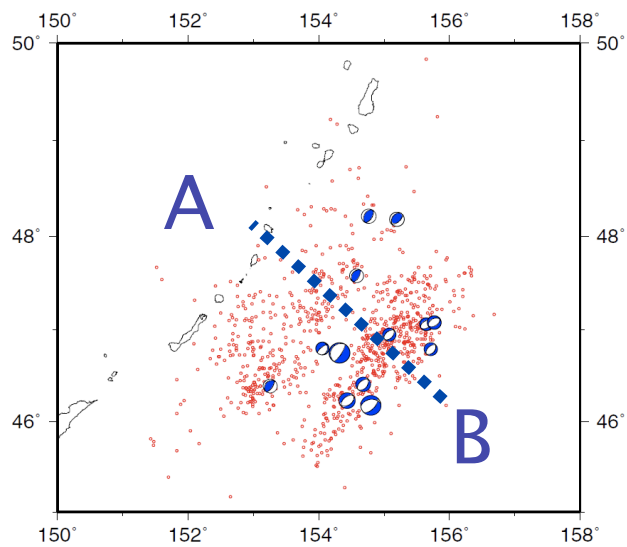
Aftershock activity of 15Nov2006 event (M8.3)



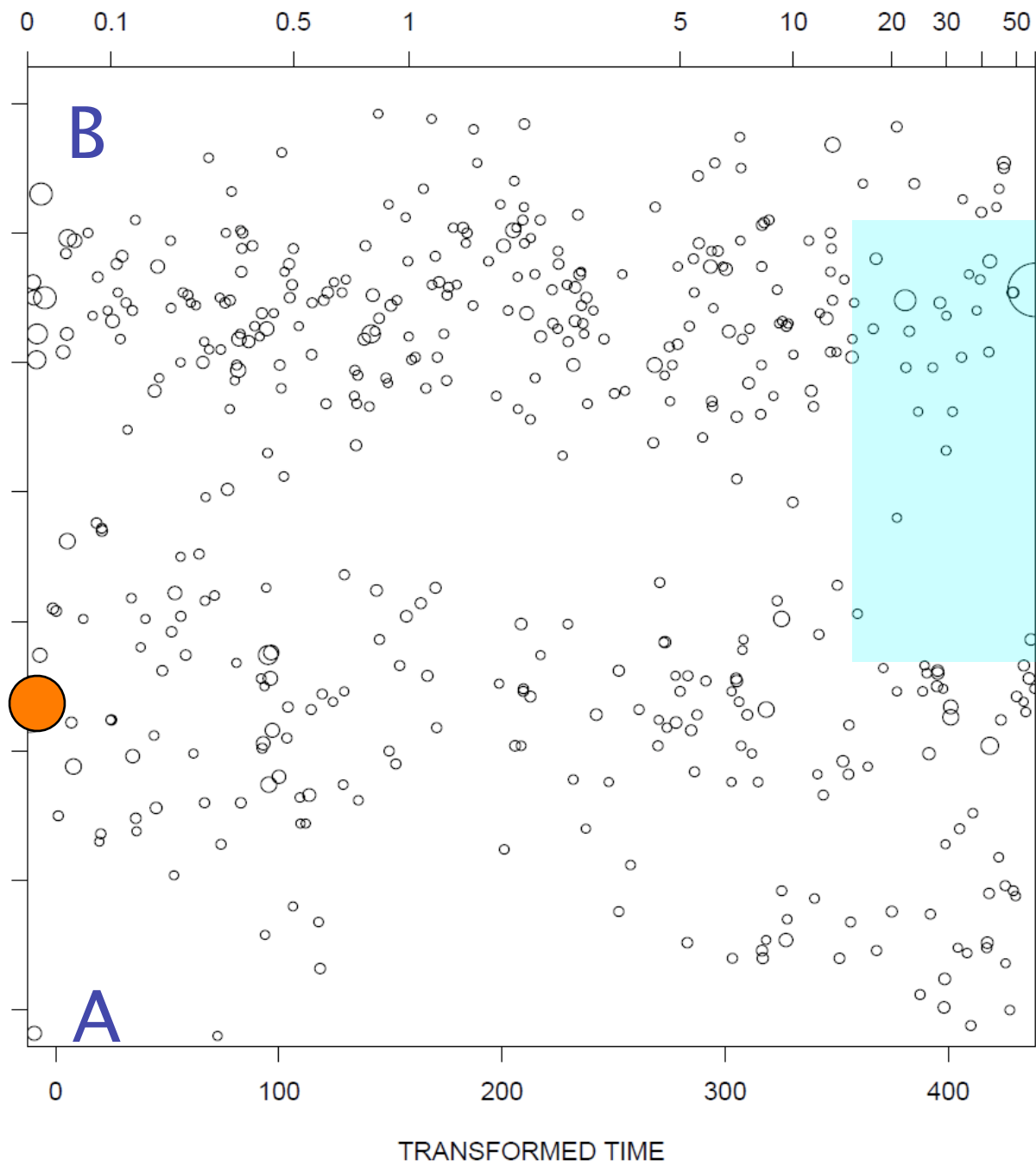


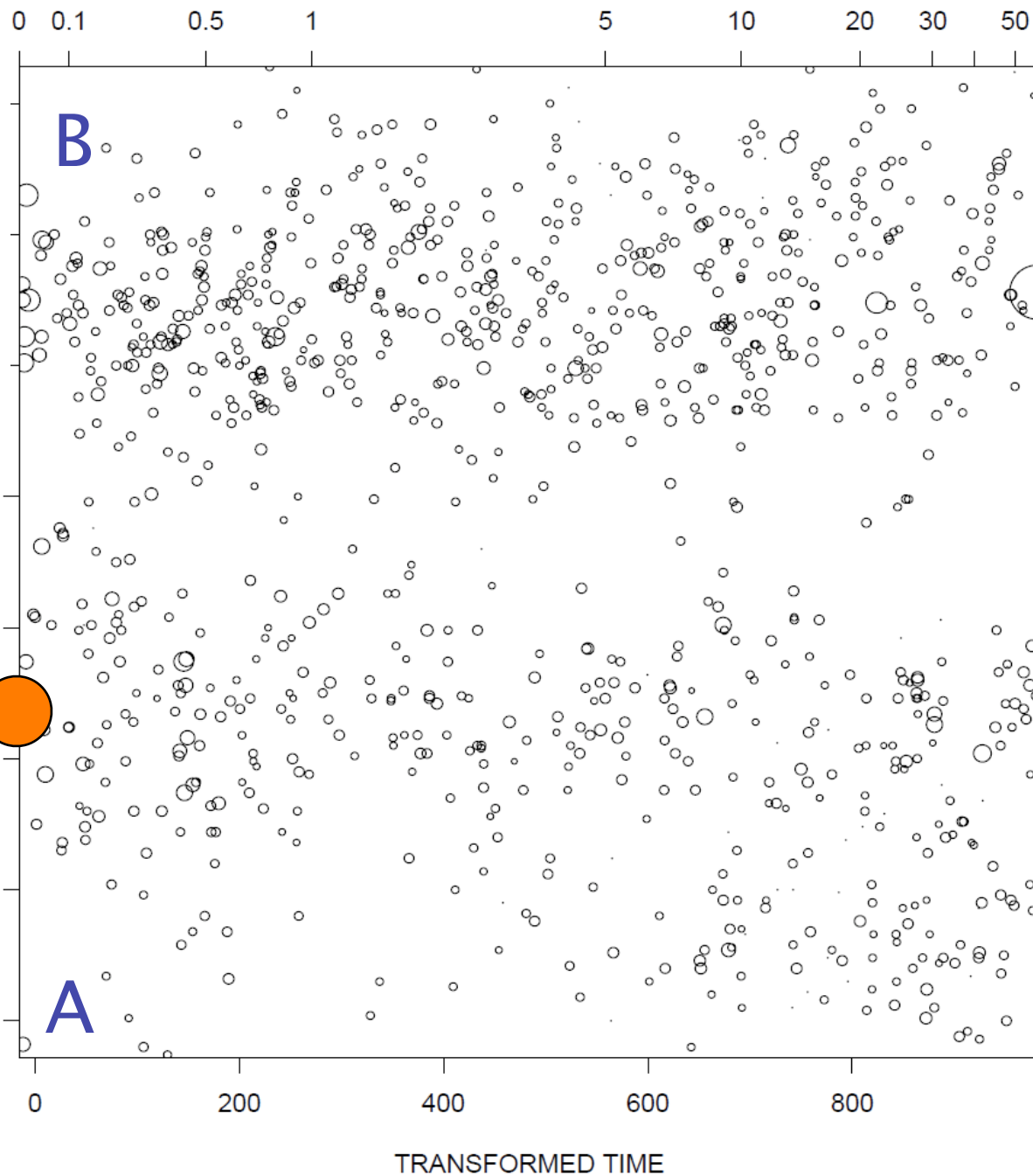
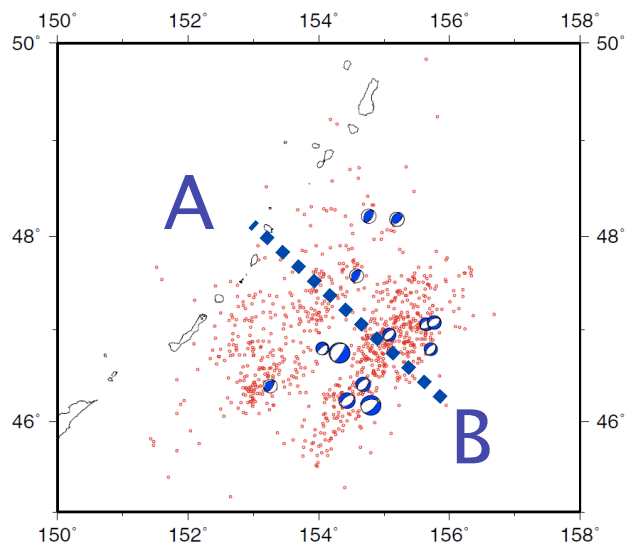
M \geq 4.6



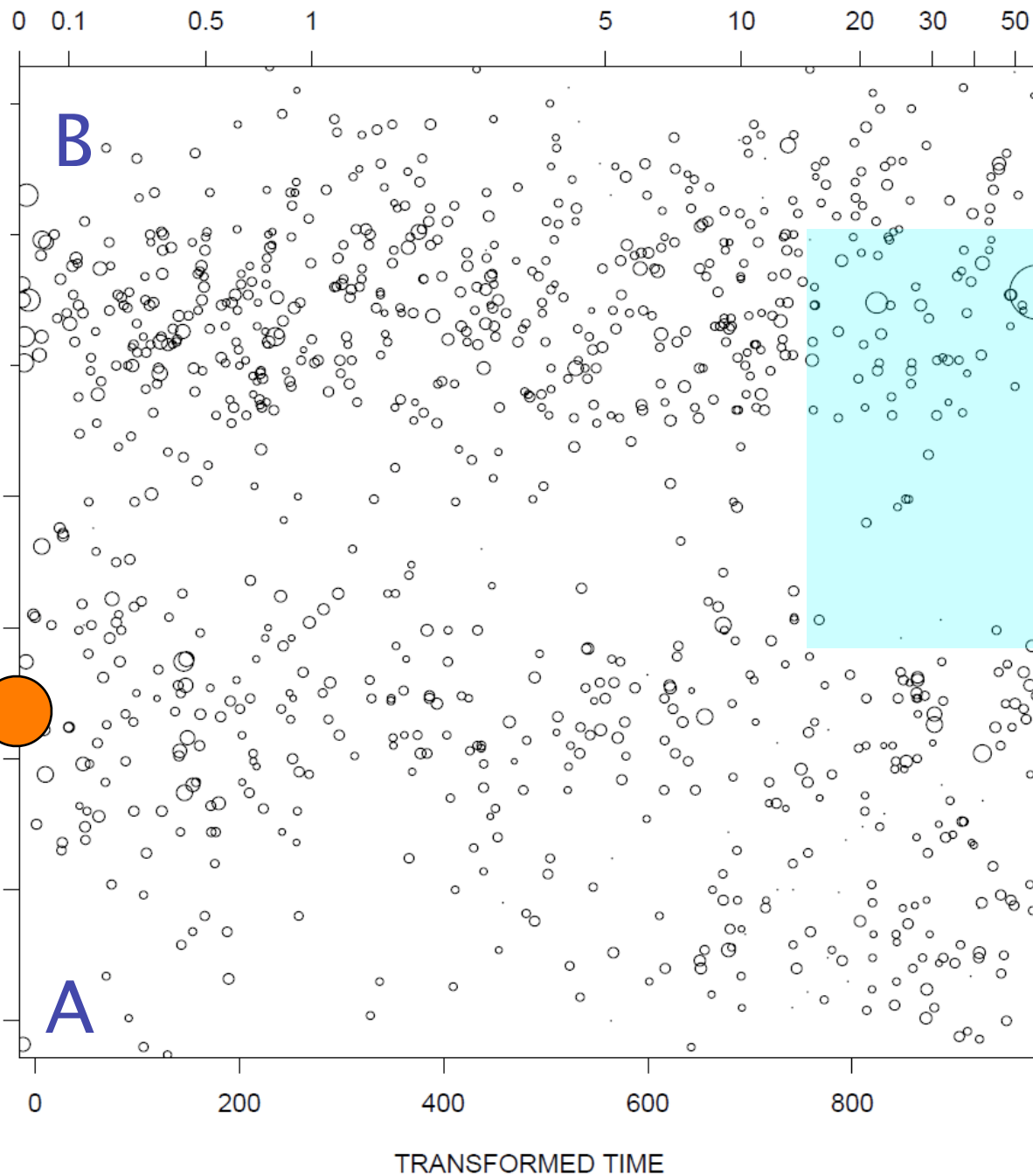
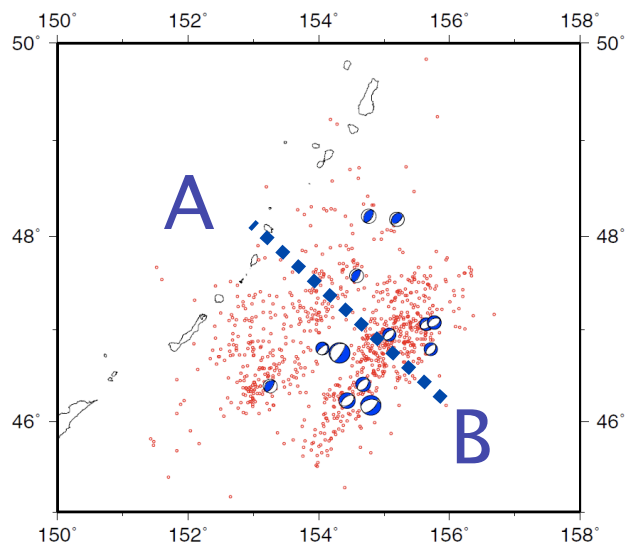


M \geq 4.6

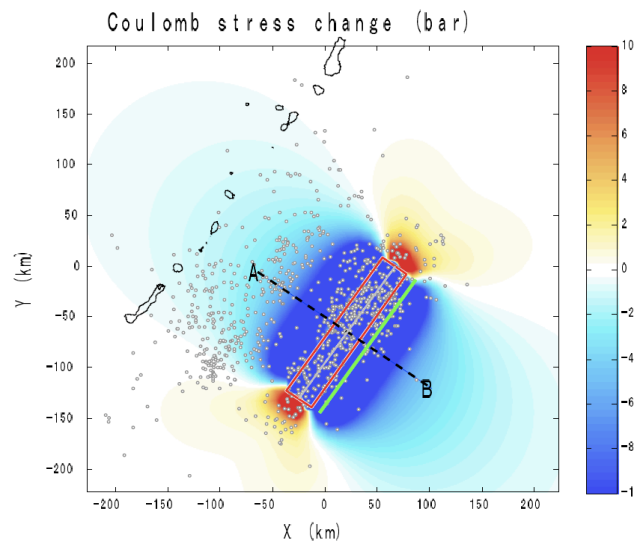




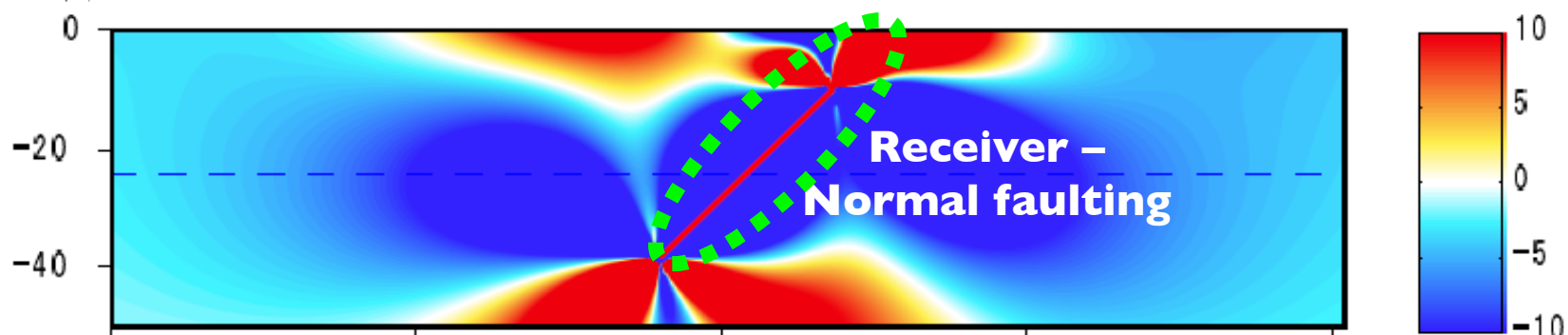
**All detected
events**



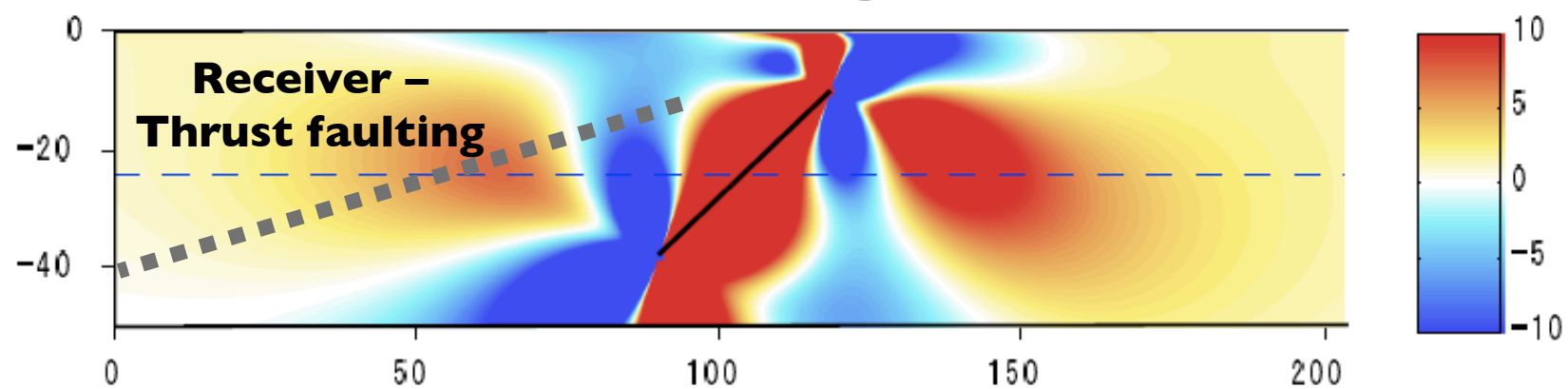
**All detected
events**



stress change (bar)



A Coulomb stress change (bar)



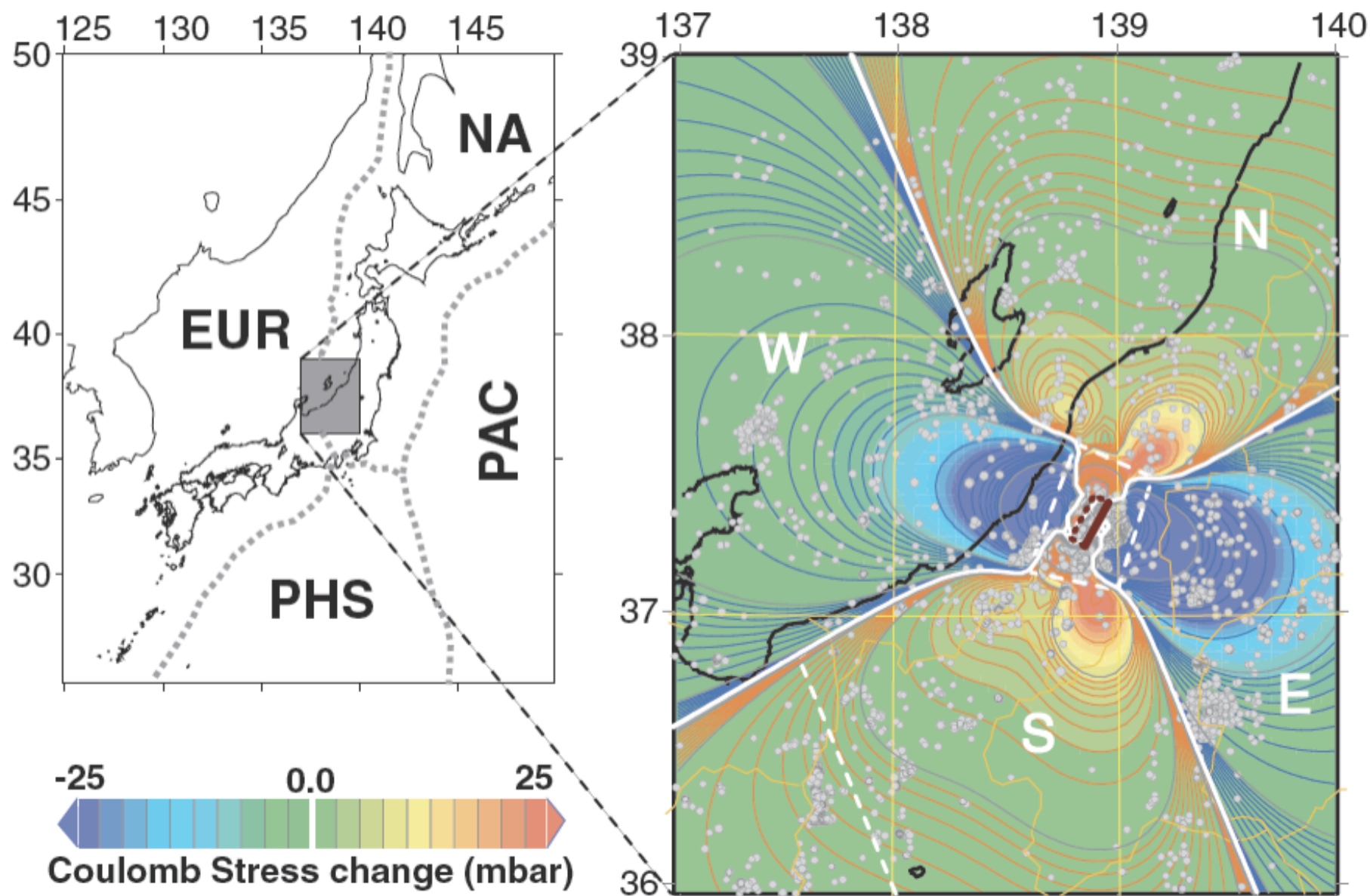
B

The 2004 Chuetsu Earthquake

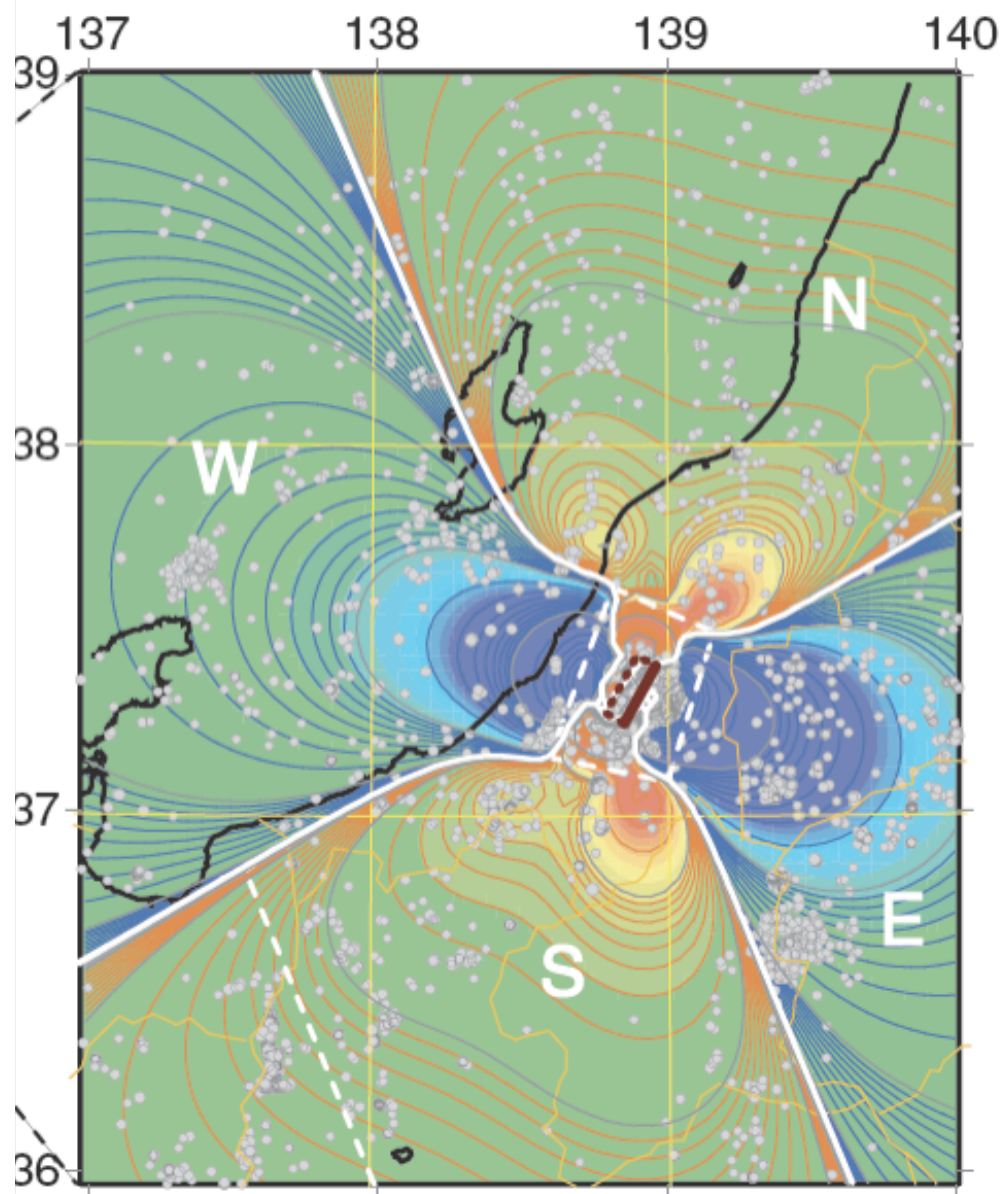
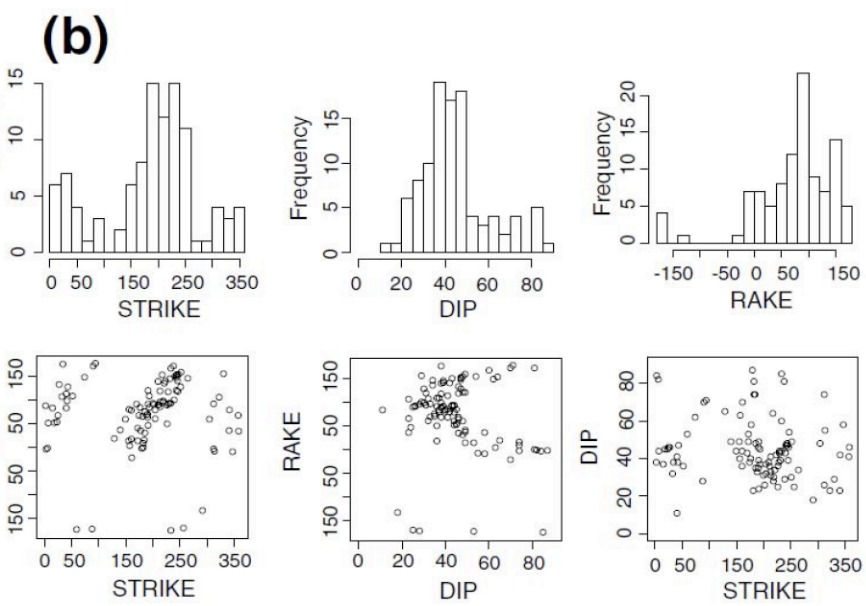
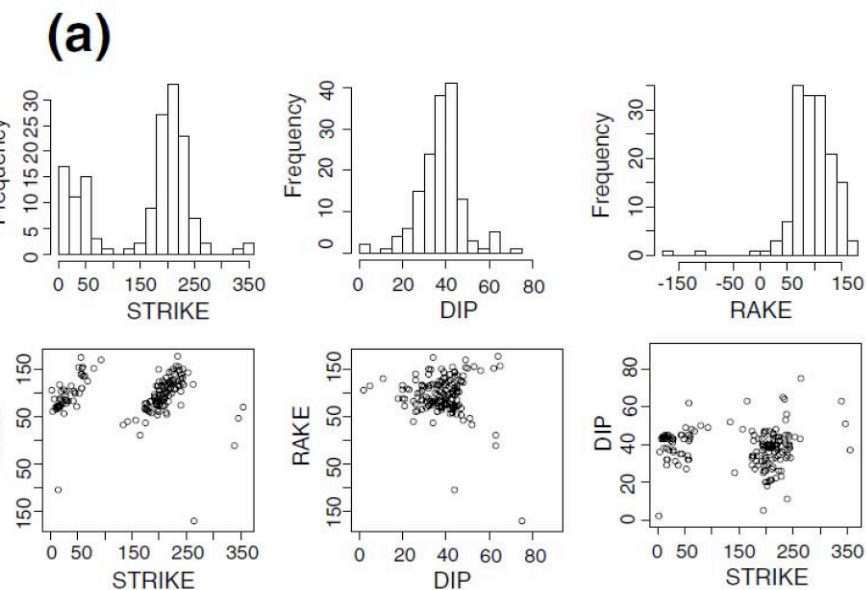
1997/01/01 - 2004/10/30 Number of events = 4060

46

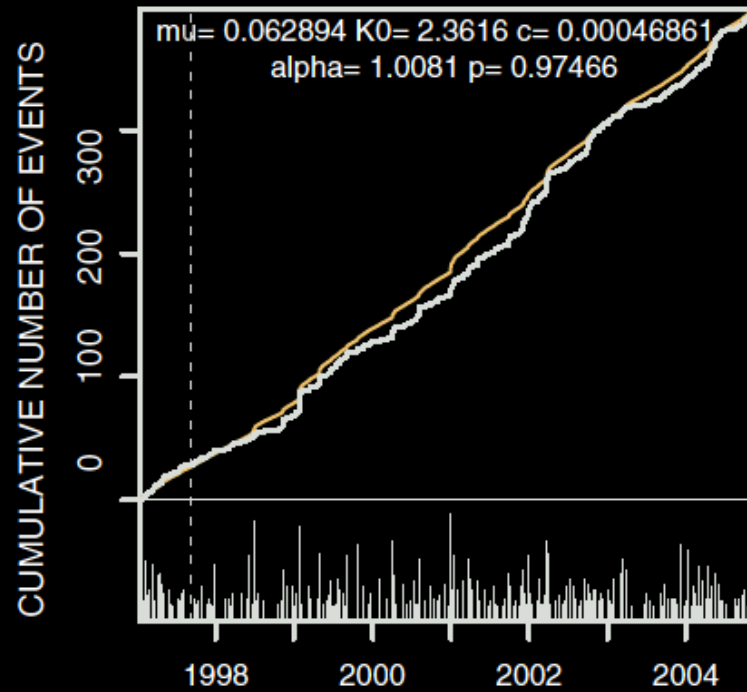
Depth ≤ 25.0 km, $M \geq 2.0$



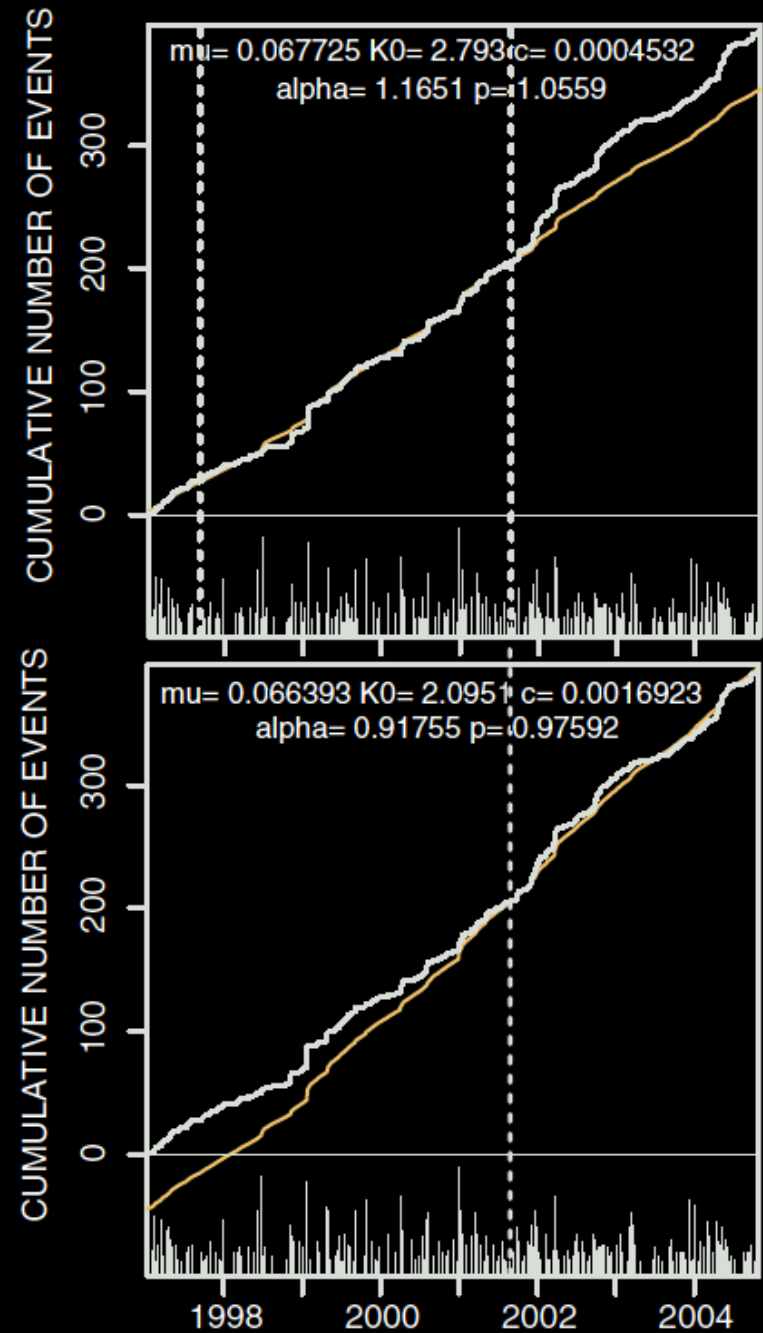
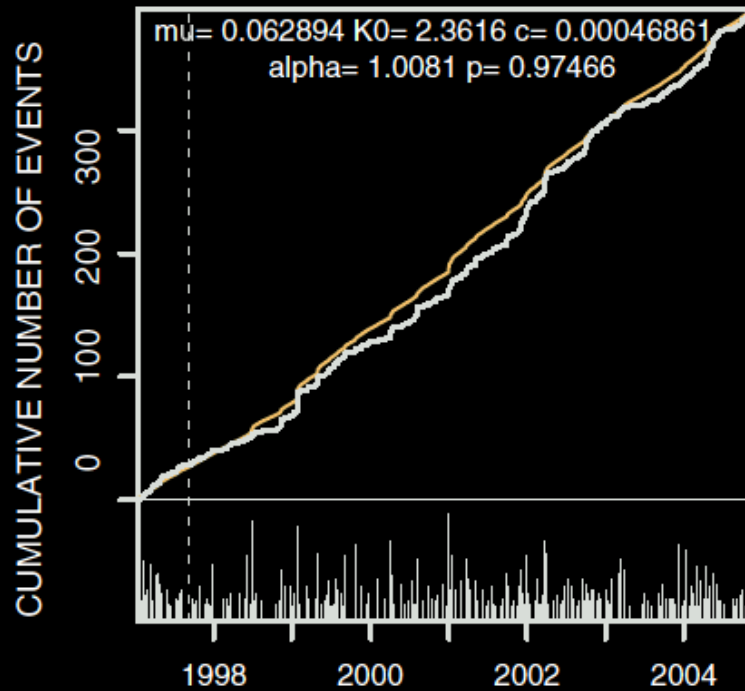
1997/01/01 - 2004/10/30 Number of events = 4060

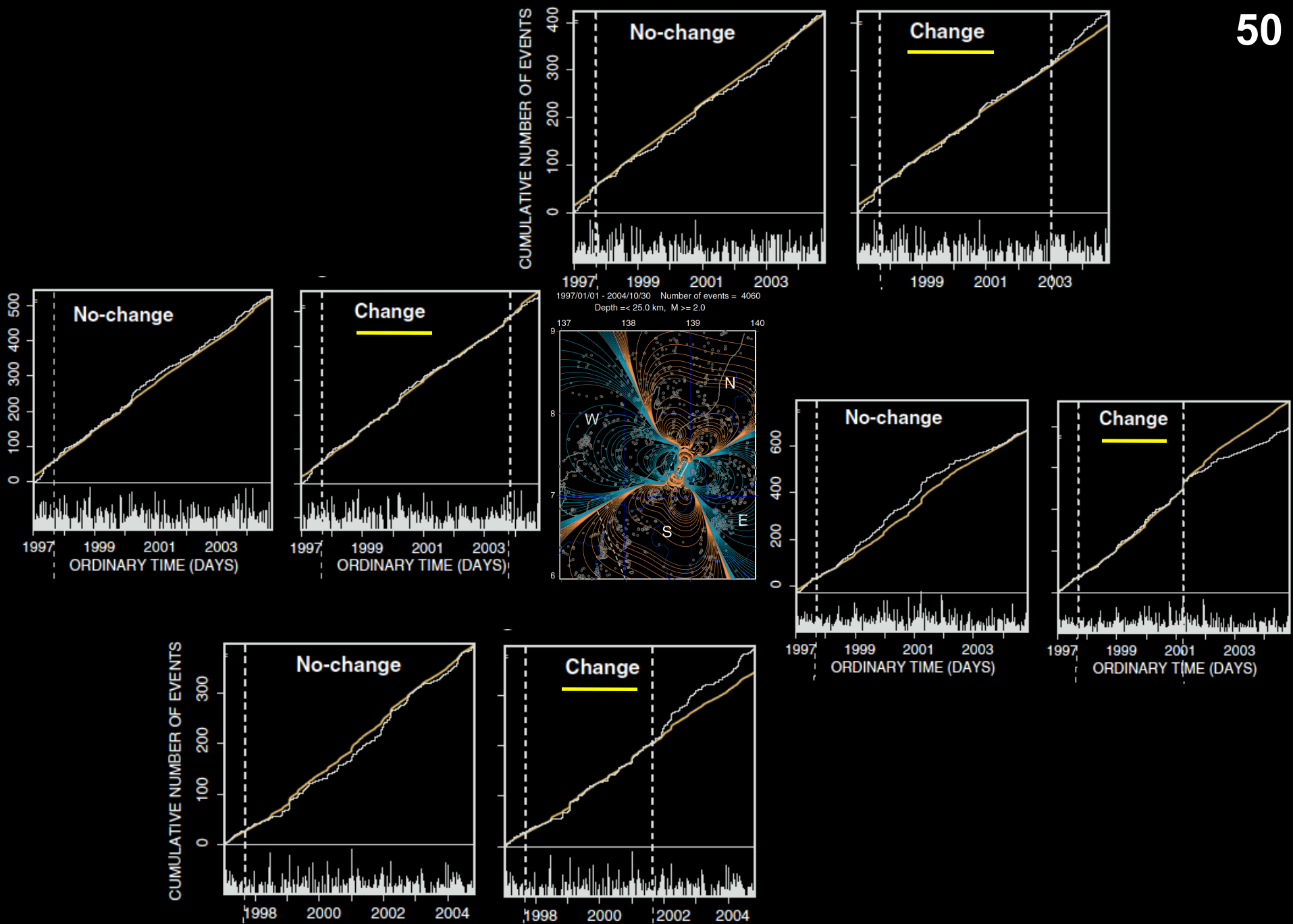
Depth ≤ 25.0 km, $M \geq 2.0$ 

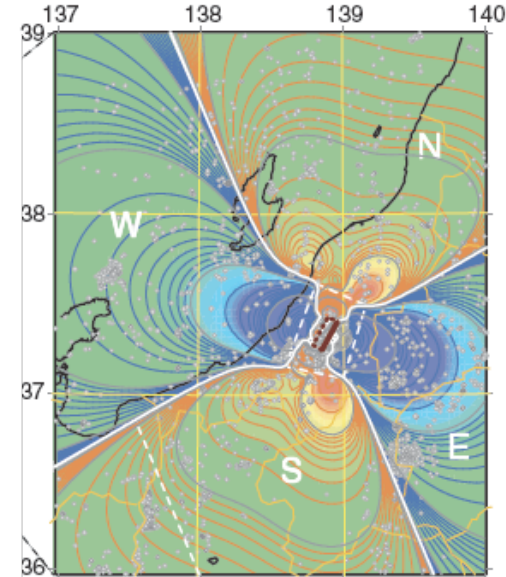
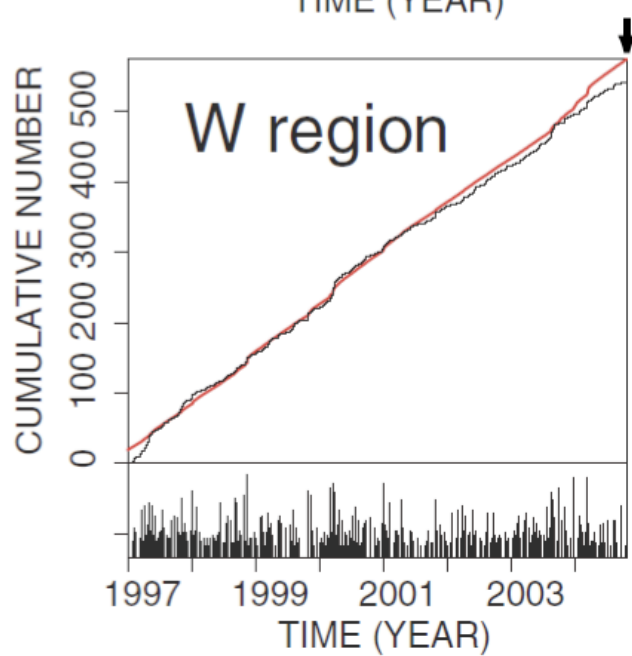
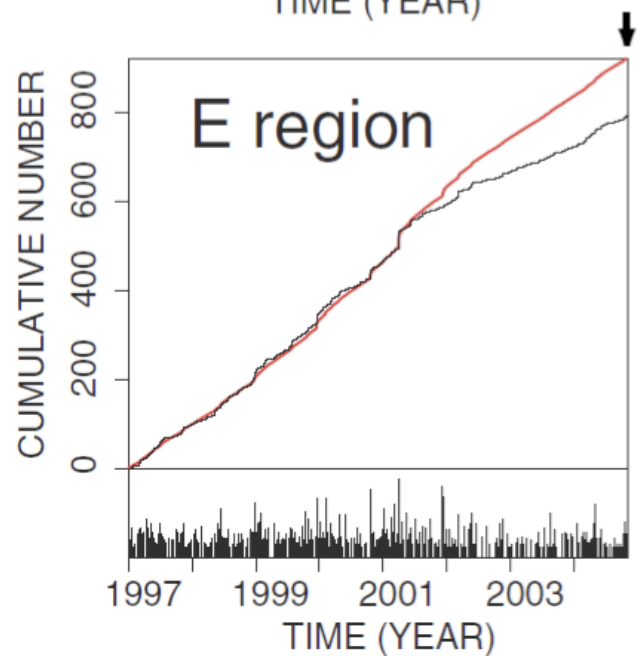
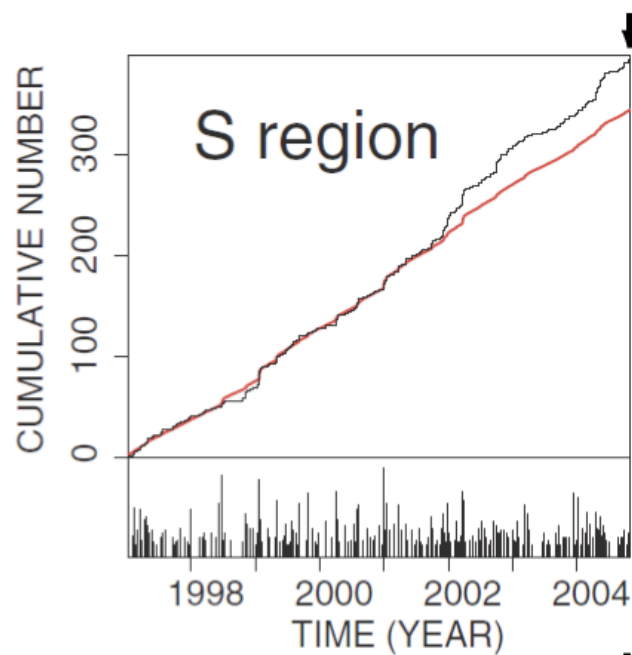
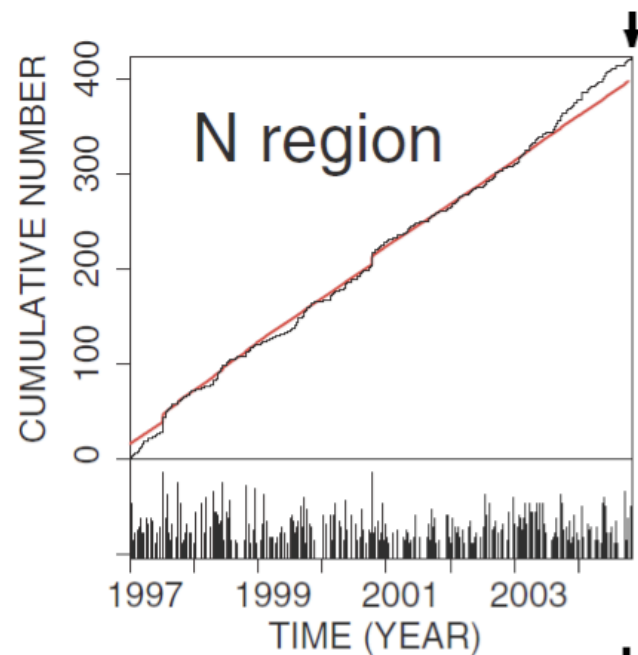
No-Change

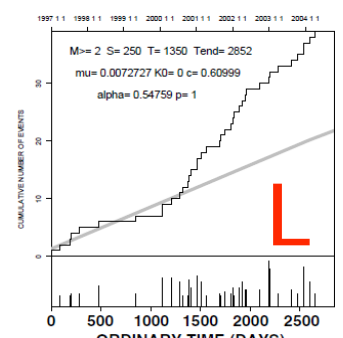
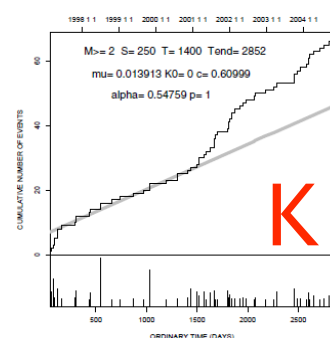
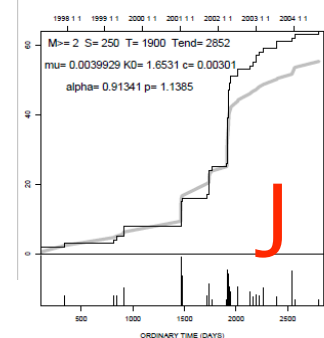
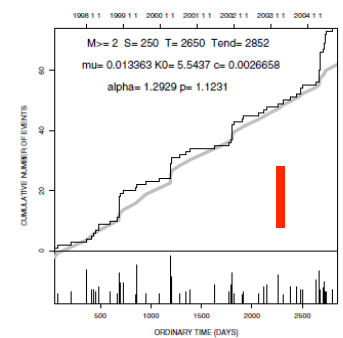
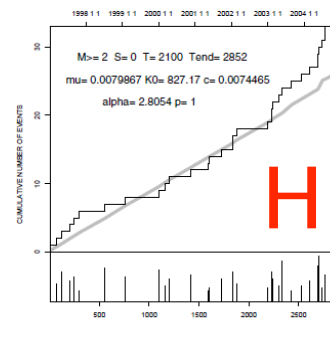
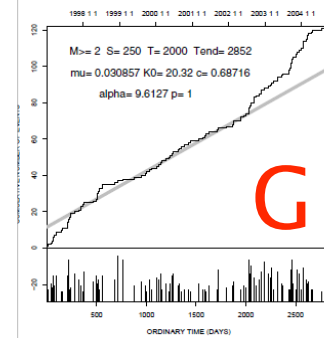
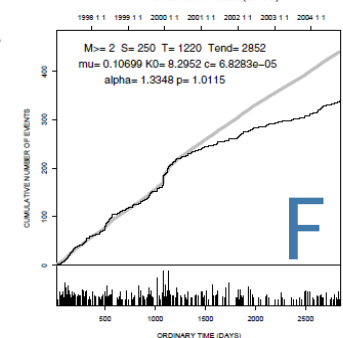
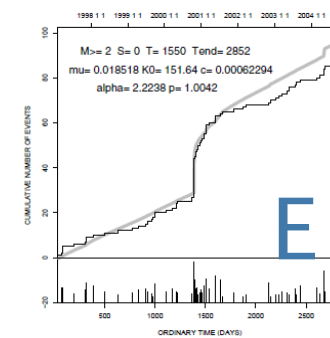
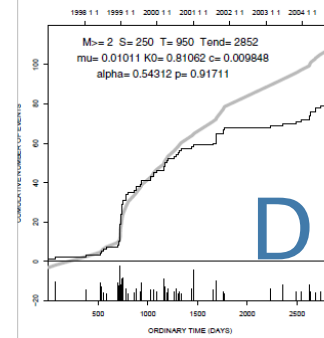
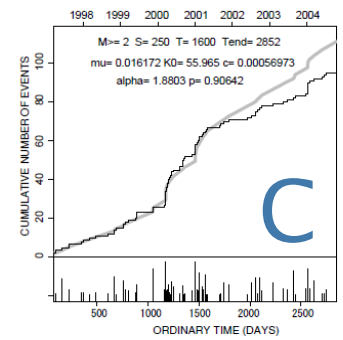
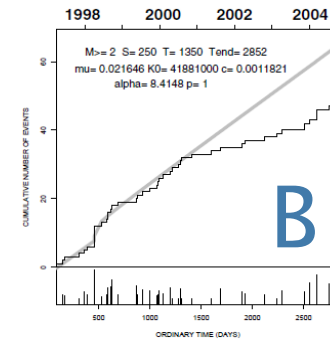
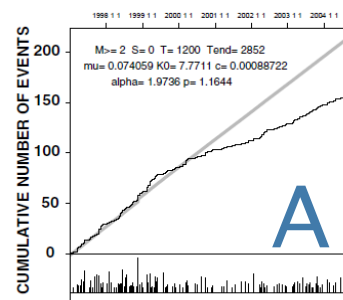
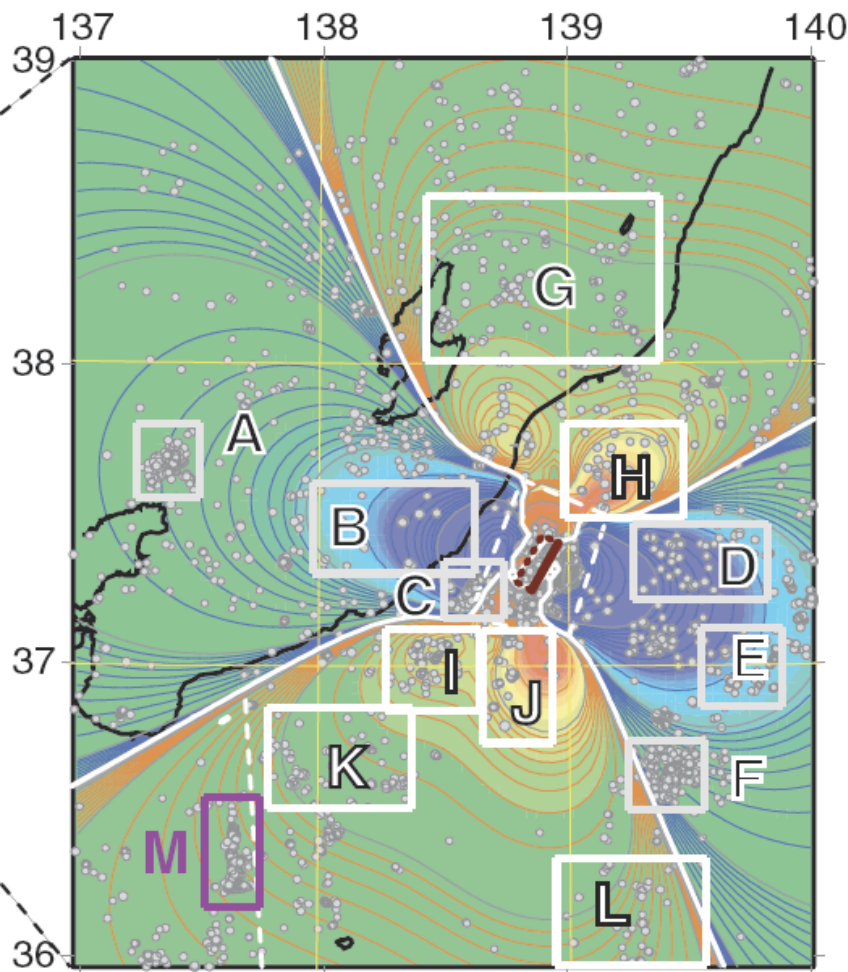


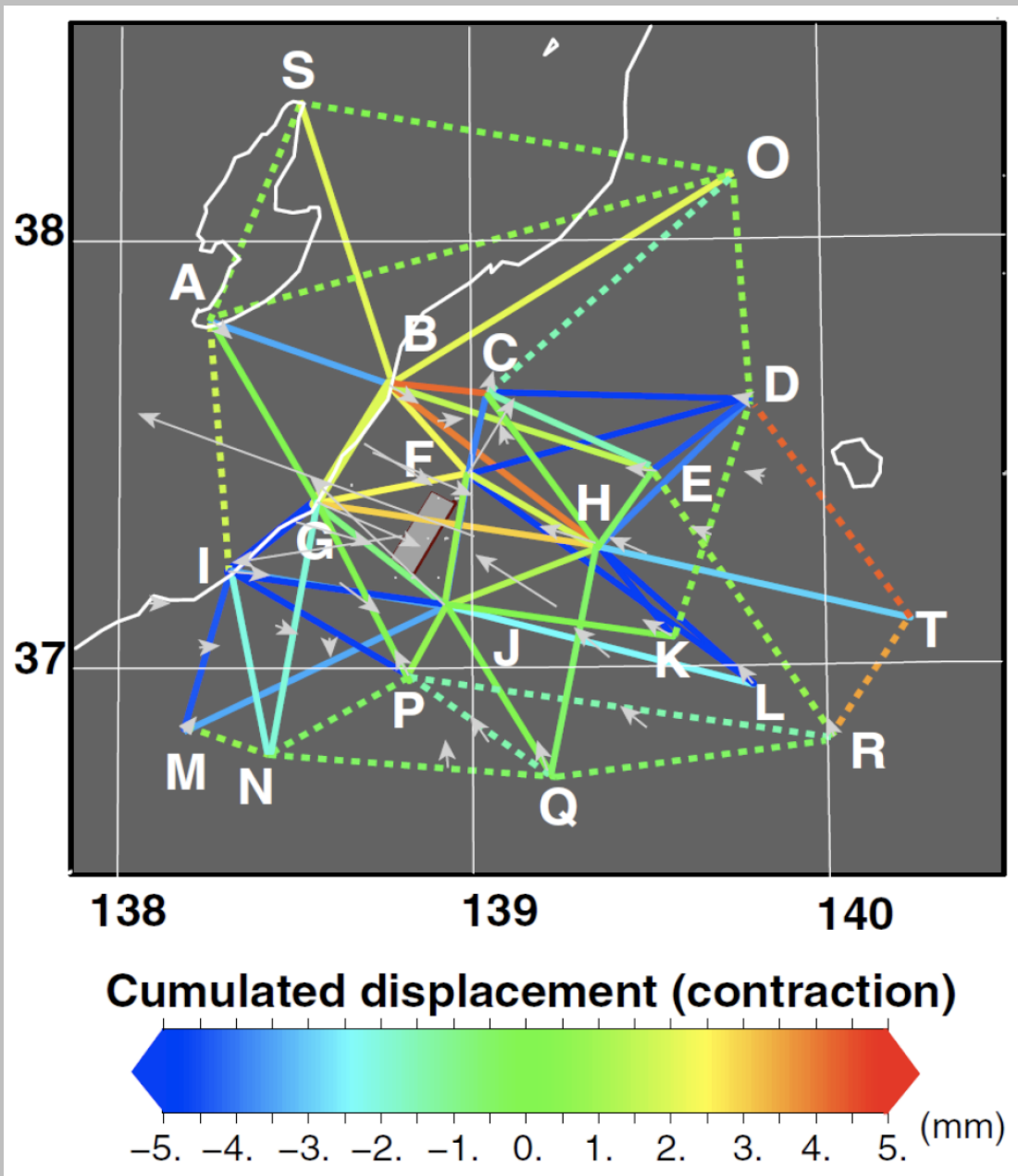
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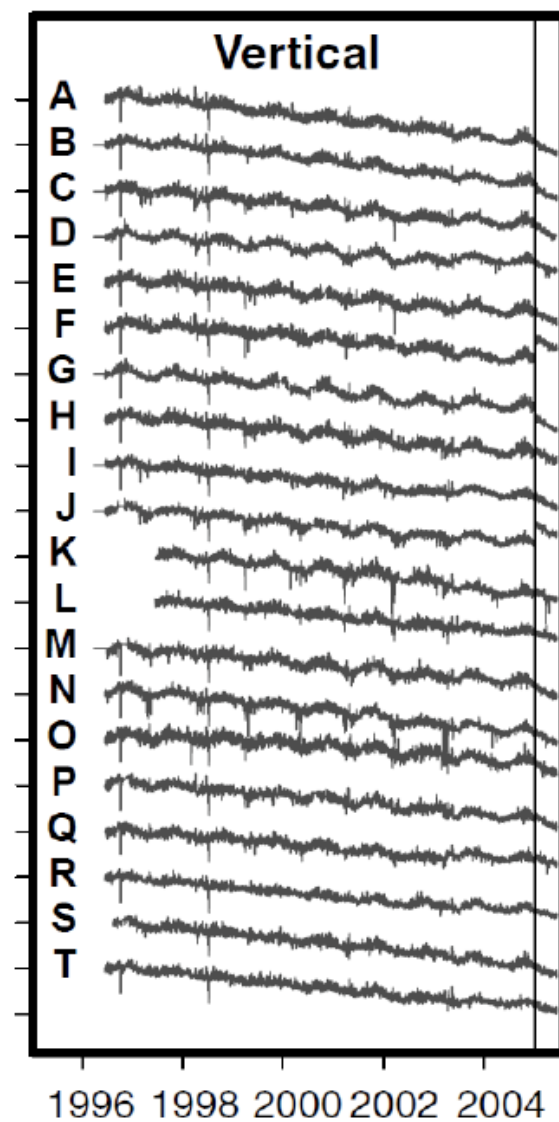
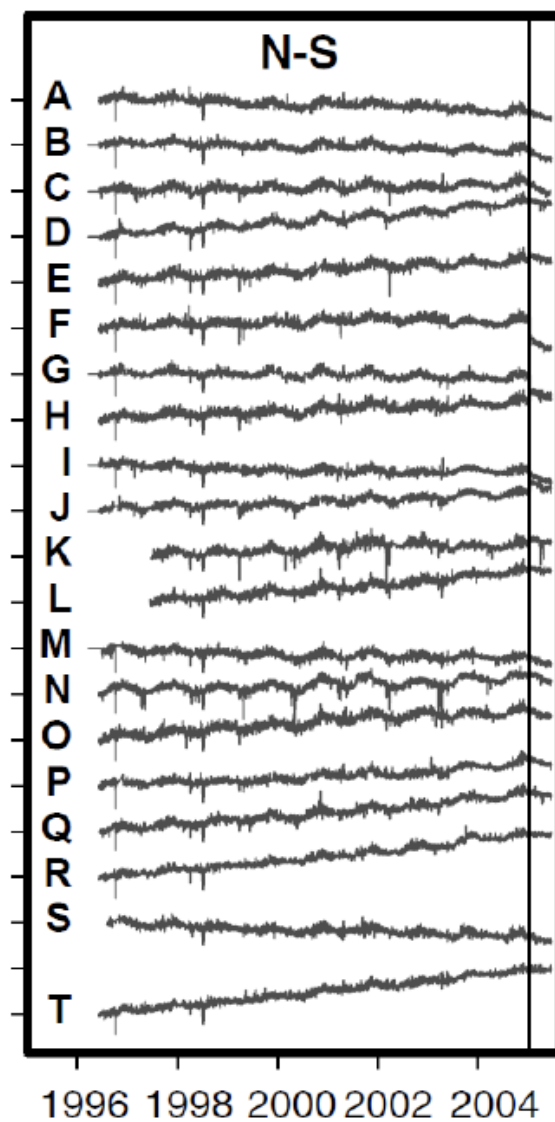
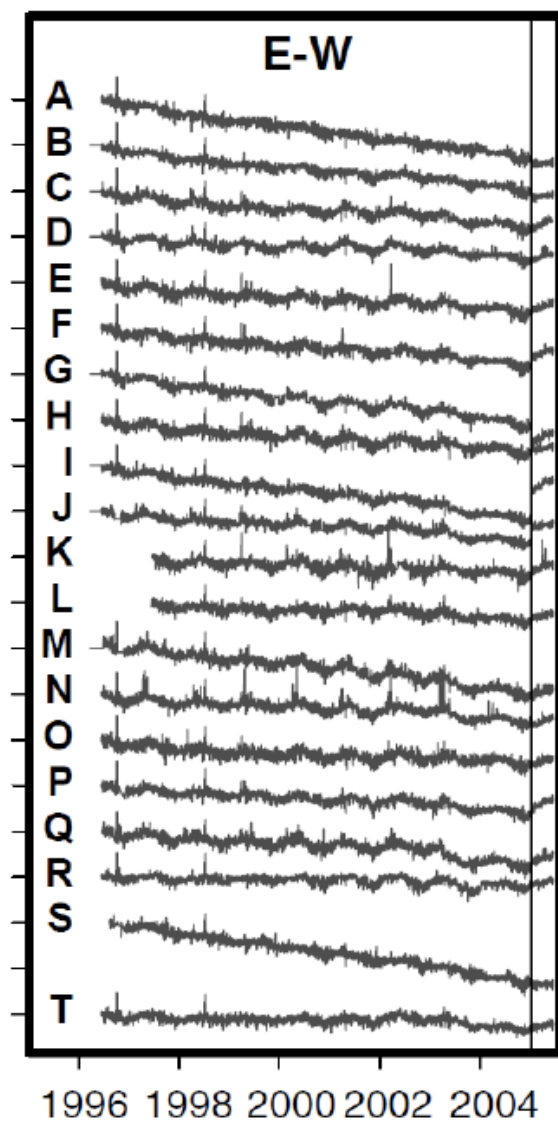


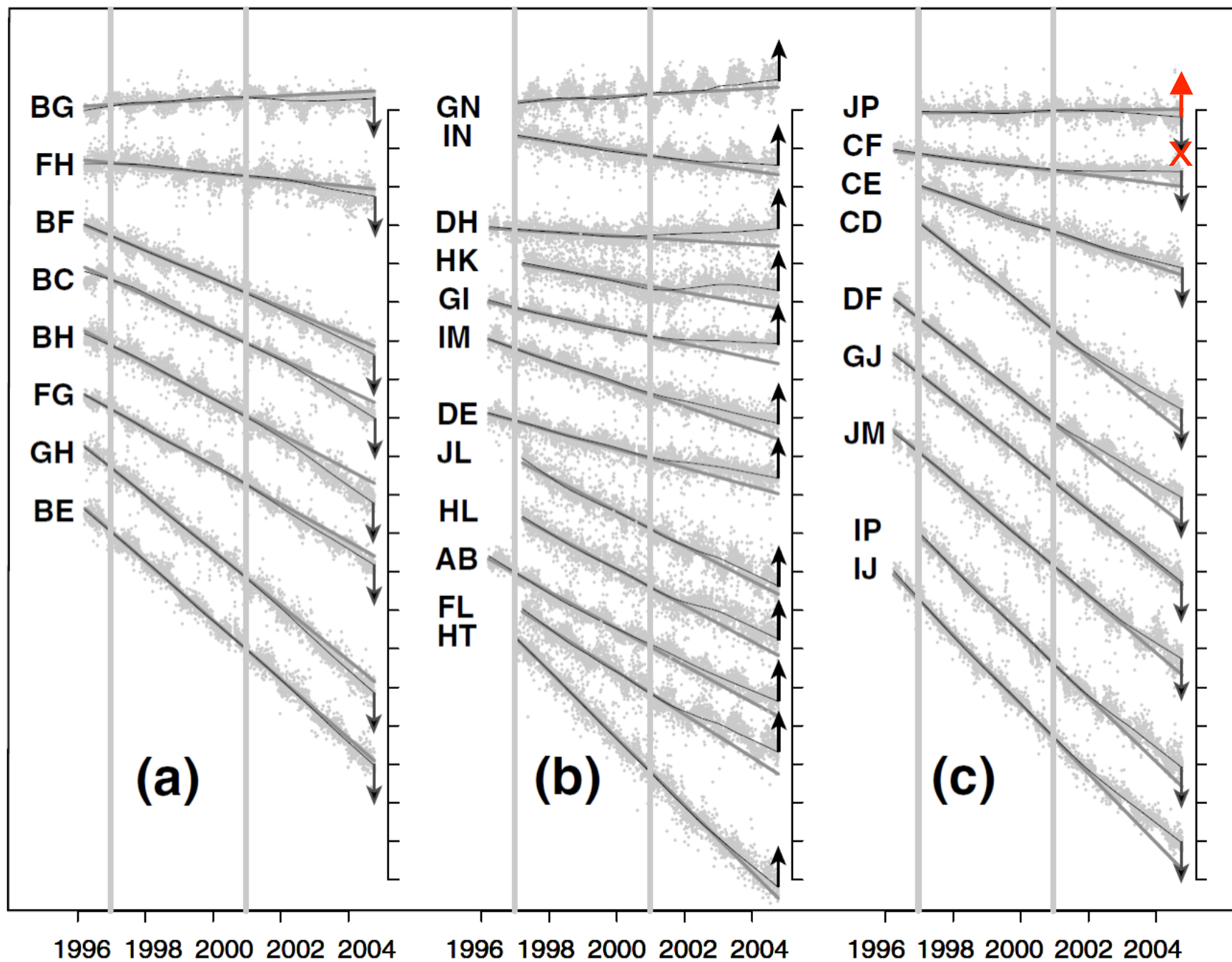


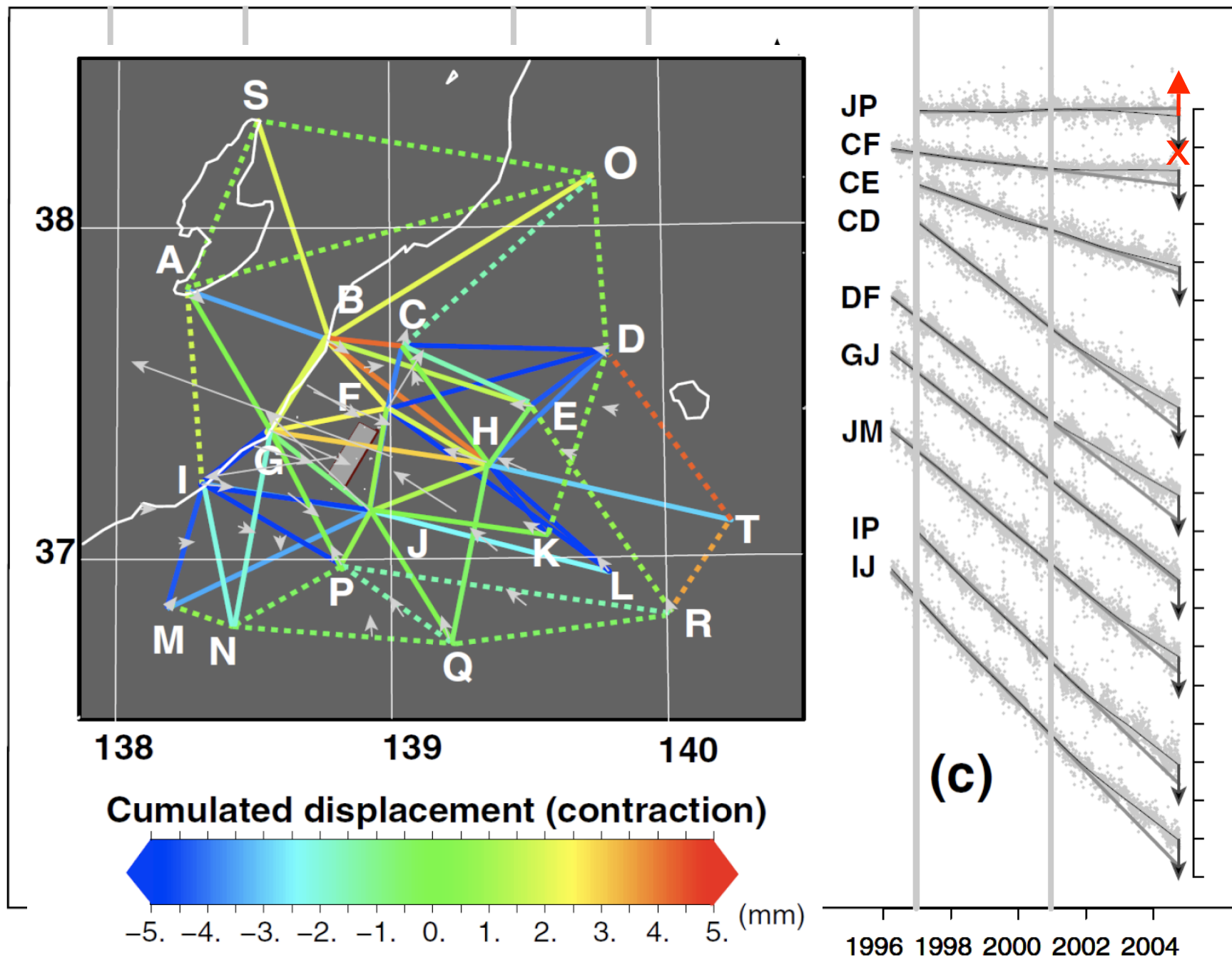


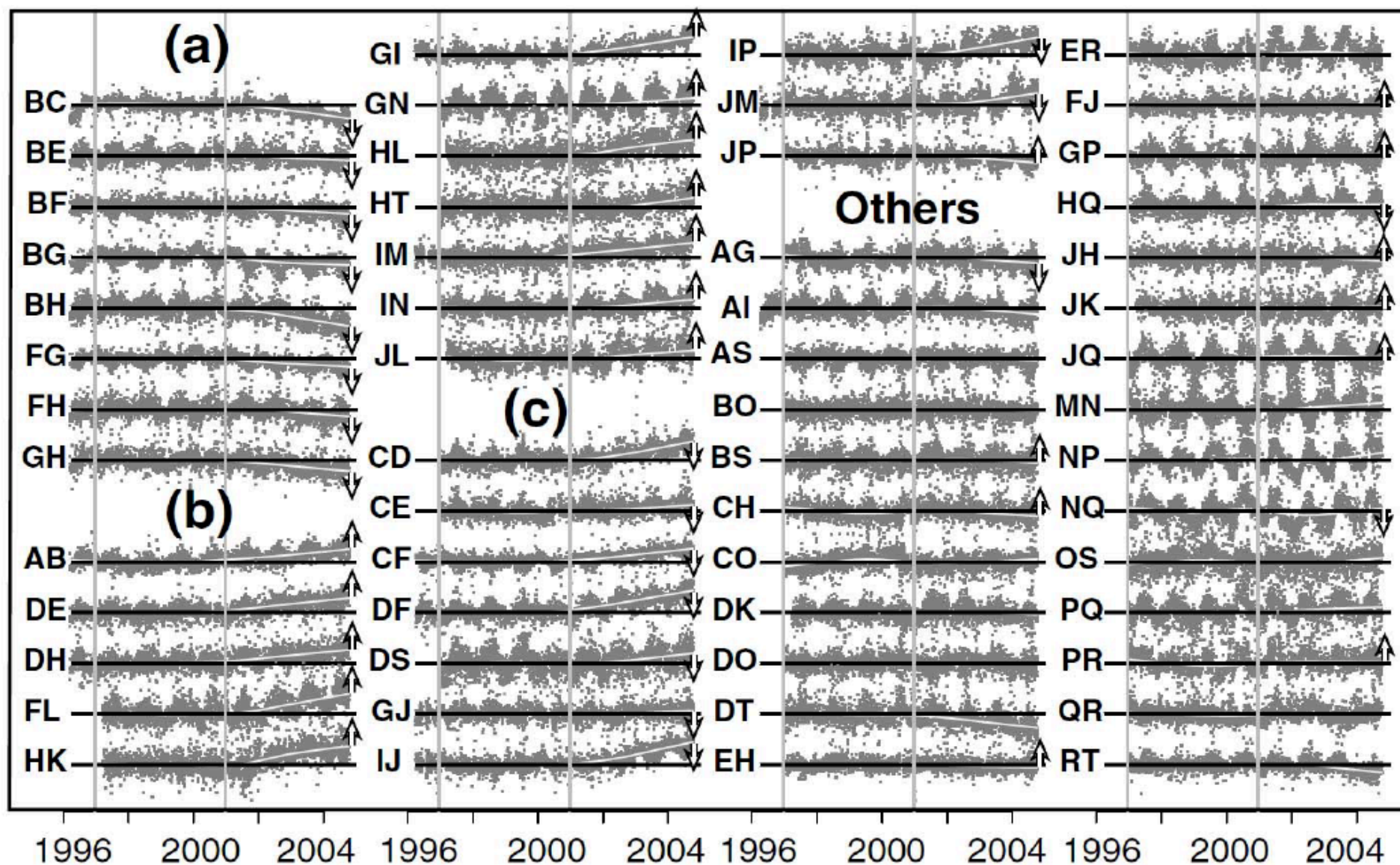


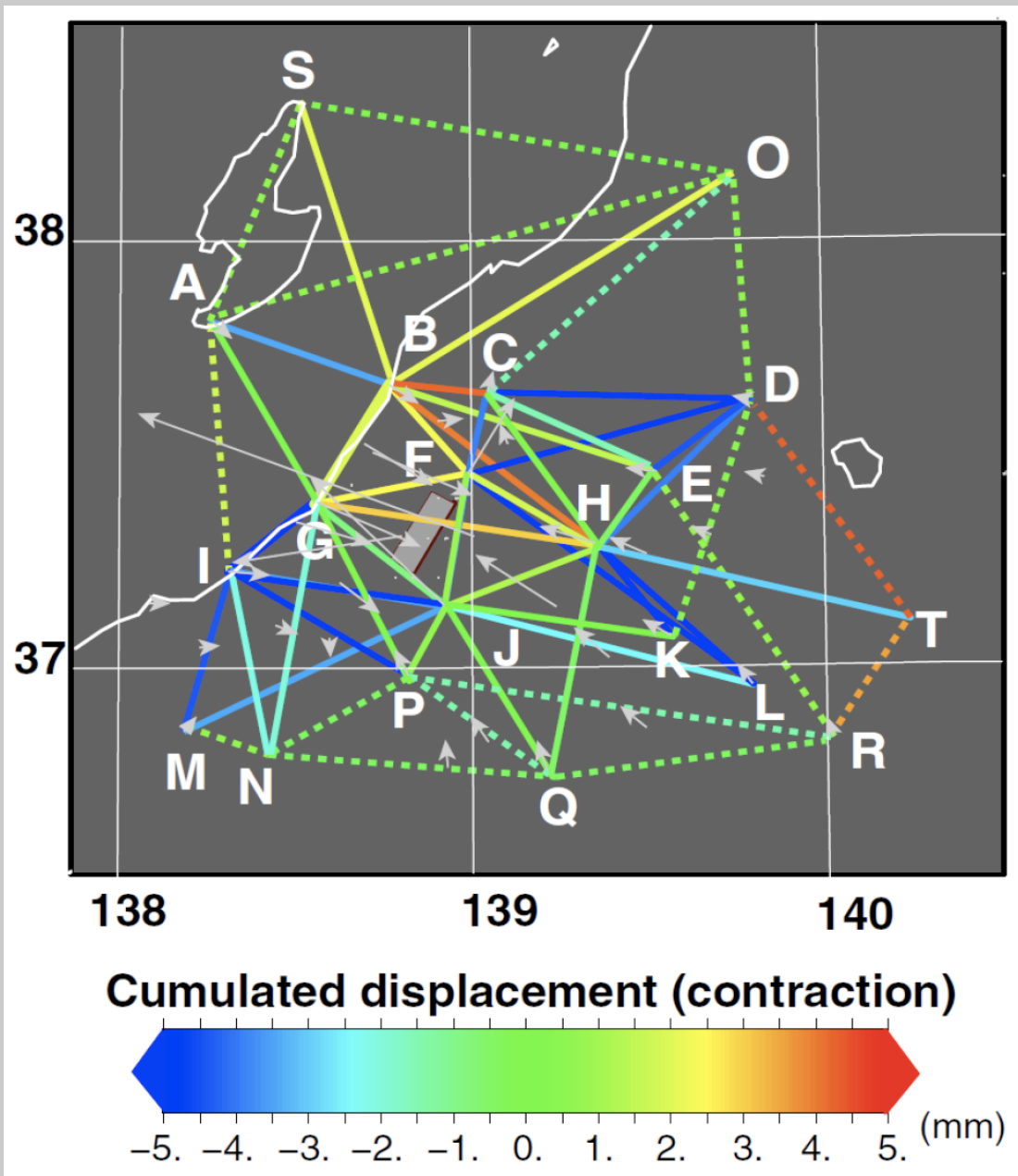




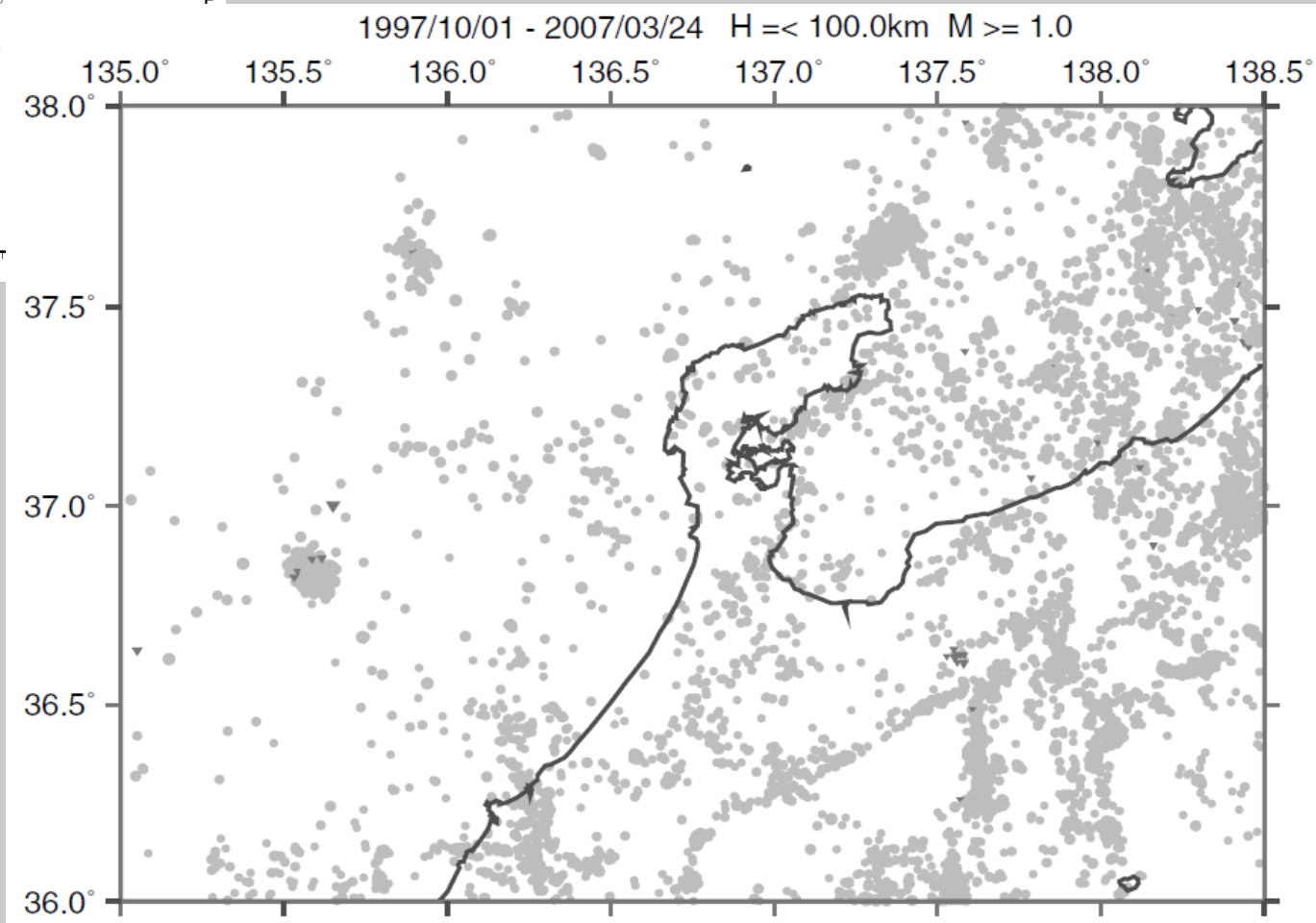
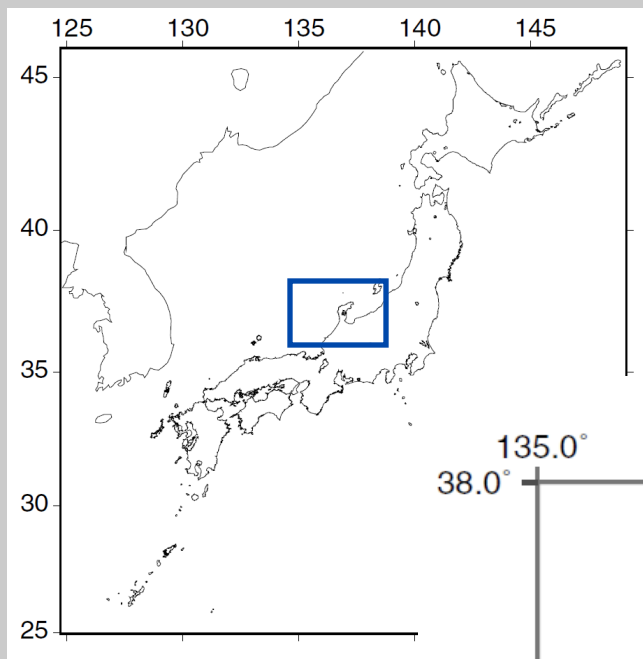


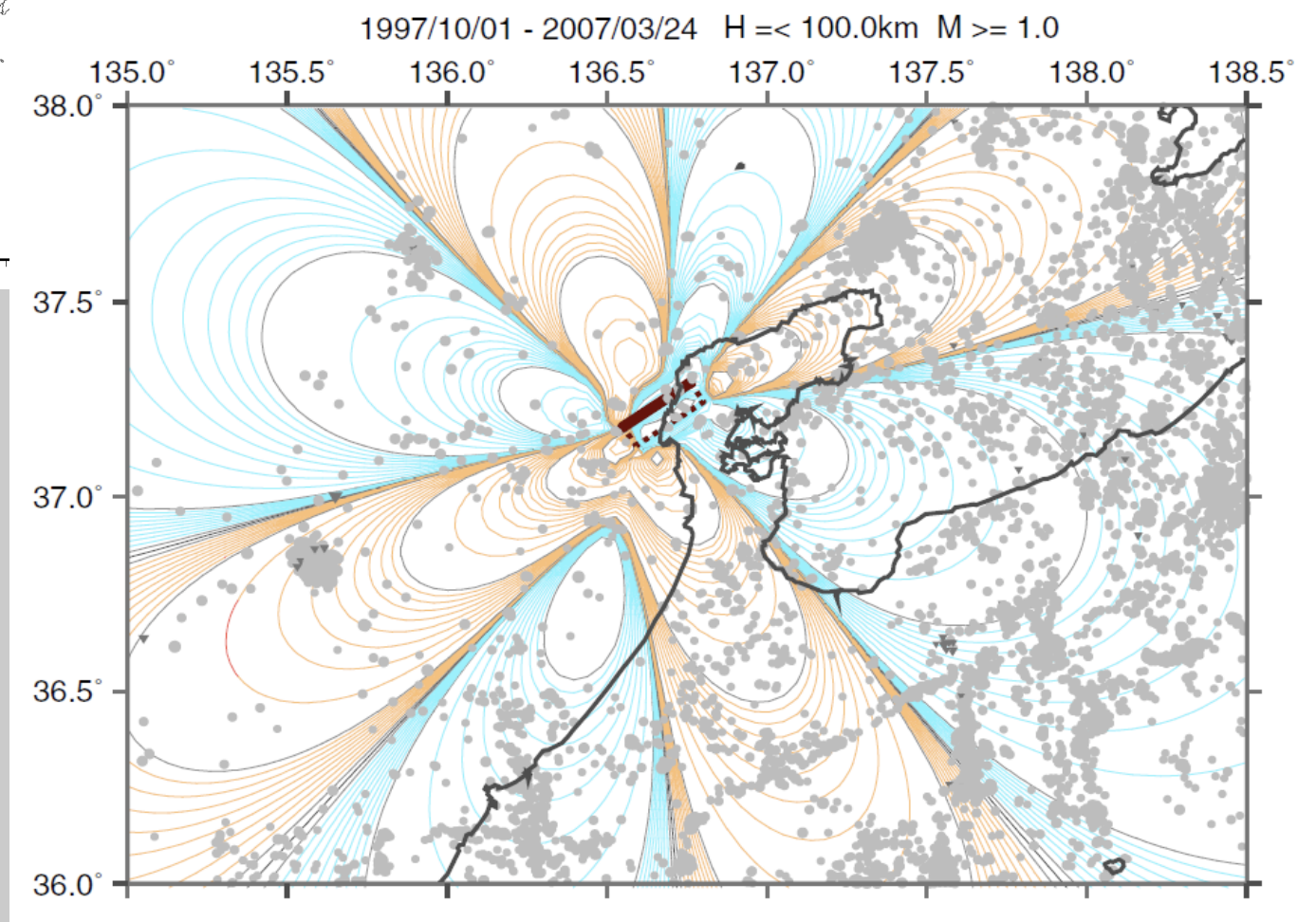
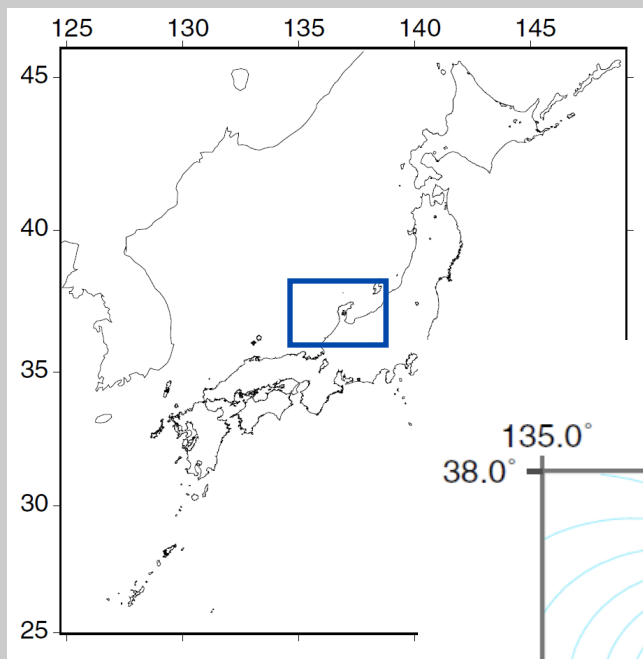


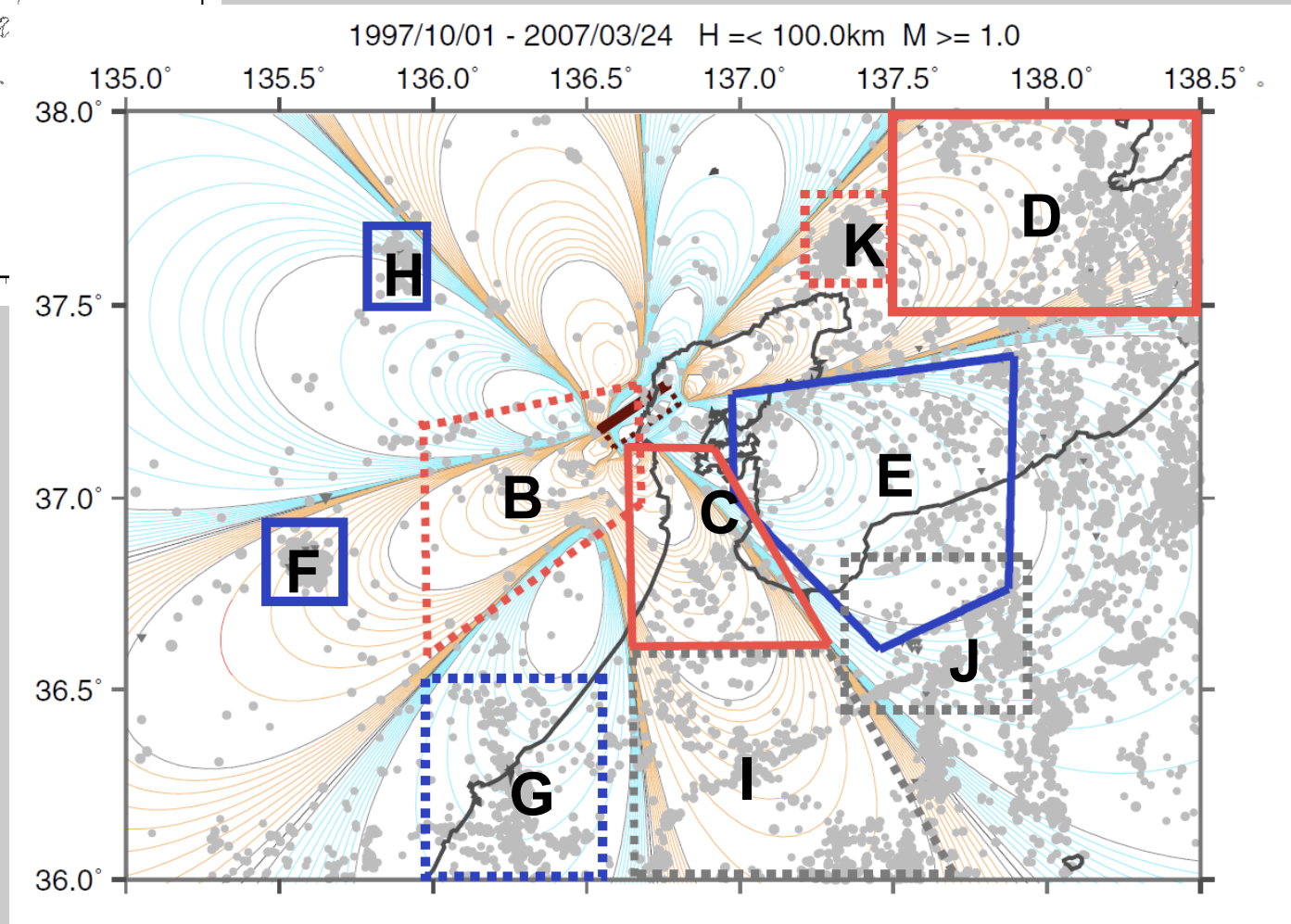
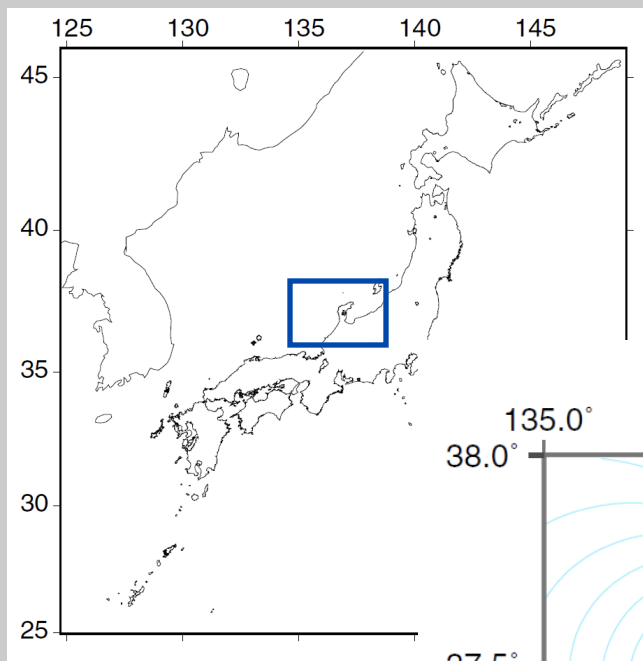


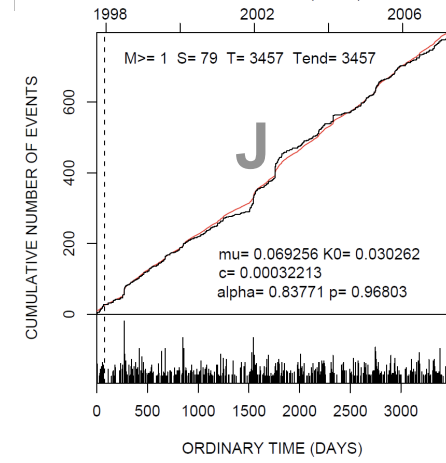
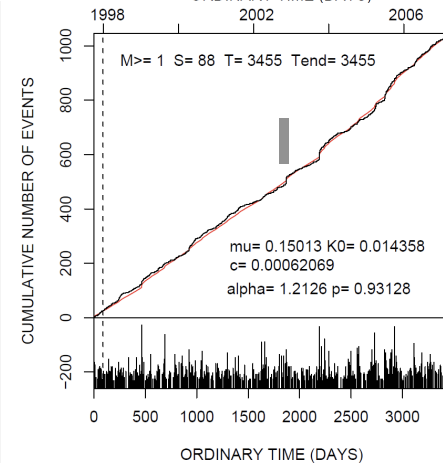
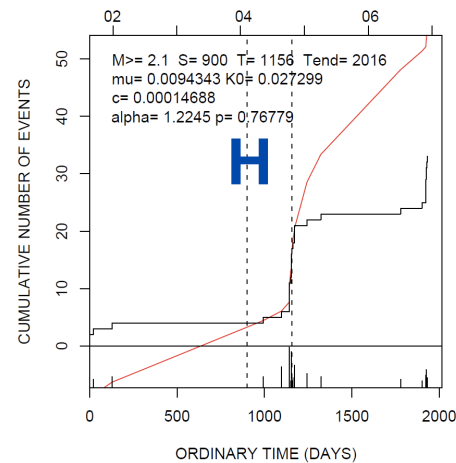
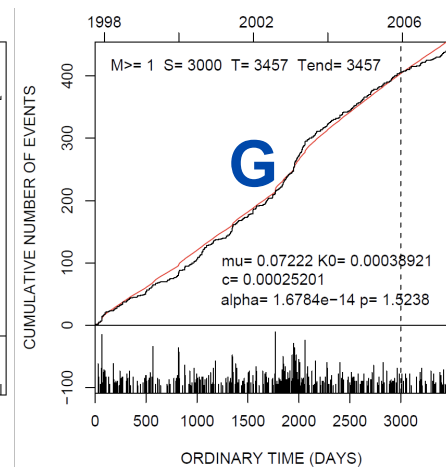
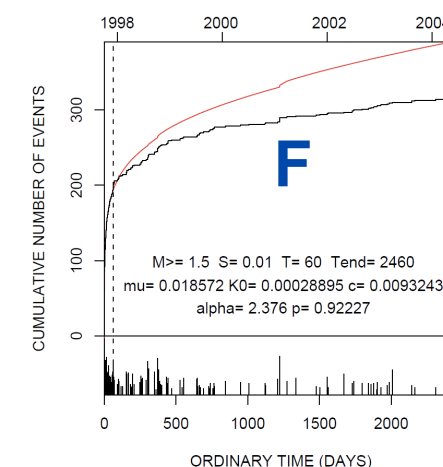
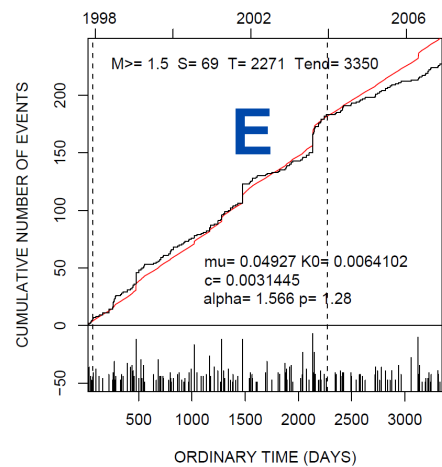
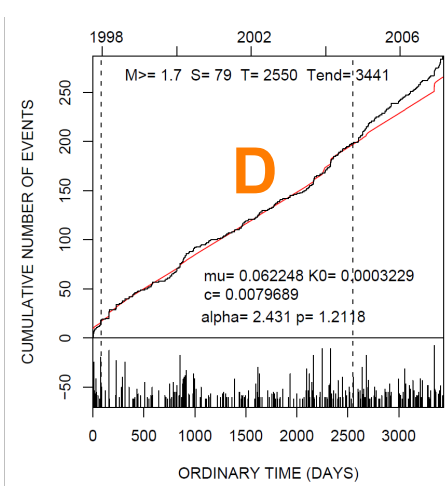
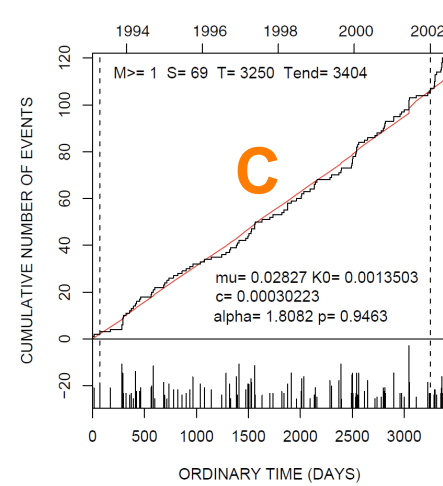
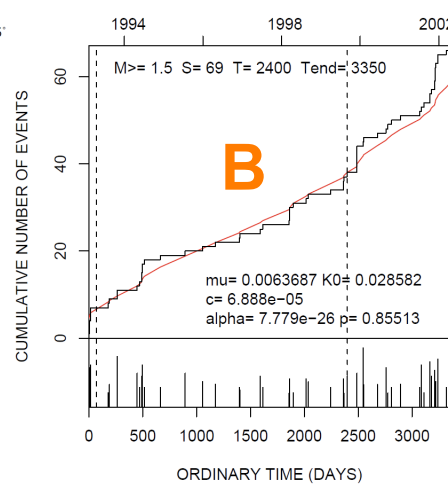
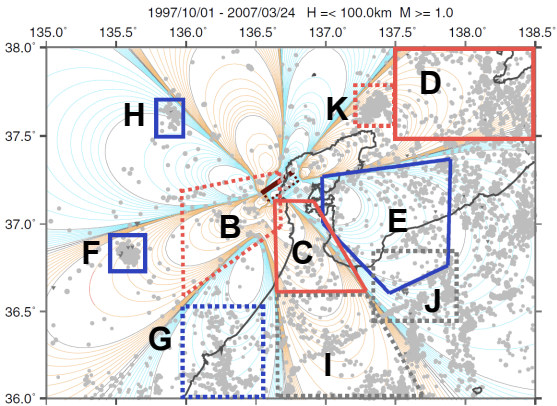


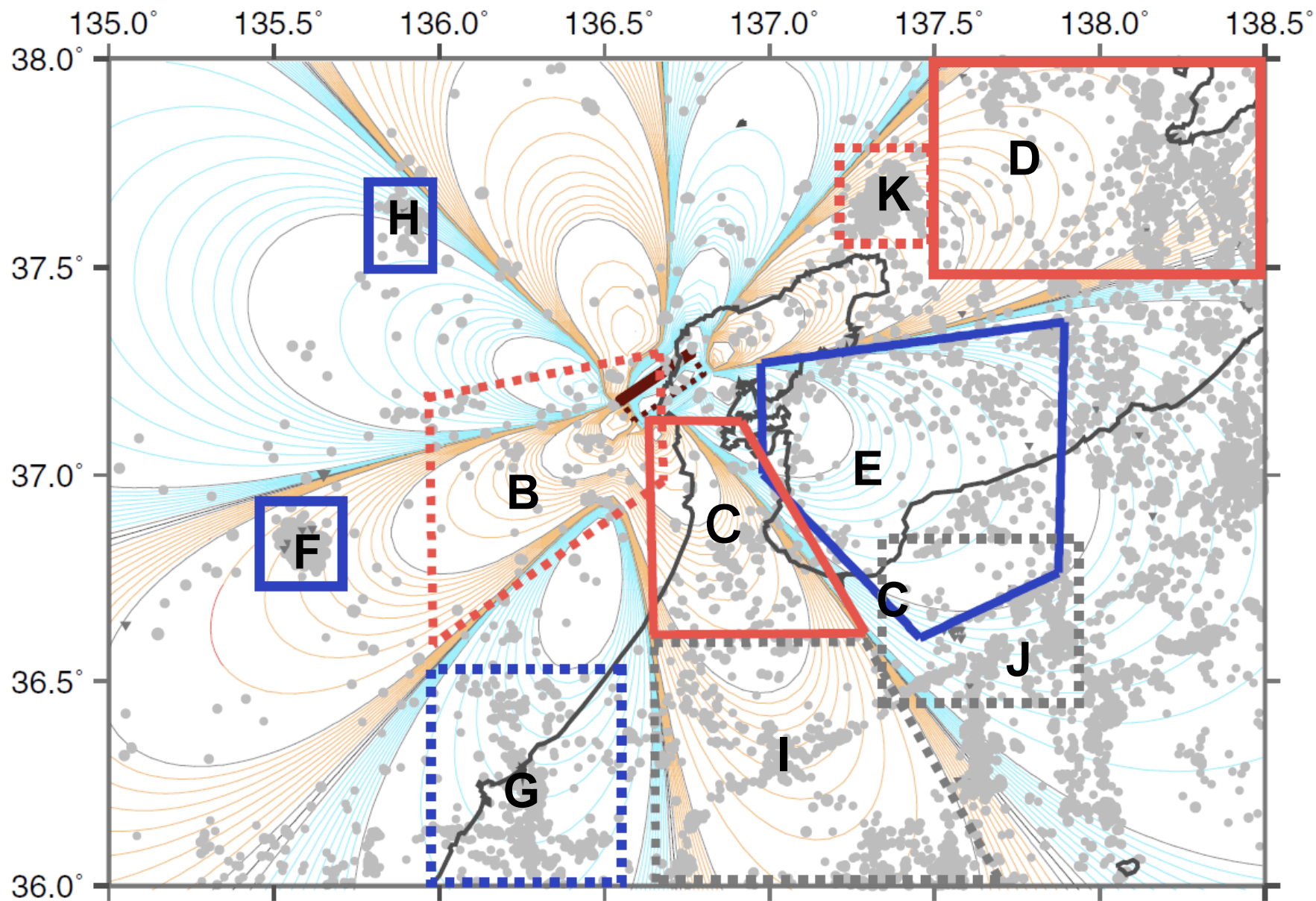
The March 2007 Noto Peninsula Earthquake

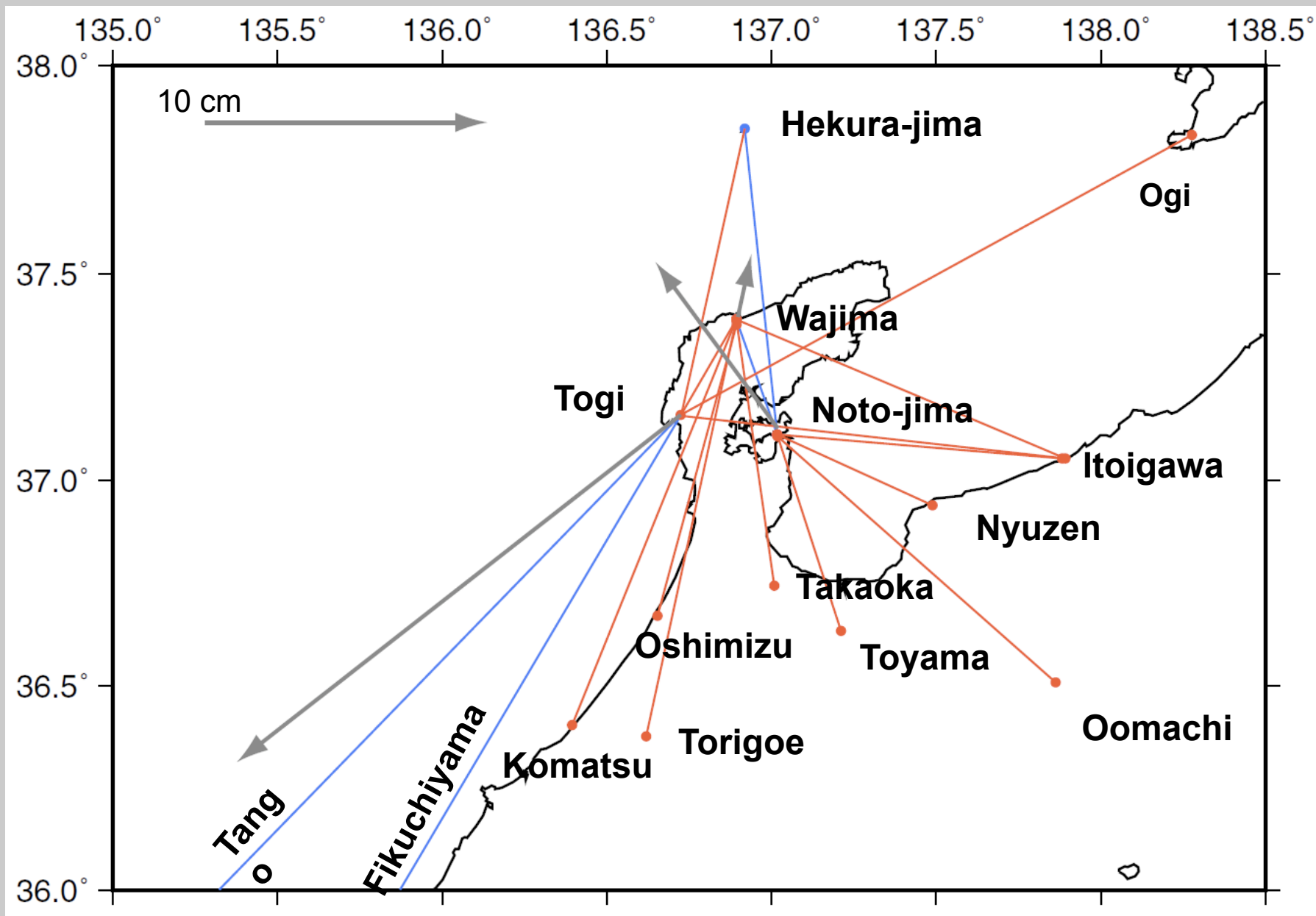


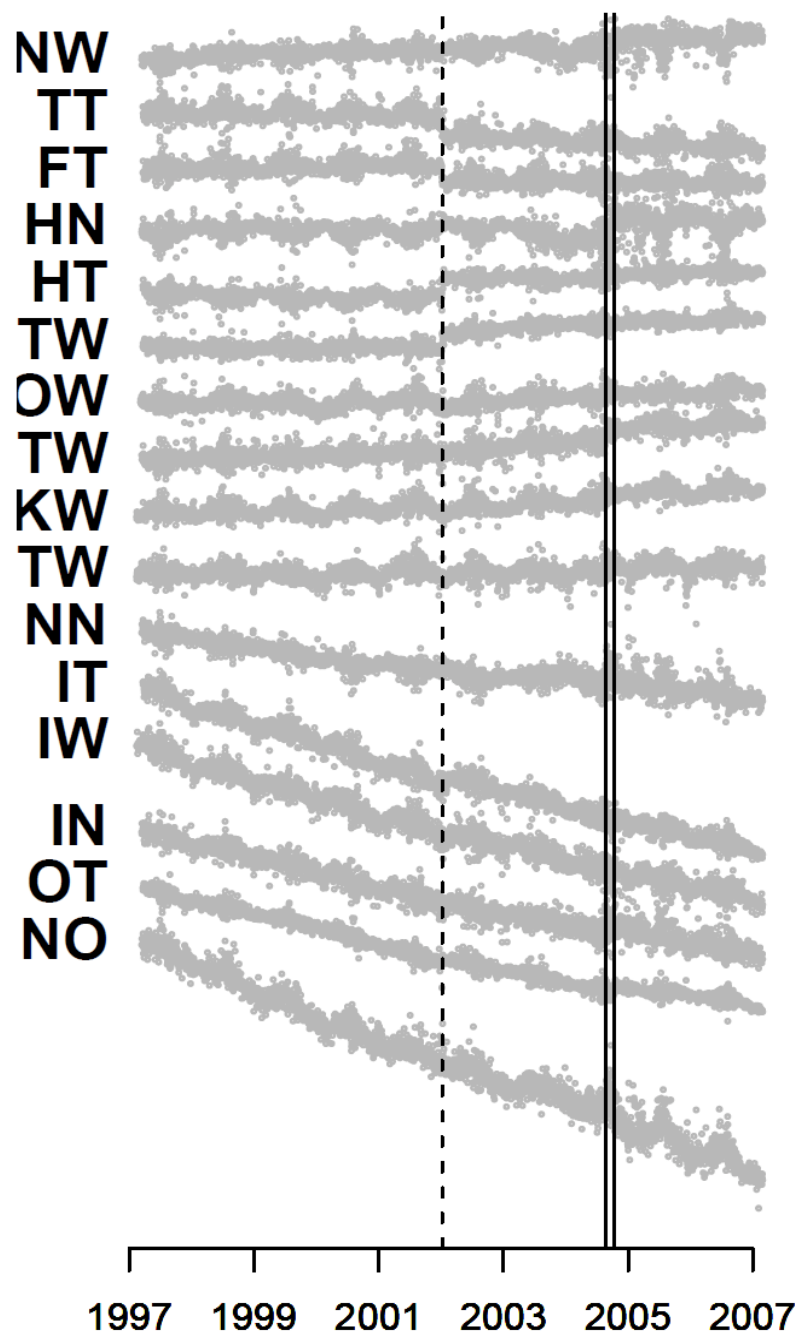


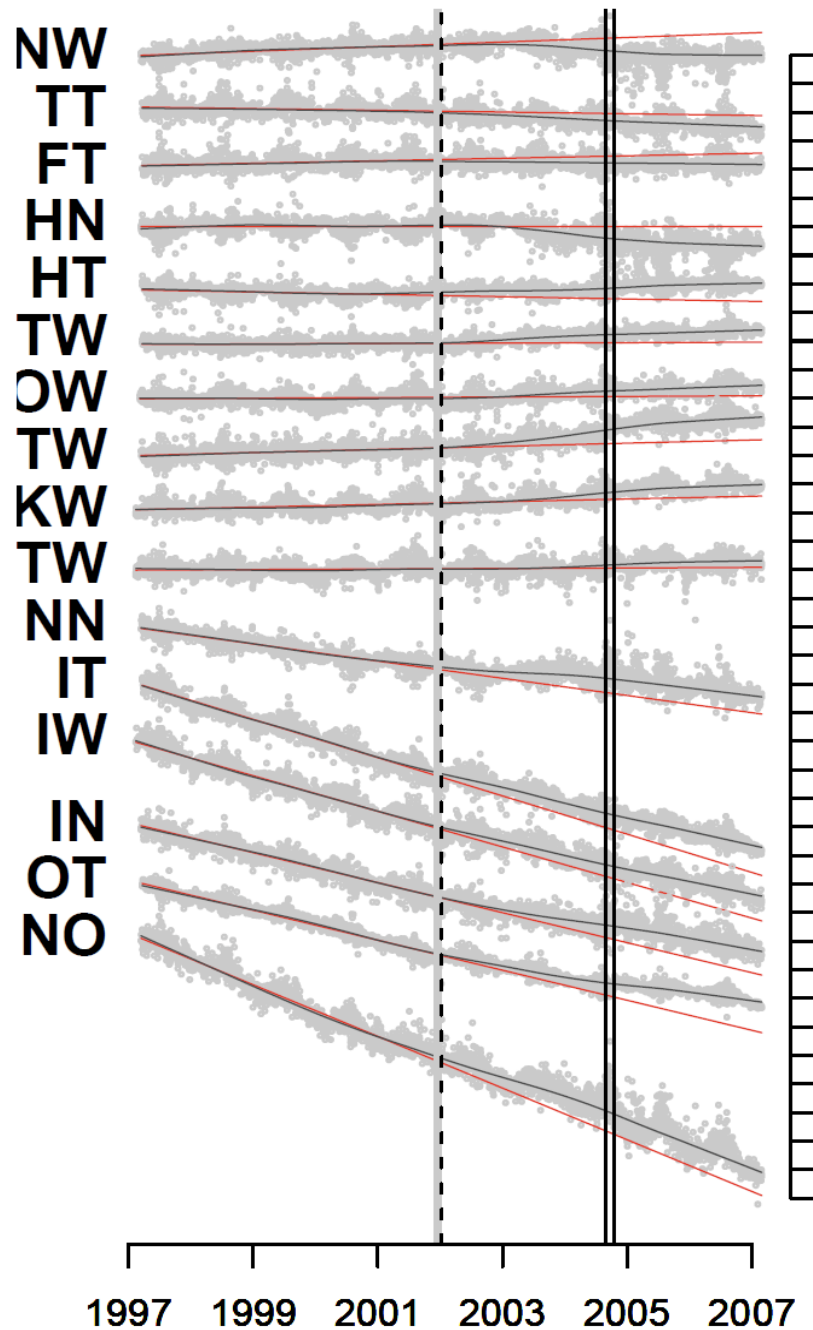
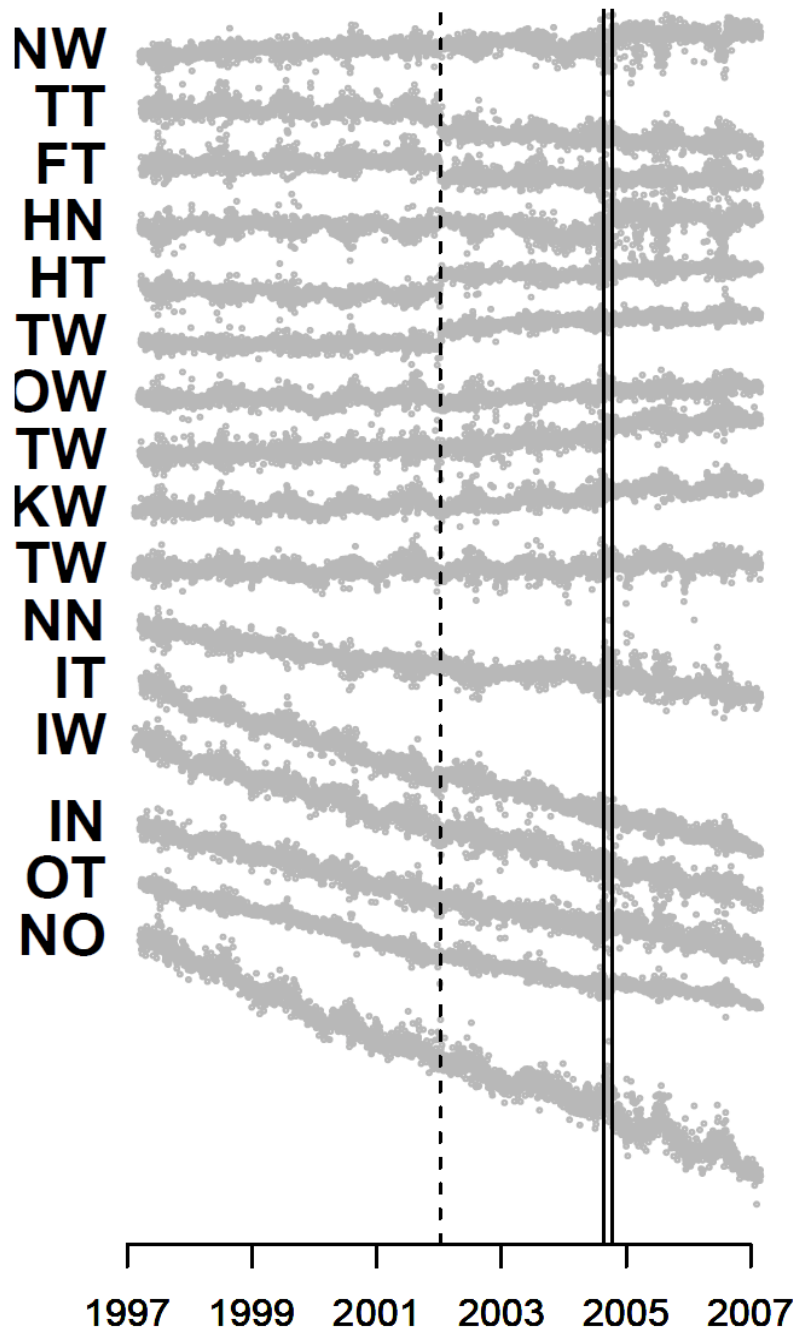


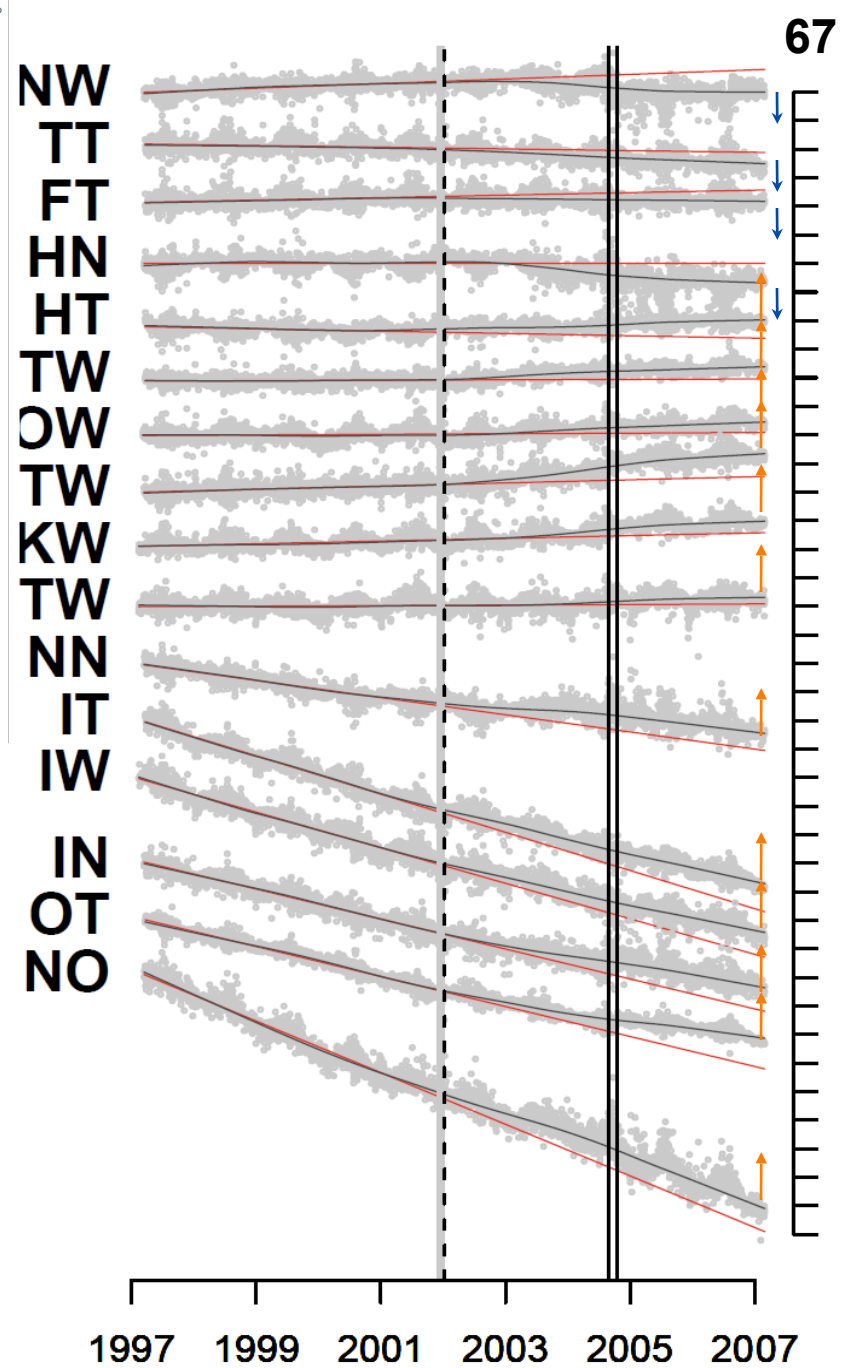
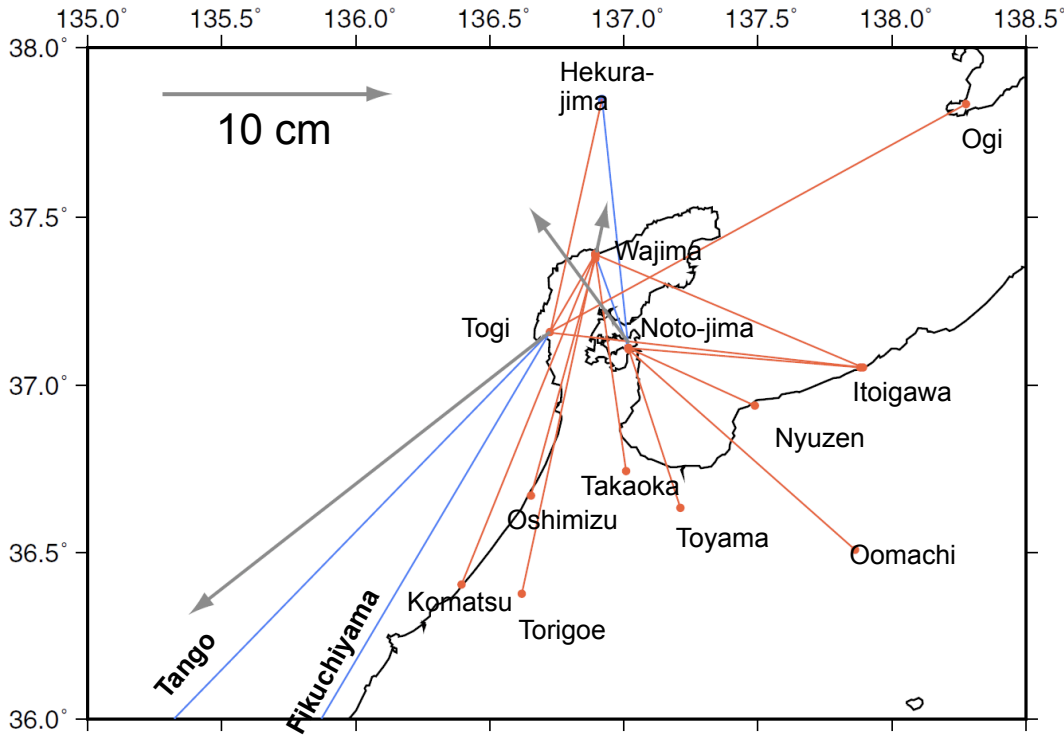


1997/10/01 - 2007/03/24 $H \leq 100.0\text{km}$ $M \geq 1.0$ 

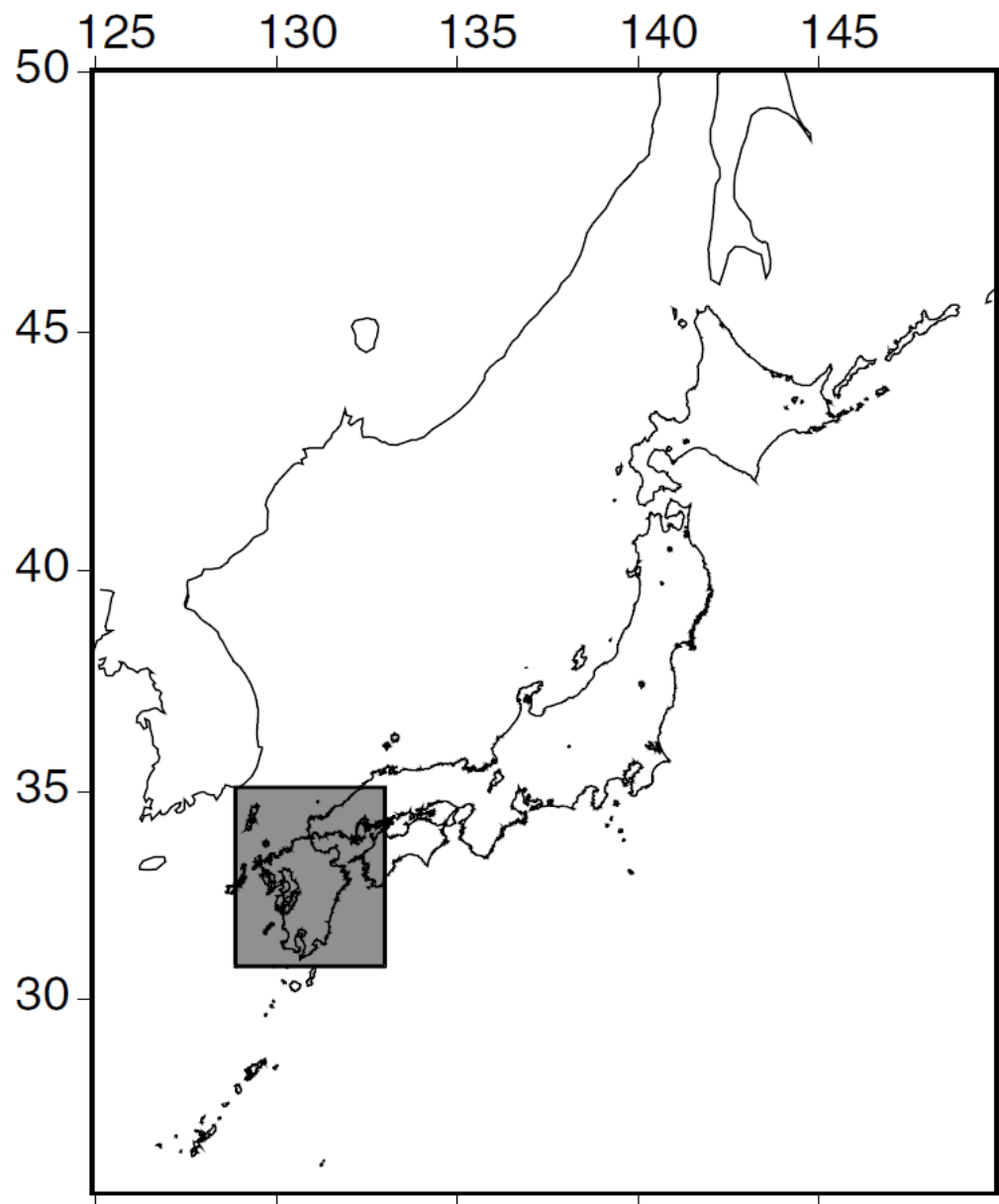






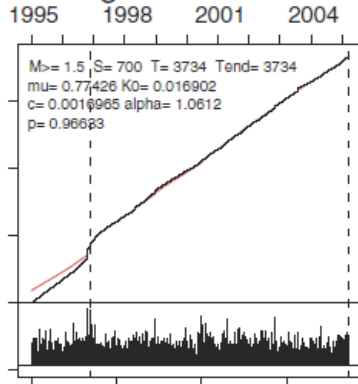


The 2005 Off coast of Western Fukuoka-Ken Earthquake

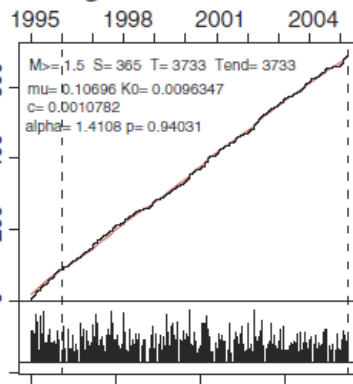


CUMULATIVE NUMBER OF EVENTS

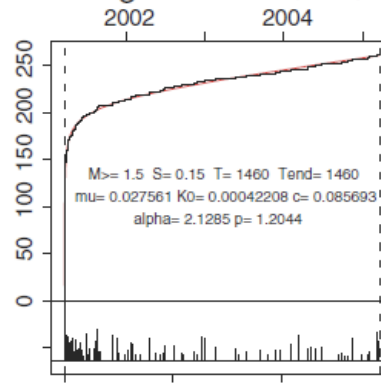
A region 宮崎県沖



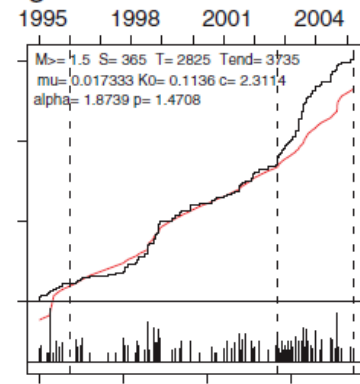
B region 長崎県南部地域



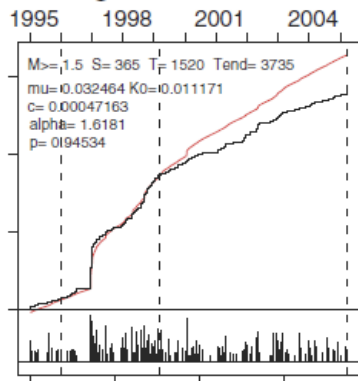
C region 芸予地震余震域



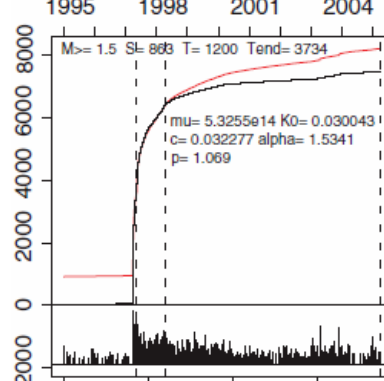
E region 福岡県警固断層付近



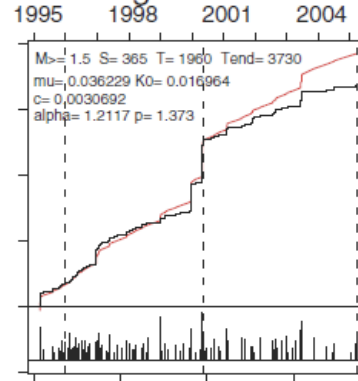
D region 周防灘



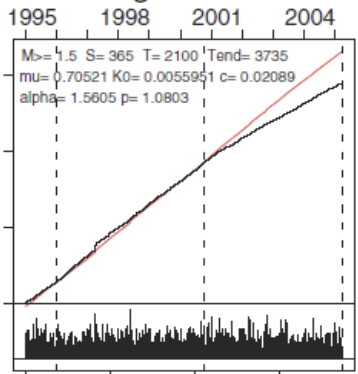
J region 鹿児島県西北部地震帯



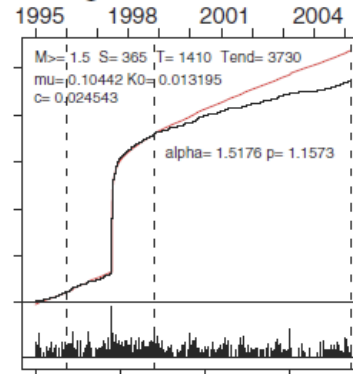
F region 別府付近



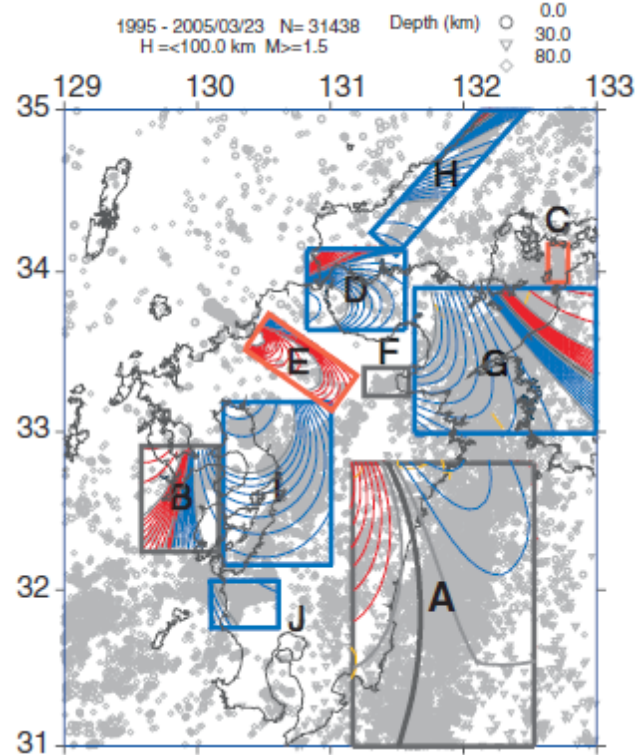
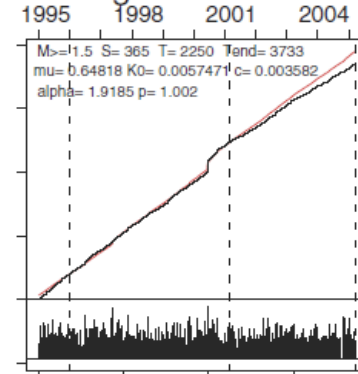
G region 大分県沖

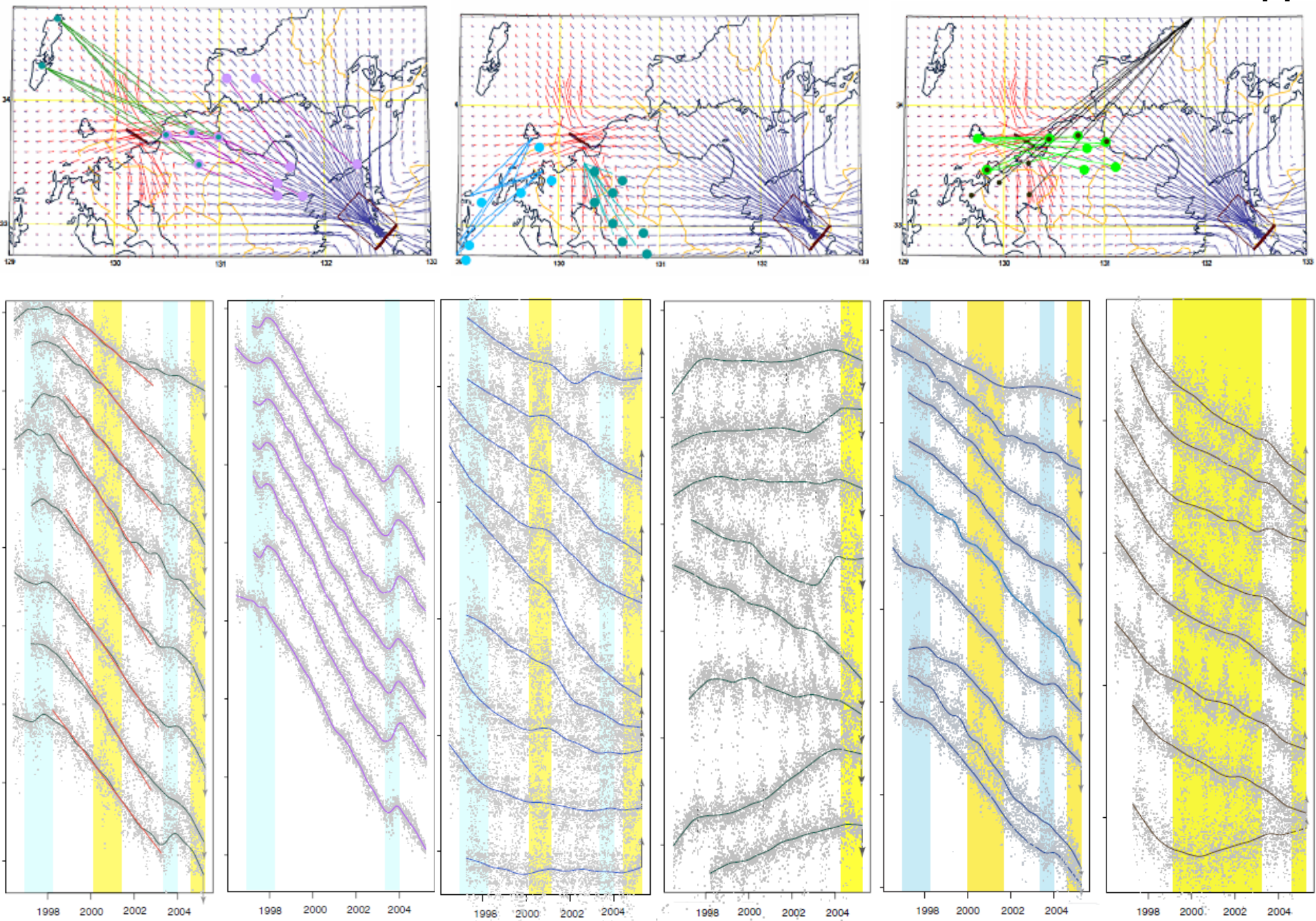


H region 山口島根県地震帯



I region 熊本県平野部





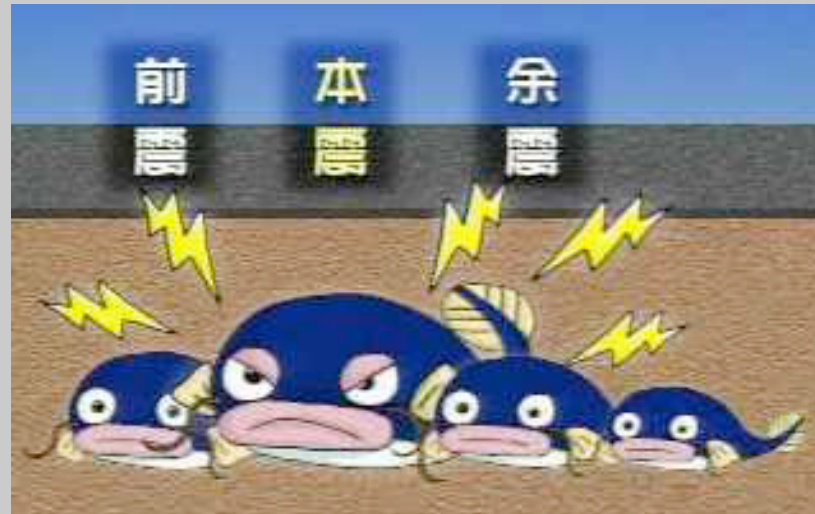
Summary with the ETAS model

- The ETAS model summarizes the seismicity due to triggering effect within the contiguous hierarchical complex faults.
- Deviations of the seismic activities from the predicted rate by the ETAS model are useful to detect regional stress changes.
- The respective deviations are explained by the changes in Coulomb failure stresses that are caused by seismic or aseismic slips.

Software and manuals are available at

[http://www.ism.ac.jp/~ogata/Ssg/
softwareE.html](http://www.ism.ac.jp/~ogata/Ssg/softwareE.html)

Thank you very much for listening



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